

• (I) Transmission

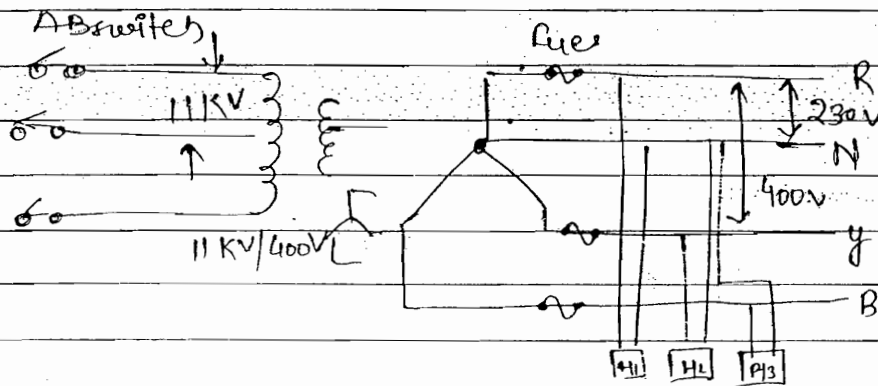
- ↳ Basics
- ↳ voltage / Reactive Power control
- ↳ Power flow through Tr-line
- ↳ Tr-line parameters
- ↳ " " performance
- ↳ Travelling waves
- ↳ Corona

• II

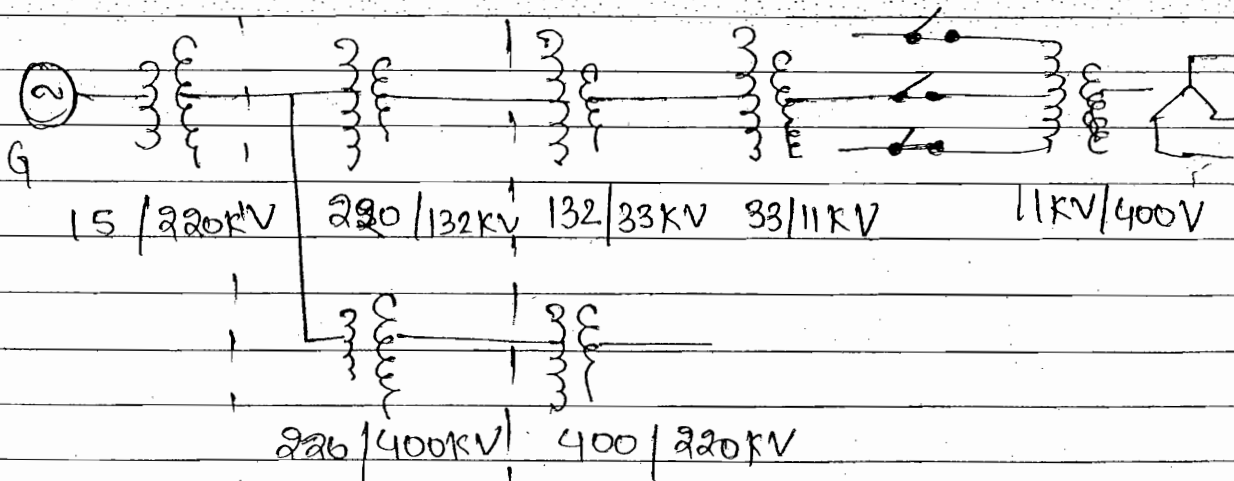
- ↳ Power generation
- ↳ Economic factors
- ↳ load freq. Control

• III.

- ↳ Switchgear and protection.



↳ When the power cut take place in any one phase, then AB switch are get open, after repairing fire AB switch again closed.



Generation Transmission Distribution

↳ RMS line (or) line-line voltage $[V_{ll}/V_l]$
 400V, 11kV, 33, 132, 220, 400, 765 kV

↳ RMS phase voltage (V_{ph}) $V_{ph} = 230V$

• Objective of Power System:-

- (1) Cost of electrical energy per unit must be minimum
 - Economic load dispatch
 - Economic factors
 - Generation Method.

- (2) Rated voltage and freq. has to be supplied to the consumer.
 - voltage control
 - load freq. control

- (3) Reliable power supply has to be available
 - Generation Method
 - Transmission
 - HVDC.

- (4) Most efficient protection system has to be available for faster identification and isolation of faulty section from the healthy section.
 - fault analysis
 - Switch gear and protection

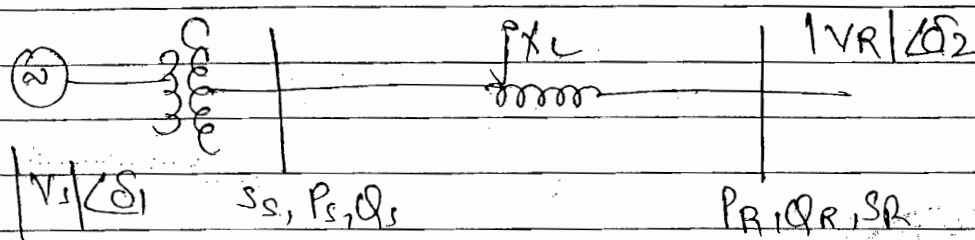
- (5) Most efficient generator has to be used which are to be most stable, should not lose synchronism under faulty condition
 - stability.

- (6) Flexible power transfer has to be available.
 - power cables.

• Transmission :- By using transmission line line elec. power is transferred from the remote generating station to the load centre where the electrical power is utilise.

• Objective:-

(1) Transmission line must be capable of transferring Maximum power with minimum transmission line losses and money.



$$P_s = P_R = \left| \frac{V_s \times V_R}{X_L} \right| \sin(\delta_1 - \delta_2)$$

$$\text{let } \delta = \delta_1 - \delta_2$$

$$P_R = \left| \frac{V_s V_R}{X_L} \right| \sin \delta \quad \text{Assume } |V_R| = |V_s|$$

$$P_R = \left| \frac{V_s^2}{X_L} \right| \sin \delta = P_{\max} \sin \delta \quad P_{\max} = \left| \frac{V_s^2}{X_L} \right|$$

$$P_{\max} = \left| \frac{V_s^2}{X_L} \right|$$

• Advantage of higher V_s :-

(1) $P_{\max} \propto V_s^2$. By $\uparrow V_s$ maximum power can be transferred.

$$\boxed{P_{\max} \propto V_s^2}$$

(2) Transmission losses are minimise
line

$$P = VI \cos \phi$$

$$I = \frac{P}{V \cos \phi}$$

$$P_{\text{loss}} = I^2 R$$

$$P_L = \frac{P^2 \cdot R}{V^2 \cos^2 \phi} \quad \text{--- (1)}$$

$$P_L \propto \frac{1}{V^2}$$

Condition:- $P, R, \cos \phi = \text{constant}$.

(3) Area of cross section and volume of conductor is minimised.

$$R = \frac{\rho l}{A} \quad A = \frac{\rho l}{R} = \frac{\rho l \cdot P^2}{V^2 \cos^2 \phi P_L} \quad [\text{from (1)}]$$

$$A \propto \frac{1}{V^2}$$

$$\text{Volume} = \rho \cdot A \cdot l \quad \left[K \propto A \propto \frac{1}{V^2} \right]$$

Condition:- $\rho, l, P, P_L, \cos \phi = \text{constant}$

(4) By reducing volume material requirement will be reduce. So the cost is minimised.

Because of above advantage we operating voltage of x-mission sys. is ranges from 11-33-132-220-400-765 KV.

Limitations:- (1) Beyond 765 KV more insulation required which increases the cost of x-mission

• Methods of Reducing X_L :

$$P_{\text{max}} \propto \frac{1}{X_L}$$

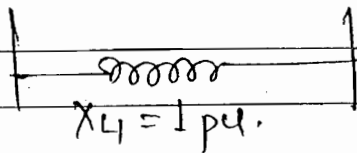
↳ By reducing X_L P_{max} is increased.

(a) By using parallel (or) double circuit line

Single line

$$|V_s| = 1$$

$$|V_R| = 1$$

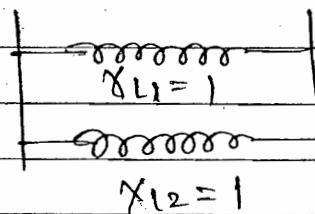


$$P_{max1} = \frac{|V_s|}{1} = 1 \text{ p.u.}$$

Double line

$$|V_s| = 1$$

$$|V_R| = 1$$



$$X_L = \frac{|X|}{1+1} = 0.5$$

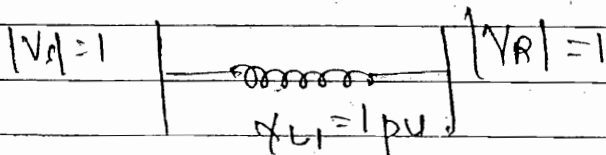
$$P_{max2} = \frac{|V_s|}{0.5} = 2$$

$$P_{max} \propto \frac{1}{X_L}$$

$$P_{max2} > P_{max1}$$

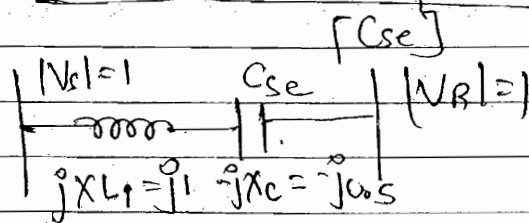
(b) By using series capacitor

Without Series Capacitor



$$P_{max1} = \frac{|V_s|}{1} = 1 \text{ p.u.}$$

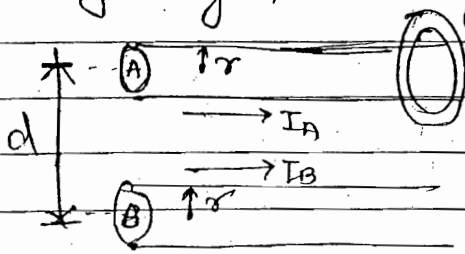
With Series Capacitor



$$X_L = 1 - 0.5 = 0.5$$

$$P_{max2} = \frac{|V_s|}{0.5} = 2 > P_{max1}$$

(c) By using Bundle Conductors :-



$$L_A = L_B = 2 \times 10^{-7} \ln \frac{d}{r} \quad \text{Obtaining}$$

$$X_L = 2\pi f L_A$$

$$P_{max} \propto \frac{1}{X_L} \quad \text{Bundle conductor}$$

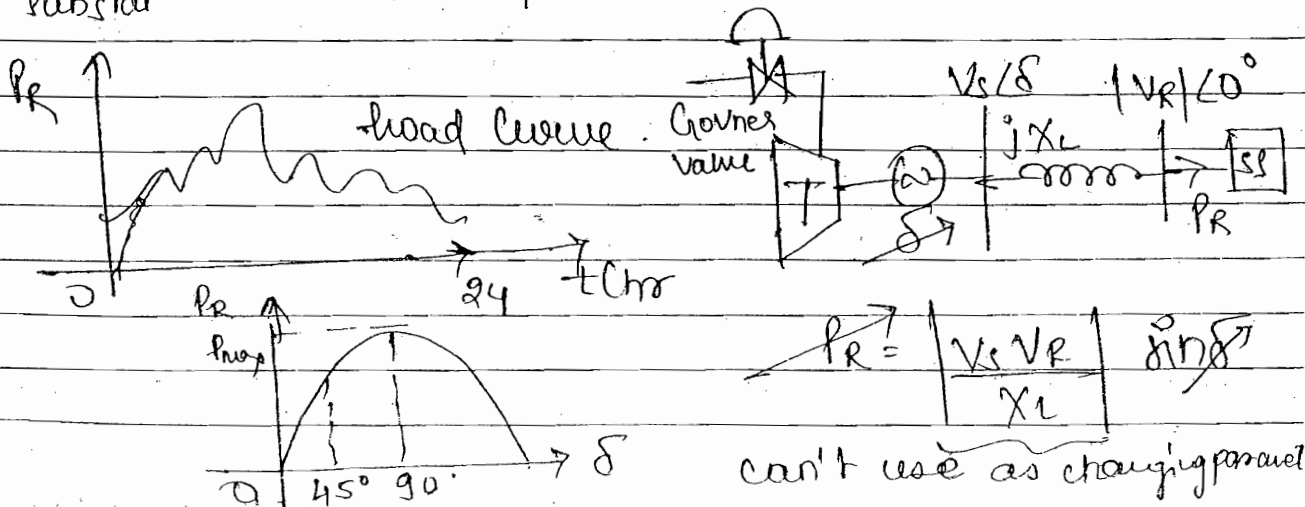
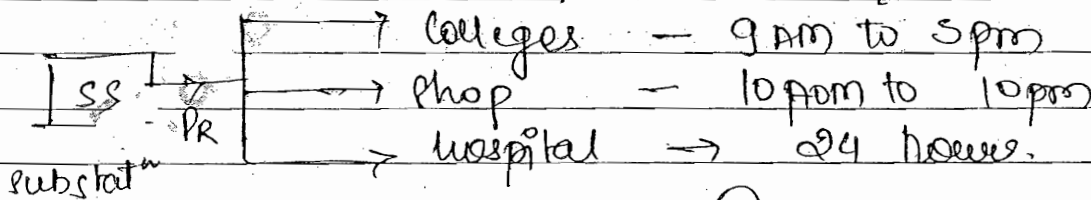
By $\downarrow X_L$ we can $\uparrow P_{max}$, we can $\downarrow X_L$ by $\downarrow L_A$.
 L_A can be $\downarrow$ by (1) $\downarrow d$ (2) $\uparrow r$.

0.7788r $\rightarrow$ Bundle conductor.

By $\downarrow d$ (diameter) $\rightarrow$ effect corona losses so we $\uparrow r$.

By using Bundle conductor effective radius of conductor is $\uparrow$ so that L and X_L are $\downarrow$.
 P_{max} increases.

$$P_s = P_R = P_{max} \sin \delta \quad P_R = \frac{|V_s|^2}{|X_L|} \sin \delta$$



• Importance of δ :-

- (1) load demand is continuously variable parameter w.r.t time. for supplying this variable load, load or power angle δ is selected as variable.

Practical value of $\delta \rightarrow 32^\circ$ to 45° due to stability limitation.

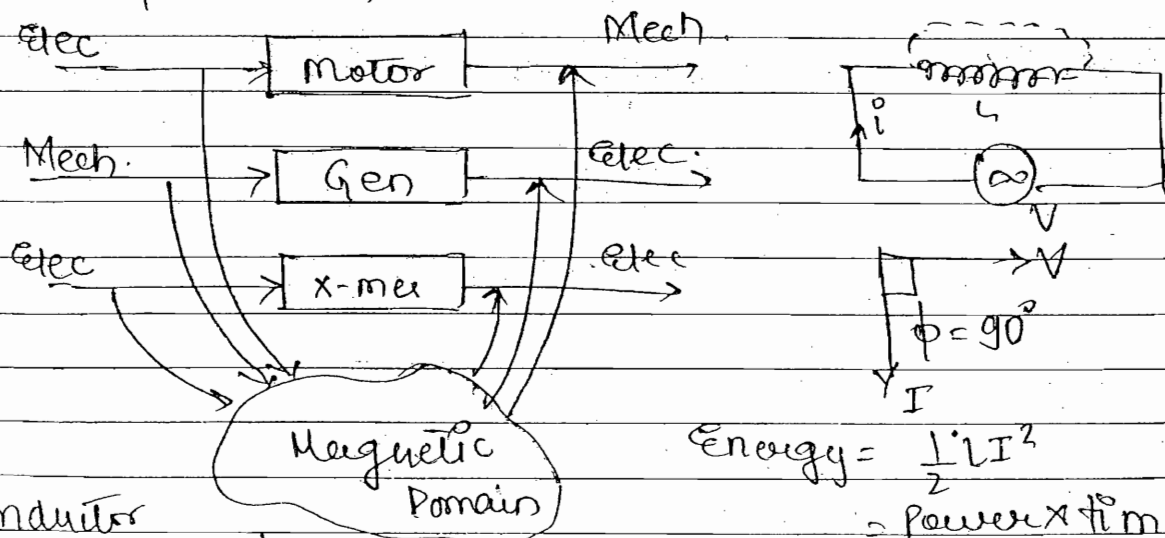
- (2) Voltage Regulation is to be minimum or zero.

$$\% V_{REG} = \frac{|V_s| - |V_R|}{|V_R|} \times 100.$$

$$\text{If } |V_s| = |V_R| \Rightarrow \boxed{V_{REG} = 0\%}$$

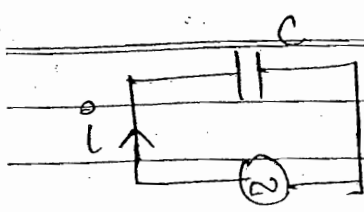
- For controlling the voltage reactive power of the supply has to be control

• Important of Reactive Power :-



Inductor
consume reactive
power for producing $\frac{1}{2} LI^2$
Magnetic domain

$$\begin{aligned} \Phi &= NI \sin \phi \\ &= VI \sin 90^\circ \\ &= VI \\ P &= VI \cos \phi \\ P &= VI \cos 90^\circ \\ &= 0 \end{aligned}$$



$$\text{Energy} = \frac{1}{2} CV^2$$

$$= \text{Power} \times \text{Time}$$

$$P = VI \cos \phi$$

$$= VI \cos 90^\circ$$

$$= 0$$

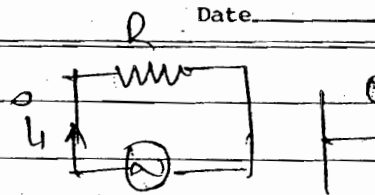
$$Q = VI \sin \phi$$

$$= VI \sin 90^\circ$$

$$Q = VI$$

$$\frac{1}{2} CV^2$$

Capacitor consume reactive power for storing energy



$$\text{Heat} = I^2 R t$$

$$= \text{Power} \times \text{Time}$$

$$P = VI \cos \phi$$

$$= VI \cos 0^\circ$$

$$P = VI$$

$$Q = VI \sin \phi$$

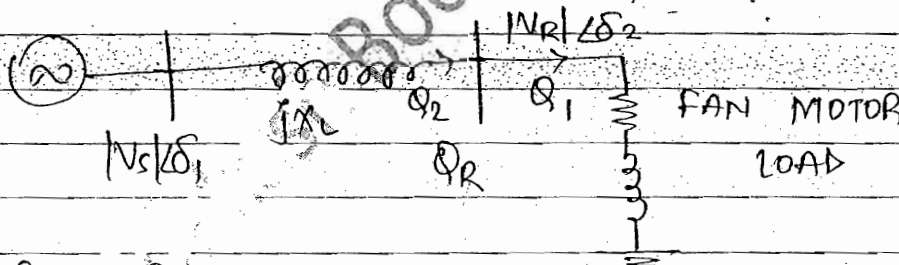
$$= VI \sin 0^\circ$$

$$Q = 0$$

$$I^2 R t$$

Resistor consume active power for giving heating effect.

• Relation Between Reactive power and Voltage



Q_1 = Reactive power demand by load

Q_2 = - " " " supply by source

$$Q_R = Q_1 - Q_2$$

$$Q_R = \left| \frac{V_s V_R}{X_L} \right| \cos (\delta_1 - \delta_2) = \left| \frac{V_R^2}{X_L} \right|$$

Assume $(\delta_1 - \delta_2) \approx 0$

$$Q_R = \left| \frac{V_s V_R}{X_L} \right| - \left| \frac{V_R^2}{X_L} \right|$$

$$V_R^2 - V_S V_R + X_L \cdot Q_R = 0$$

$$[ax^2 + bx + c = 0]$$

$$V_R = \frac{V_S}{2} \pm \frac{\sqrt{V_S^2 - 4X_L Q_R}}{2}$$

$$(1) \quad V_R = \frac{V_S}{2} + \frac{\sqrt{V_S^2 - 4X_L Q_R}}{2}$$

$$(a) \quad \text{If } Q_R = 0 \Rightarrow Q_1 = Q_2$$

$$V_R = V_S \Rightarrow V_{REG} = 0\%$$

$$(b) \quad \text{If } Q_R > 0 \Rightarrow Q_1 > Q_2$$

$$V_R < V_S$$

$$\Rightarrow V_{REG} = +ve$$

• Occur during Peak load
Tuning

$$(c) \quad \text{If } Q_R < 0 \Rightarrow Q_1 < Q_2$$

$$V_R > V_S$$

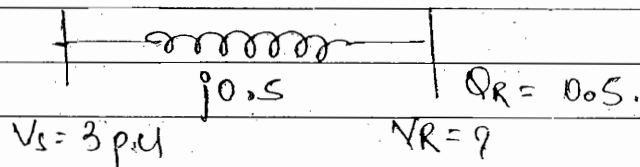
$$\Rightarrow V_{REG} = -ve$$

• Occur during DPP Peak
load tuning.
(fermantic effect)

$$(2) \quad V_R = \frac{V_S}{2} - \frac{\sqrt{V_S^2 - 4X_L Q_R}}{2} \quad \text{Not a valid eqn.}$$

Q A π -line has a reactance of 0.5 pu. operating at $V_S = 3$ pu. and receiving end Reactive power = 0.5 pu. find voltage drop across the line.

Solution



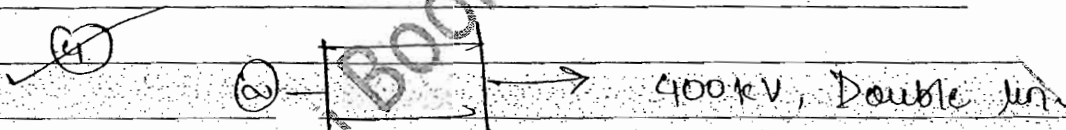
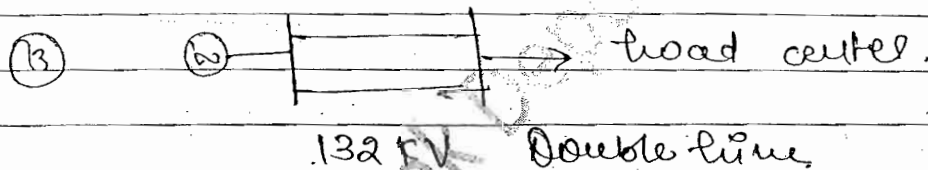
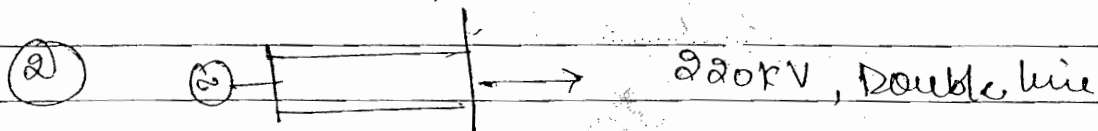
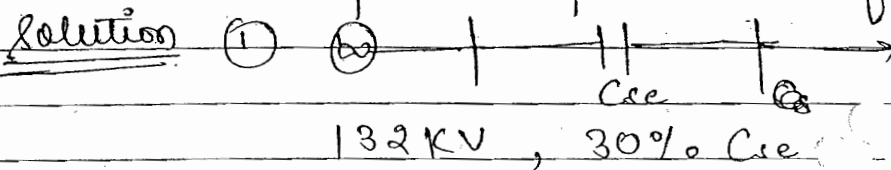
$$V_R = \frac{V_S}{2} + \frac{\sqrt{V_S^2 - 4X_L Q_R}}{2}$$

$$= \frac{3}{2} + \frac{\sqrt{3^2 - 4 \times 0.5 \times 0.5}}{2} = 2.914$$

$$\Delta V = V_s - V_R = 3 - 2.9 = 0.1 \text{ p.u.}$$

$$\% \text{ NREG} = \frac{V_s - V_R}{V_R} \times 100 = \frac{3 - 2.9}{2.9} \times 100 = 3.4\% \text{ Ag}$$

Q A Nuclear power gen. stat. is generating 500 MW to a load center which of the following is more suitable for this power transfer



Q A 133 kV X-line is delivering 10 MW. If the line voltage is change to 133.8 kV then the power deliver by line is

Solution $P = \frac{V_s^2}{X_L}$ $P \propto V_s^2$

$$\frac{P_1}{P_2} = \frac{V_{s1}^2}{V_{s2}^2}$$

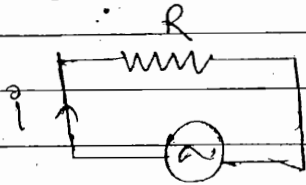
$$P_2 = P_1 \frac{V_{s2}^2}{V_{s1}^2} = 160 \text{ MW}$$

$$P_2 = \left(\frac{133.8}{133} \right)^2 \times 10 = 160 \text{ MW}$$

- Power Factor:- For controlling of the voltage reactive power has to be control which is control by using power factor compensator Methode like
 - (1) Shunt capacitor
 - (2) Shunt Reactor
 - (3) Syn. phase Modifier
 - (4) Tap changing xmer etc.

✓ It is a degree at which a given load (R_L, R_C) matches with that of pure resistive load.

(1) R-load:-



$$v = V_m \sin \omega t$$

$$i = \frac{V_m}{R} \sin \omega t$$

$$i = I_m \sin \omega t$$

• Instantaneous power,

$$P = v \cdot i$$

$$= V_m I_m \sin^2 \omega t$$

$$= \frac{V_m I_m}{2} (1 - \cos 2\omega t)$$

$$= \frac{V_m}{\sqrt{2}} \cdot \frac{I_m}{\sqrt{2}} (1 - \cos 2\omega t)$$

$$= V_{RMS} \cdot I_{RMS} (1 - \cos 2\omega t)$$

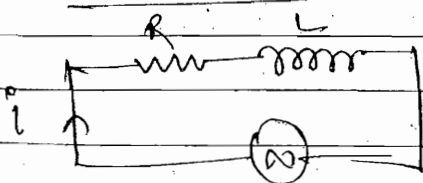
$$P = VI (1 - \cos 2\omega t)$$

• Average Power

$$P_{avg} = \frac{1}{2\pi} \int_0^{2\pi} p \cdot d(\omega t)$$

$$P_{avg} = VI = P_R$$

(2) RL load:-



$$v = V_m \sin \omega t$$

$$i = I_m \sin(\omega t - \phi)$$

$$I_m = \frac{V_m}{Z} = \frac{V_m}{\sqrt{R^2 + \omega^2 L^2}}$$

$$\phi = \tan^{-1} \left(\frac{\omega L}{R} \right)$$

• Instantaneous Power:-

$$p = v \cdot i = V_m I_m \sin \omega t \sin(\omega t - \phi)$$

$$= \frac{V_m I_m}{2} (\cos \phi - \cos(2\omega t - \phi))$$

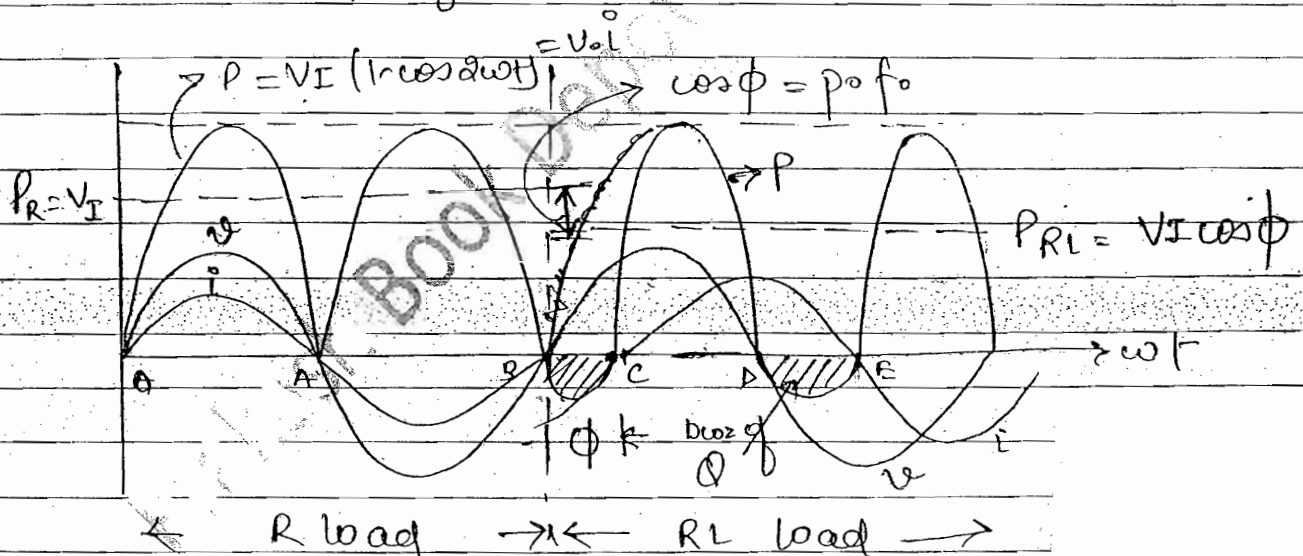
$$= \frac{V_m I_m}{2} (\cos(1 - \cos 2\omega t)) - \frac{V_m I_m \sin \phi \sin 2\omega t}{2}$$

$$P = P(1 - \cos 2\omega t) - Q \sin 2\omega t$$

where $P = VI \cos \phi$, $Q = VI \sin \phi$

• Avg. Power:-

$$P_{avg} = \frac{1}{2\pi} \int_0^{2\pi} p \cdot d(\omega t) \quad [P_{avg} = VI \cos \phi = P_{RL}]$$

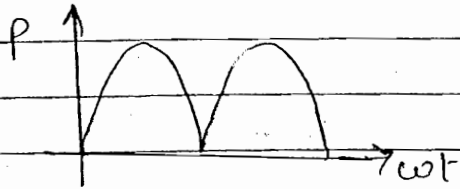
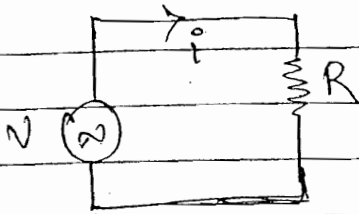


$$\frac{P_{RL}}{P_R} = \frac{VI \cos \phi}{VI} = \cos \phi = p_0 f$$

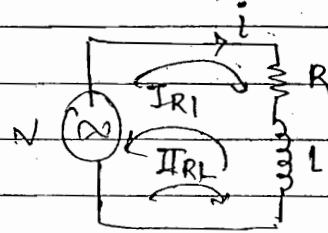
→ average power of RL load reduce due to
posi-ve power. (This is due to reactive power)

→ In-ve portion power deliver by L to source

• R-load :-

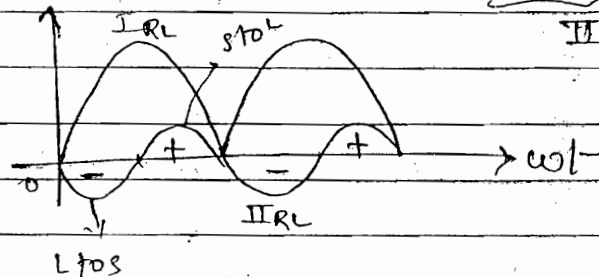


• RL load :-

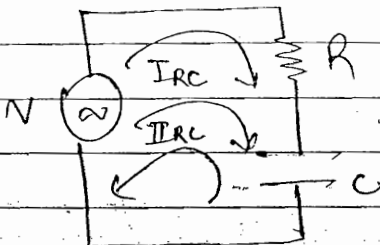


$$P = P(1 - \cos 2\omega t) - Q \sin 2\omega t$$

I_{RC}

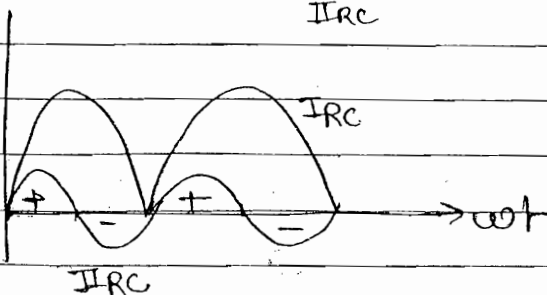


• RC load :-

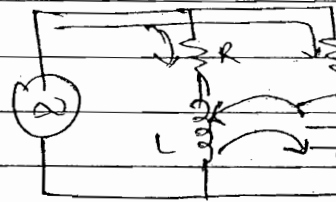


$$P = V_i I_i = P(1 - \cos 2\omega t) + Q \sin 2\omega t$$

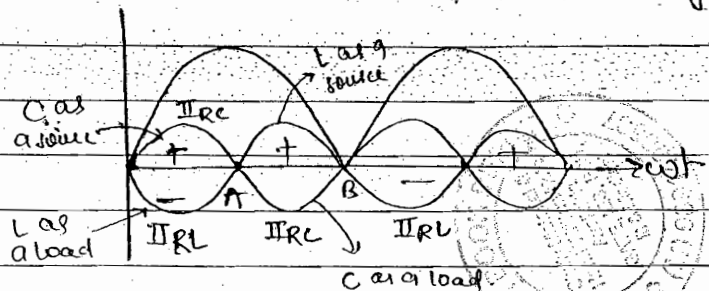
I_{RC}



• RL & RC combine ! :-



power exchange b/w L & C by some time delay



	(Deliver) Source	(Absorb) Sink
L	leading VARs	lagging VARs
C	lagging VARs	leading VARs

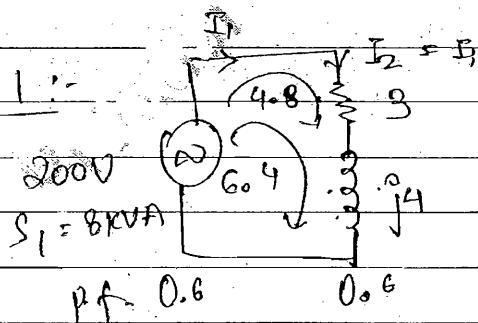
→ Inductor absorb lagging power and deliver leading power
 → Capacitor absorb leading power and deliver lagging power

- If the voltage regulation is +ve indicates lagging VAR's demand is more than supply. By using a capacitor lagging VAR's can be compensated so that voltage regulation is zero and improvement of power factor can be achieved.
- If the voltage regulation is -ve indicates lagging VAR's demand is less than supply. For absorbing this excess lagging VAR's inductor or shunt reactor has to be used so that zero voltage regulation can be achieved.

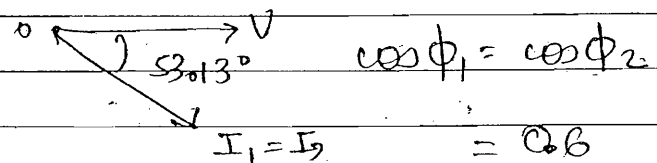
Q1 A single- ϕ Induction Motor having impedance of $3+j4$ is connected to 200V supply. Find currents and power and power factor of the load and source.

Q2 If the capacitance of $j6.25$ is connected parallel to I/M. Find currents, p.f. and power across each device.

Solution 1 :-



$$I_1 = I_2 = \frac{200}{3+j4} = 40 \angle -53.13^\circ$$



$$S_1 = S_2 = V \cdot I_1^*$$

$$= 200 \times (40 \angle -53.13^\circ)^*$$

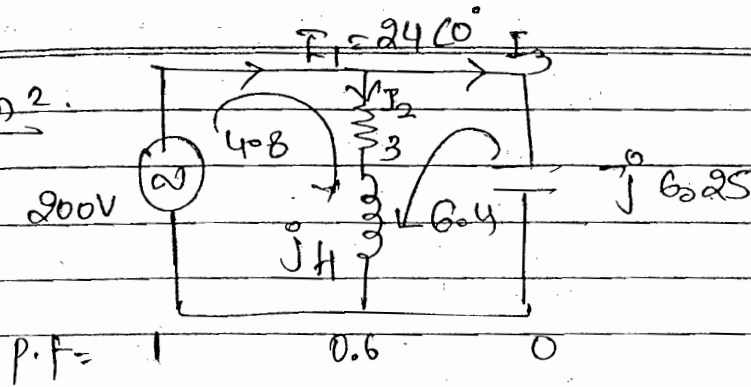
$$= (408 + j6.4) \text{ kVA}$$

$$P_2 = 408 \text{ kW}$$

$$Q_2 = 6.4 \text{ kVAR}$$

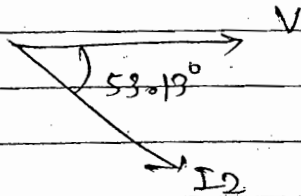
$$|S_1| = 8 \text{ kVA}$$

Solution 2.



$$I_2 = \frac{200}{3 + j4}$$

$$= 40 \angle -53.13^\circ$$



$$\cos \phi = \cos 53.13^\circ = 0.6$$

$$S_2 = V_a I_2^* = 200 \times (40 \angle -53.13^\circ)^*$$

$$= (40.8 + j6.4) \text{ KVA}$$

$$I_3 = \frac{200}{-j6.25} \Rightarrow 32 \angle 90^\circ$$

$$\cos \phi_3 = \cos 90^\circ = 0$$

$$S_3 = V \cdot I_3^* = 200 \times 32 \angle 90^\circ$$

$$= -j6.4 \text{ KVA}$$

$$= 0 - j6.4 \text{ KVAR}$$

$$I_1 = I_2 + I_3$$

$$= 40 \angle -53.13^\circ + 32 \angle 90^\circ$$

$$= 24 \angle 0^\circ$$

$$\cos \phi_1 = \cos 0^\circ = 1$$

$$S_1 = V \cdot I_1^*$$

$$= 200 \times 24 \angle 0^\circ$$

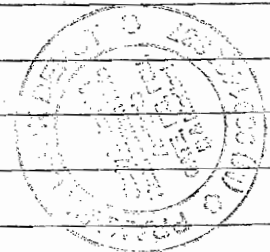
$$= 40.8 \text{ KW}$$

$$= 40.8 + j0 \text{ KVA}$$

$$|S_1| = 40.8 \text{ KVA}$$

• Advantage of Higher P.F.:-

- (1) Current through x-line reduce
- (2) X-mission η improves.
- (3) Power loss is reduce
- (4) Voltage regulation can be minimised
- (5) Rated of generator is minimised



Date 6/7/2014

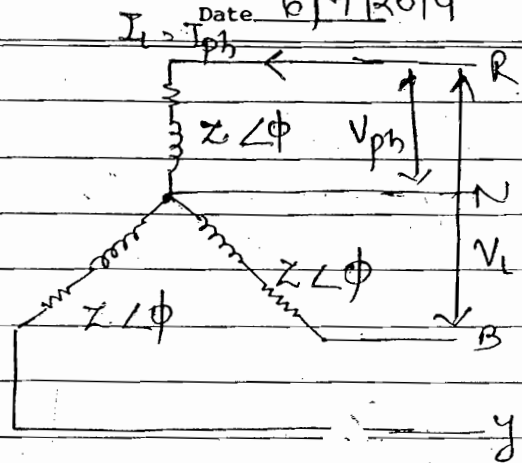
• Star

$$V_{ph} = \frac{V_L}{\sqrt{3}}, \quad I_{ph} = I_L$$

$$P_{3\phi} = \sqrt{3} V_L I_L \cos \phi$$

$$= \frac{|V_L|^2}{|Z|} \cos \phi$$

$$Q_{3\phi} = \frac{|V_L|^2}{|Z|} \sin \phi$$



• Delta

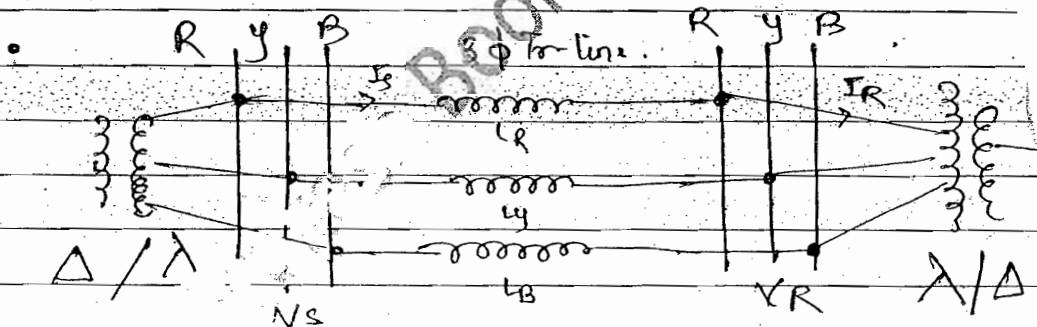
$$V_{ph} = V_L, \quad I_{ph} = I_L / \sqrt{3}$$

$$P_{3\phi} = \sqrt{3} V_L I_L \cos \phi$$

$$= 3 \frac{|V_L|^2}{|Z|} \cos \phi$$

$$Q_{3\phi} = 3 \frac{|V_L|^2}{|Z|} \sin \phi$$

$$Q_{3\phi} = P_{3\phi} \cdot \tan \phi$$



→ Y & Δ are neither series connected nor parallel connected.

R, L, C, G
or
A, B, C, D

3 φ Tr-line are represented

per phase only

OX 1

$$V_s = A V_R + B I_R$$

$\downarrow$ $\downarrow$ $\downarrow$ $\downarrow$
 ? ph ph ?

→ convert all terms in phase values.

$$V_{sph} = A \frac{V_R}{\sqrt{3}} + B \cdot I_R$$

By VR related
to $\sqrt{3}$. I_R
remain same.

$$V_{SL} = \sqrt{3} V_{sph}$$

$$I_s = C V_R + D I_R$$

$\downarrow$ $\downarrow$ $\downarrow$ $\downarrow$ $\downarrow$
 ? ph ϕ^L ph ?

$$I_{sph} = C \frac{V_R}{\sqrt{3}} + D \cdot I_R$$

$$I_{SL} = I_{sph}$$

As VR related to $\sqrt{3}$. $I_{SL} = I_{sph}$

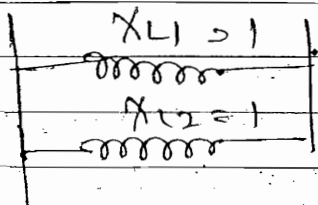
ex-2 $P_R = \left| \frac{V_s V_R}{X_L} \right| \sin \delta$

$$P_{Rph} = \left| \frac{V_{sph} \cdot V_{Rph}}{X_{Lph}} \right| \sin \delta$$

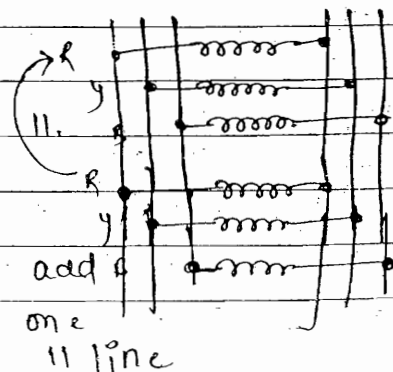
$$P_{R,3\phi} = 3 \left| \frac{V_{sph} \cdot V_{Rph}}{X_{Lph}} \right| \sin \delta = 3 \left| \frac{\frac{V_{SL}}{\sqrt{3}} \cdot \frac{V_{RL}}{\sqrt{3}}}{X_{Lph}} \right| \sin \delta$$

$$P_{R,3\phi} = \left| \frac{V_{SL} \cdot V_{RL}}{X_{Lph}} \right| \sin \delta$$

- voltages are always line values whereas R, L, C, G, A, B, C, D parameters are always in per phase values. in 3 ϕ



$$X = \frac{1 \times 1}{1+1} = 0.5$$



• Methods of Reactive Power Control :-

Receiving End Methods

- (1) Shunt Capacitor
- (2) Shunt Reactor
- (3) Series Capacitor
- (4) Syn. Phase Modifier (SPM)

(5) on-load Tap changing (OLTC) X-mes

(6) Boosters X-mes

Source End Method

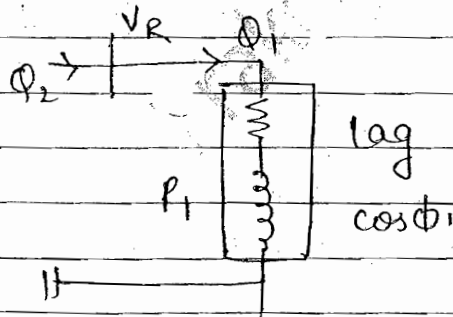
- (1) Gen. Excitation Control

(1) Shunt Capacitor Compensation :-

Shunt Capacitor is used for :-

- (1) Improve voltage regulation
- (2) Improve power factor
- (3) Improve sys stability. By reducing load angle δ .

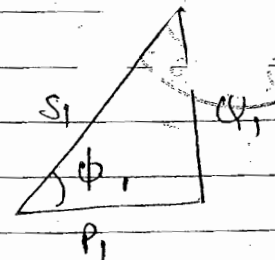
(a) without Shunt Capacitor :-



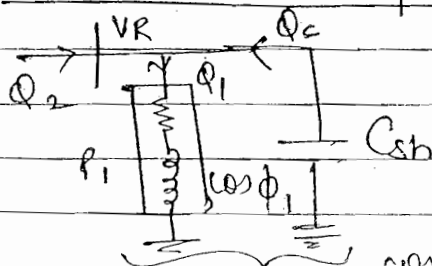
Assume

$$Q_1 > Q_2$$

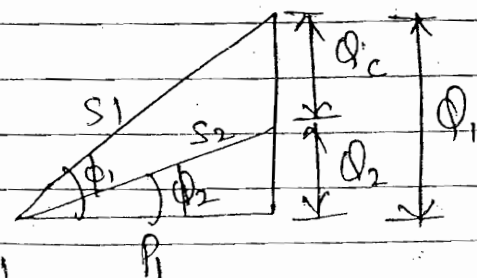
$$V_R < V_S$$



(b) With Shunt Capacitor :-



$$\cos \phi_2 > \cos \phi_1$$



For pure capacitor $\phi = 90^\circ$, $I_{ph} = \frac{V_{ph}}{X_c} = 2\pi f C_{ph} V_{ph}$

$$Q_{cph} = V_{ph} (2\pi f C_{ph} V_{ph}) \sin 90^\circ$$

$$Q_{cph} = 2\pi f C_{ph} V_{ph}^2$$

$$C_{ph} = \frac{Q_{cph}}{2\pi f V_{ph}^2} = \frac{Q_c}{3(2\pi f V_{ph}^2)}$$

$$C_{ph} = \frac{P_1 (\tan \phi_1 - \tan \phi_2)}{3(2\pi f V_{ph}^2)}$$

load power

(1) Star Cap. Bank $= V_{ph} = \frac{V_L}{\sqrt{3}}$

(2) Delta Cap. Bank $= V_{ph} = V_L$

• Capacitance of Each Cell:- $[C_s]$:-

$$C_s = n C_{ph}$$

$n = \text{No. of cells/phase}$

• In cap. Bank, multiple capacitor are used. But if we use single capacitor insulation $\uparrow$, cost $\uparrow$.

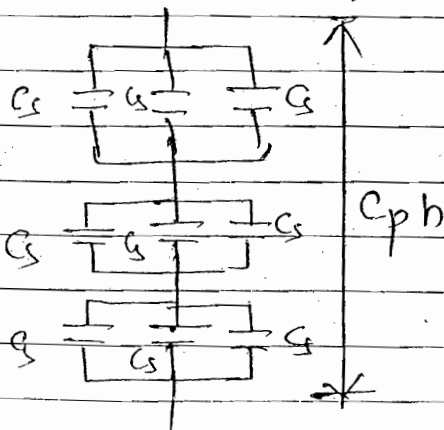


fig ① can also show us.

Q A 3 ϕ IM Drawing p.f = 0.6 lag is connected to a O/p load of 9 MW and has η of 90%. Find the rating of shunt capacitor required for Improving the power factor to 0.8 lagging.

Solution $\eta = \frac{O/p}{S/p}$ $S/p = \frac{O/p}{\eta} = \frac{9}{0.90} = 10 \text{ MW}$

$$\begin{aligned} Q_c &= 10 [\tan \phi_1 - \tan \phi_2] \\ &= 10 [\tan \cos^{-1} 0.6 - \tan \cos^{-1} 0.8] \\ &= 5.8 \text{ MVAR.} \end{aligned}$$

Q A 3 ϕ IM connected in Δ across 11 KV and the Motor has impedance of $3 + j4 \Omega$ /phase a Star connected cap. Bank is used for improving p.f to 0.9 lag. If the capacitor Bank has 5 cells per phase. Calculate capacitance of each cell.

Solution $C_s = 5 C_{ph}$ $Q = 2\pi f C_{ph} V_{ph}^2$

$$\Delta \text{ load:- } P_1 = \frac{3V_L^2 \cos \phi}{Z} = \frac{3 \cdot 11^2 \cos [\tan^{-1} 4/3]}{\sqrt{3^2 + 4^2}}$$

$$P_1 = 43.56 \text{ MW}$$

$$C_s = n C_{ph} = \frac{n \cdot P_1 (\tan \phi_1 - \tan \phi_2)}{3(2\pi f V_{ph}^2)}$$

$$= \frac{5 \times 43.56 (\tan \cos^{-1} 0.6 - \tan \cos^{-1} 0.9)}{3(2\pi \times 50 \times (11/\sqrt{3})^2)}$$

$$C_s = \frac{217.8 (0.8490)}{38013.27} = 4.86 \times 10^{-3}$$

- Capacitor Banks are used in the 33 and 132 KV substation.

(2) Shunt Reactor [L_{sh}]:-

Shunt Reactor is used:-

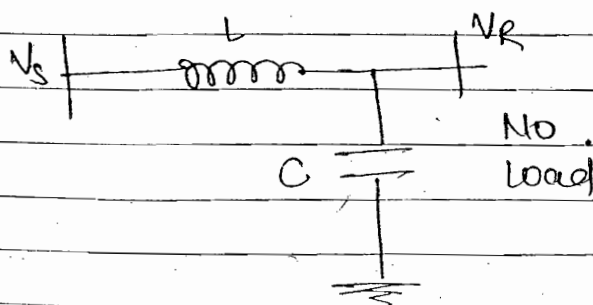
- (1) For compensation of Ferranti Effect.
- (2) Changes the factor from leading to lagging. That is $\cos \phi$ is reduce.
- (3) System stability is reduce by increasing δ .

Ferranti Effect: - Neglecting R , & G parameters.

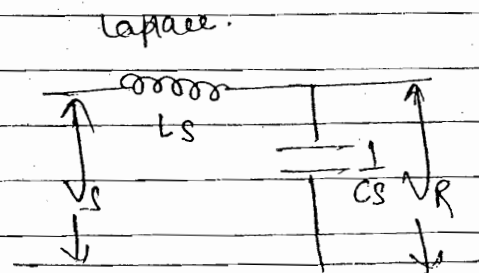
In case of NO LOAD or LIGHT LOAD due to RC component of the Tr-line, VAR $V_R > V_S$ occurs and this is dominant in medium and long Tr-line. For compensating this ferranti effect shunt reactor is used.

- Voltage is more dangerous than current.
 voltage $\uparrow \rightarrow$ insulation breakdown
 Current $\uparrow \rightarrow I^2 R$ losses $\rightarrow$ insulat failure delay.

- Shunt Reactor are used in 400 KV and 765 KV substation.



L, C = Tr-line parameters



$$V_R = \frac{V_s / s}{s + V_s} = \frac{V_s}{Ls^2 + 1}$$

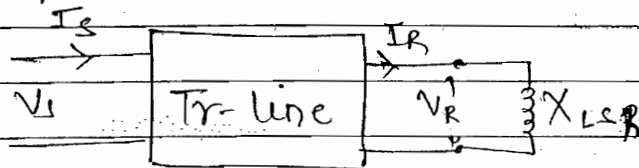
$$V_R = V_s + V_s \cdot \omega^2 LC$$

$$V_R = V_s + \Delta V_R$$

$$\Delta V_R = V_s \omega^2 LC$$

$$V_R > V_s$$

Compensation of Ferranti effect:-



$$X_{Lsh} = \text{Reactance of } L_{sh} = \frac{V_R}{I_R}$$

At No load $V_R > V_s$

with L_{sh} :-

$$V_R = V_s$$

$$V_R = AV_R + BI_R$$

$$V_s = AV_R + BI_R$$

$$V_R(1-A) = B \cdot I_R$$

$$X_{Lsh} = \frac{V_R}{I_R} = \frac{B}{(1-A)}$$

$$V_s = AV_R + BI_R$$

At No load :- $I_R = 0 \Rightarrow V_s = AV_R$

$$V_R = V_s / A$$

$V_R \rightarrow$ Receiving end voltage

$$I_s = CV_R + DI_R$$

At No load $I_R = 0 \Rightarrow I_s = CV_R$

$I_s =$ charging current of line $= I_c$

$$V_{Rph} = \frac{V_{sph}}{A_{ph}} \Rightarrow \frac{V_{RL}}{\sqrt{3}} = \frac{V_{SL}}{\sqrt{3} A_{ph}}$$

$$V_{RL} = \frac{V_{SL}}{A}$$

A → phase value.

$$I_s = I_c = \frac{C \cdot V_R}{\sqrt{3}}$$

$$I_c = \frac{C \cdot V_{RL}}{\sqrt{3}}$$

Q A 3φ Tr-line has $V_s = 400 \text{ kV}$ $A = 0.8 \angle 0^\circ$
 $B = 100 \angle 90^\circ \Omega$, $C = 0.5 \times 10^{-6} \text{ F/m}$ Calculate V_R and
 I_c on no load (2) Shunt Reactor required
 for compensating ferranti effect.

Solution $V_R = \frac{V_s}{A} = \frac{400}{0.8 \angle 0^\circ} = 500 \text{ kV}$

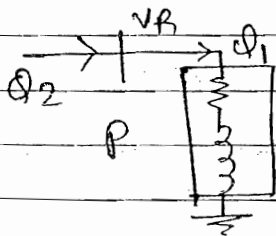
$$X_{Lsh} = \frac{B}{(1-A)} = \frac{100 \angle 90^\circ}{(1 - 0.8 \angle 0^\circ)} = \frac{100 \angle 90^\circ}{0.2}$$

$$= 500 \angle 90^\circ$$

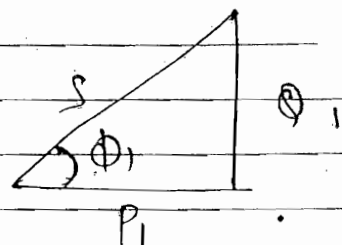
$$I_c = \frac{C \cdot V_{RL}}{\sqrt{3}} = \frac{0.5 \times 10^{-6} \times 500 \times 10^3}{\sqrt{3}}$$

$$= 0.14 \text{ A/phase}$$

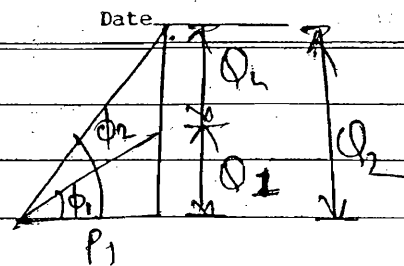
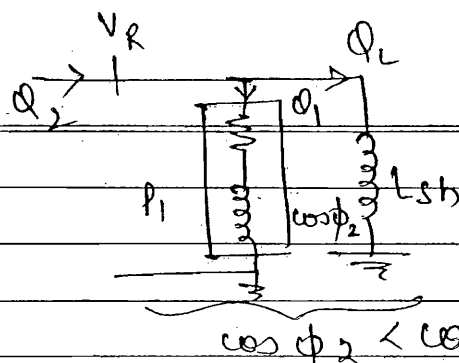
(Q) Without L_{sh} : Assume $\phi_1 < \phi_2$
 $V_R > V_s$



lag $\cos \phi$



(b) Wien Lsh :-



$Q_L = 3\phi$ VAR Rating of L_{sh} :-

$$Q_2 = Q_1 + Q_L$$

$$Q_L = Q_2 - Q_1$$

$$Q_L = P_1 (\tan \phi_2 - \tan \phi_1)$$

Inductance per phase $[L_{ph}]$:-

$$Q_{Lph} = V_{ph} \cdot I_{ph} \sin \phi$$

For pure L_{sh} , $\phi = 90^\circ$, $I_{ph} = \frac{V_{ph}}{2\pi f L_{ph}}$

$$Q_{Lph} = \frac{V_{ph}^2}{2\pi f L_{ph}}$$

$$L_{ph} = \frac{V_{ph}^2}{2\pi f Q_{Lph}}$$

From previous $Q_{Lph} = Q_L / 3$

• Relation Between Q , f , V :-

(1) Shunt Capacitor :-

$$Q_{Cph} = 2\pi f V_{ph}^2 C_{ph}$$

$$Q \propto f V^2$$

$$\frac{Q_2}{Q_1} = \left(\frac{V_2}{V_1} \right)^2 \left(\frac{f_2}{f_1} \right)$$

(2) Shunt Reactor :-

$$Q_{Lph} = \frac{V_{ph}^2}{2\pi f L_{ph}}$$

$$\left[\Phi \propto \frac{V^2}{f} \right]$$

$$\left[\frac{\Phi_2}{\Phi_1} = \left(\frac{V_2}{V_1} \right)^2 \left(\frac{f_1}{f_2} \right) \right]$$

Q If the voltage $\uparrow$ by 10%, $f \downarrow$ by 5%. How much of Reactive power has to be compensated using

(i) Shunt Capacitor.

(ii) Shunt Reactor

Solub (i) Shunt Capacitor (ii) Shunt Reactor.

$$\frac{\Phi_2}{\Phi_1} = \left(\frac{1.1 V_1}{V_1} \right)^2 \times \left(\frac{0.95 f_1}{f_1} \right)$$

$$\frac{\Phi_2}{\Phi_1} = \left(\frac{1.1 V_1}{V_1} \right)^2 \times \frac{f_1}{0.95 f_1}$$

$$\Phi_2 = 1.15 \Phi_1, 15\% \text{ Excess.}$$

$$\Phi_2 = 1.27 \Phi_1 = 27\% \text{ Excess}$$

(3) Series Capacitor Compensation

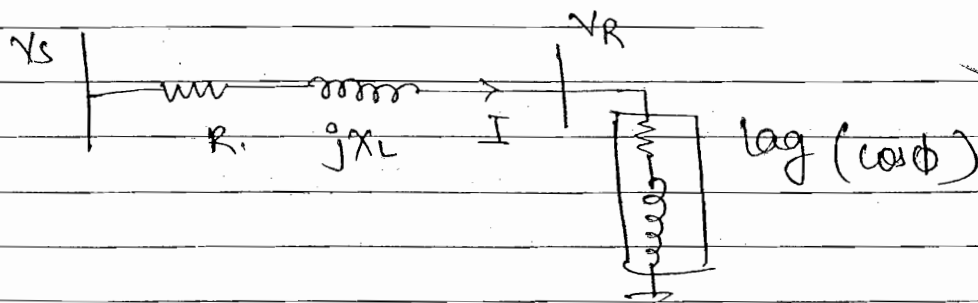
By using series capacitor :- system. also

(1) System stability $\uparrow$

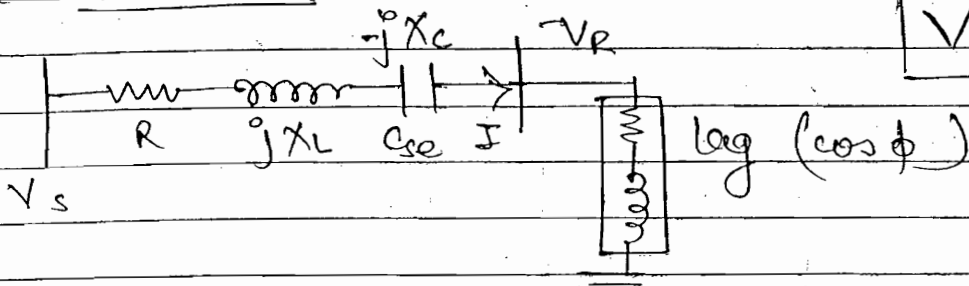
(2) power transferred to the Tr. line is $\uparrow$.

(3) Voltage Regulation is reduce.

(a) Without Csc :-



$$\% \text{ VREG} = \frac{V_s - V_R}{V_R} \times 100 = \frac{I(R \cos \phi + X_L \sin \phi)}{V_R} \times 100$$

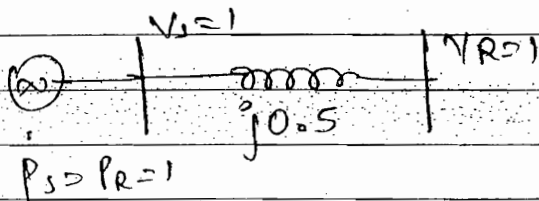
(b) with Cse :-

$$V_{REG2} < V_{REG1}$$

$$\% V_{REG} = \frac{I(R \cos \phi + (X_L - X_C) \sin \phi)}{V_R} \times 100$$

- Q A Tr-line a reactance $X = 0.5 \text{ pu}$ is connected b/w generator and load center operating $V_s = V_R = 1 \text{ pu}$. If the load 1 pu is delivered by the line. Find the load angle of the generator.
- ① Without compensator ② With ^{series cap.} compensator of 0.25 pu .

Solution ① Without Cse :-

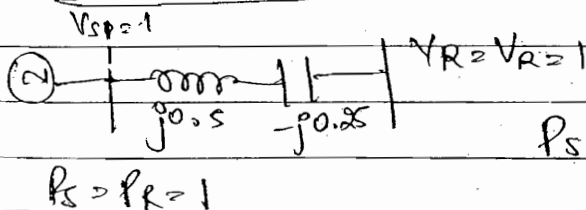


$$P_s = P_R = \frac{V_s V_R}{X} \sin \delta_1$$

$$1 = \frac{1 \times 1}{0.5} \times \sin \delta_1 = 2 \sin \delta_1$$

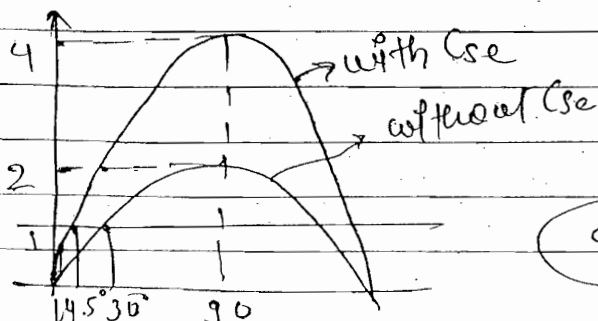
② With Cse :-

$$\delta_1 = 30^\circ$$



$$P_s = P_R = \frac{V_s V_R}{(X_L - X_C)} \sin \delta_2$$

$$1 = \frac{1 \times 1}{(0.5 - 0.25)} \sin \delta_2 = 4 \sin \delta_2$$



$$\delta_2 = 14.5^\circ$$

$$\delta_2 < \delta_1 \quad \delta_2 \rightarrow \text{More Stable}$$

(4) Synchronous Phase Modifier :- (SPM)

SPM is basically a syn Motor. It is used for

(1) Driving Mechanical load

(2) Controlling the reactive power voltage and p.f.

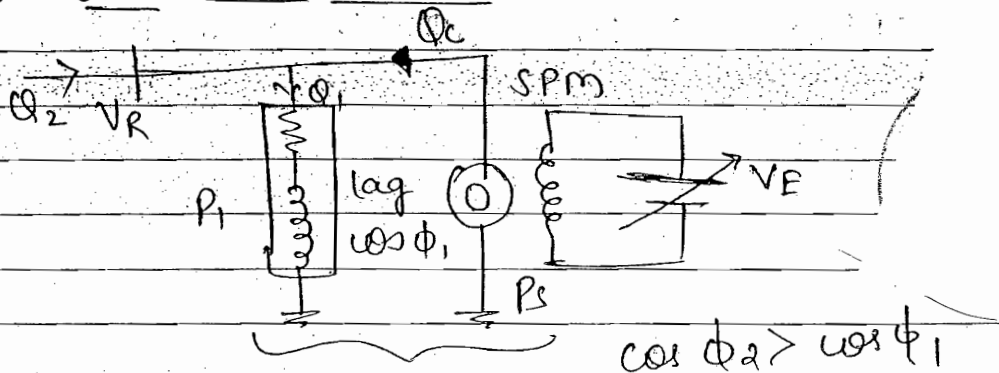
(3) If it is used for driving any mechanical load with then the load angle $\neq 0$ and maintaining b/w 30° to 45° due to stability limit.

(4) If it is used for p.f or voltage control it is normally normally maintaining at No load so that $\delta = 0$.

(5) The over excited SPM is used for supply lagging VAR's and working similar to the shunt capacitor.

(6) Under excited SPM is used for absorbing lagging VAR's or delivering leading VAR's. It is working similar to the shunt reactor.

(a) Over Excited SPM: Assume $V_R < V_s$



• Rating of SPM:-

(1) If $P_s \neq 0$

$$Q_c = P_1 \tan \phi_1 - (P_1 + P_s) \tan \phi_2$$

$$\text{Rating of SPM} = (P_s + jQ_c) \dots VA \quad V_A = V_R$$

(2) If $P_s = 0$

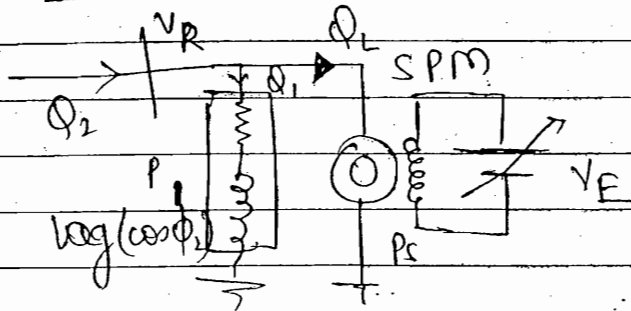
$$V_A > V_R$$

Date _____

$$\Phi_c = P_1 (\tan \phi_1 - \tan \phi_2)$$

$$\text{Rating of SPM} = \Phi_c \times V_A$$

⑥ Under Excited SPM: - Assume $V_B < V_R$



$$\cos \phi_2 < \cos \phi_1$$

• Rating of SPM:-

① If $P_s \neq 0$

② If $P_s = 0$

$$\Phi_c = (P_1 + P_s) \tan \phi_2 - \tan \phi_1 P_1$$

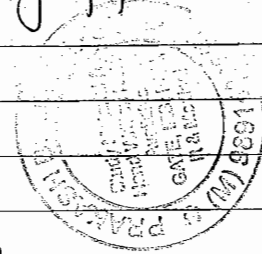
$$\Phi_c = P_1 (\tan \phi_2 - \tan \phi_1)$$

$$\text{Rating of SPM} = P_s + j\Phi_c \times V_A \quad \text{Rating of SPM} = \Phi_c \times V_A$$

Q A 3 ϕ IM as a rating of 10 MW 0.6 lagging is connected with SPM for improving pf to 0.8 lag. Find the rating of SPM if SPM

① consumes 1 MW of active power

② Running under No-load.



$$\text{Soln} \quad ① \Phi_c = P_1 \tan \phi_1 - (P_1 + P_s) \tan \phi_2$$

$$= 10 \tan \cos^{-1} 0.6 - (10 + 1) \tan \cos^{-1} 0.8$$

$$= 5.083$$

$$\text{Rating of SPM} = (P_s + j\Phi_c) \text{ MVAR}$$

$$= (1 + j 5.083) \text{ MVA}$$

② no load. $Q_c = P_1 (\tan \phi_1 - \tan \phi_2)$
 $= 10 [\tan \cos^{-1} 0.6 - \tan \cos^{-1} 0.8]$
 $= 5.833 \text{ MVA.}$

Rating of SPM = $Q_c = 5.833 \text{ MVA}$

• Comparison Between SPM and Shunt Compensation:

SPM

Shunt Compensation

(1) A single unit of SPM can be used both inductor & capacitor by adjusting excitation.

(1) Two separate units are required that is inductor & capacitor for adjustment of voltage.

(2) Smooth voltage regulation is possible.

(2) Step by step voltage regulation is possible.

(3) Initial cost of SPM is higher.

(3) Initial cost is less.

(4) SPM required more maintenance.

(4) It required less maintenance.

(5) Initial starting methods are required for bringing the syn. motor upto synchronous speed.

(5) There is no starting mechanism required.

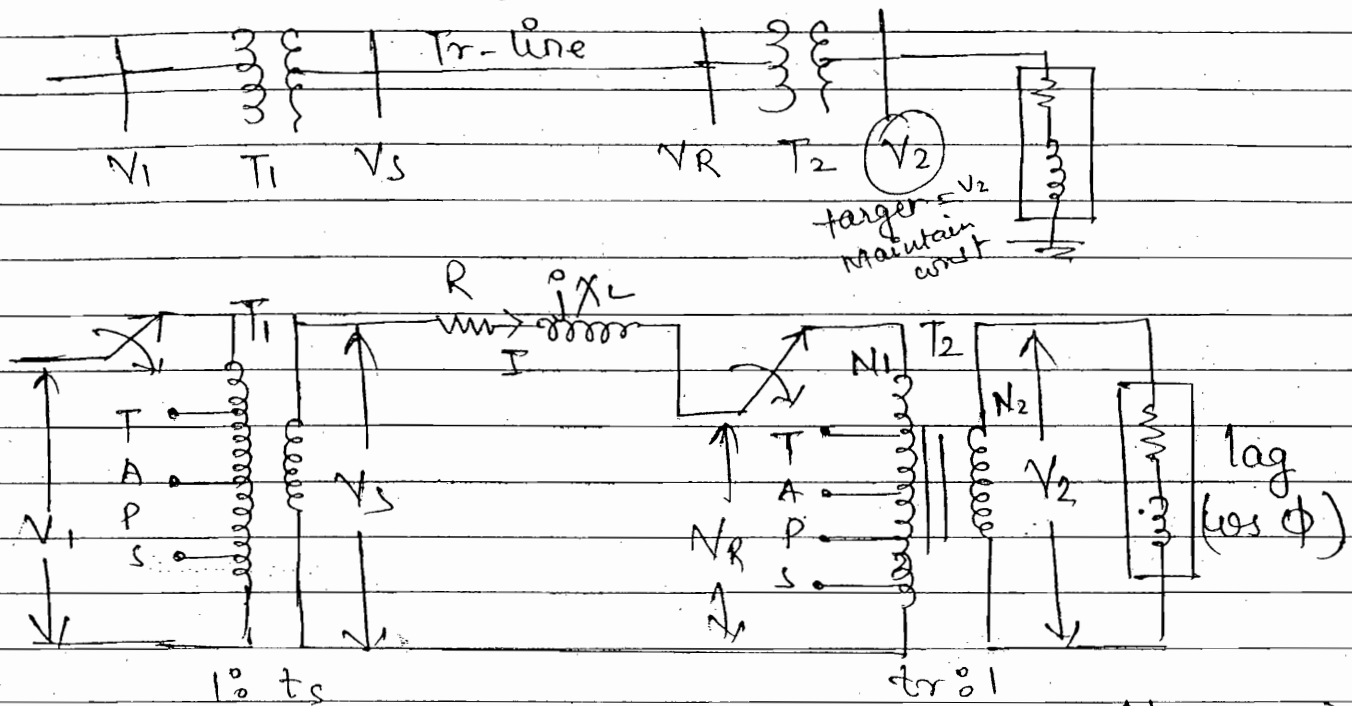
(6) It consume both active & Reactive power.

(6) consume only Reactive power.

(7) Due to above discuss, SPM is practically NOT preferred in the substations.

(7) It is most practically used in substations for the voltage control.

(5) OLTC Transformer:-



$$\frac{V_1}{V_s} = \frac{1}{t_s} \Rightarrow V_s = V_1 t_s$$

$$\frac{V_2}{V_R} = \frac{1}{t_r} \Rightarrow V_R = V_2 t_r$$

$$\frac{\text{const } N_1}{N_2} = \frac{V_2}{V_R \text{ const}}$$

$$V_s - V_R = R I \cos \phi + X_L I \sin \phi$$

$$I \cos \phi = \frac{P_R}{V_R}$$

$$I \sin \phi = \frac{Q_R}{V_R}$$

$$V_s - V_R = \frac{P_R}{V_R} + \frac{X_L Q_R}{V_R}$$

$$V_R V_s - V_R^2 = R P_R + X_L Q_R$$

$$\Rightarrow V_R^2 - V_s V_R + R P_R + X_L Q_R = 0 \quad \text{--- (2)}$$

Substitute (1) in (2)

$$V_2^2 t_r^2 - V_1 V_2 t_r t_s + R P_R + X_L \Delta R = 0$$

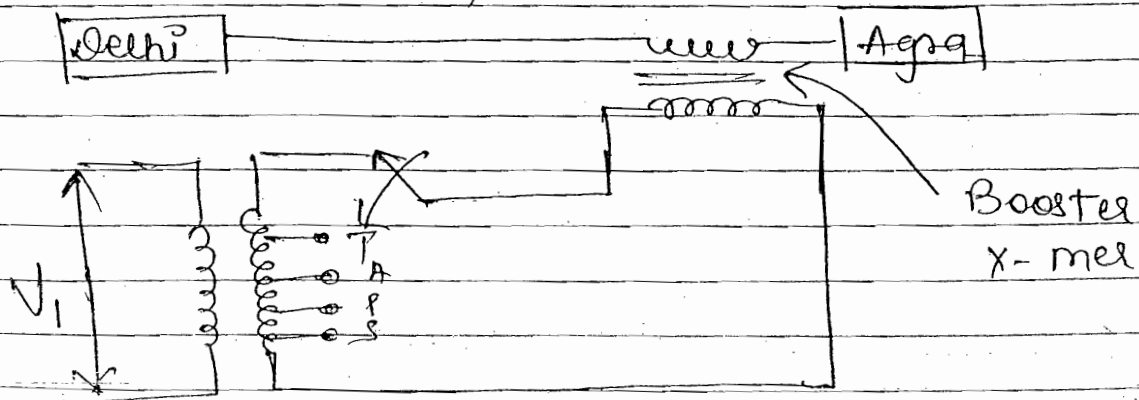
$V_2 = f [t_r, t_s]$; V_2 is controlled by controlling transformer taps t_r & t_s .

Off Normal Setting = $t_r t_s = 1$

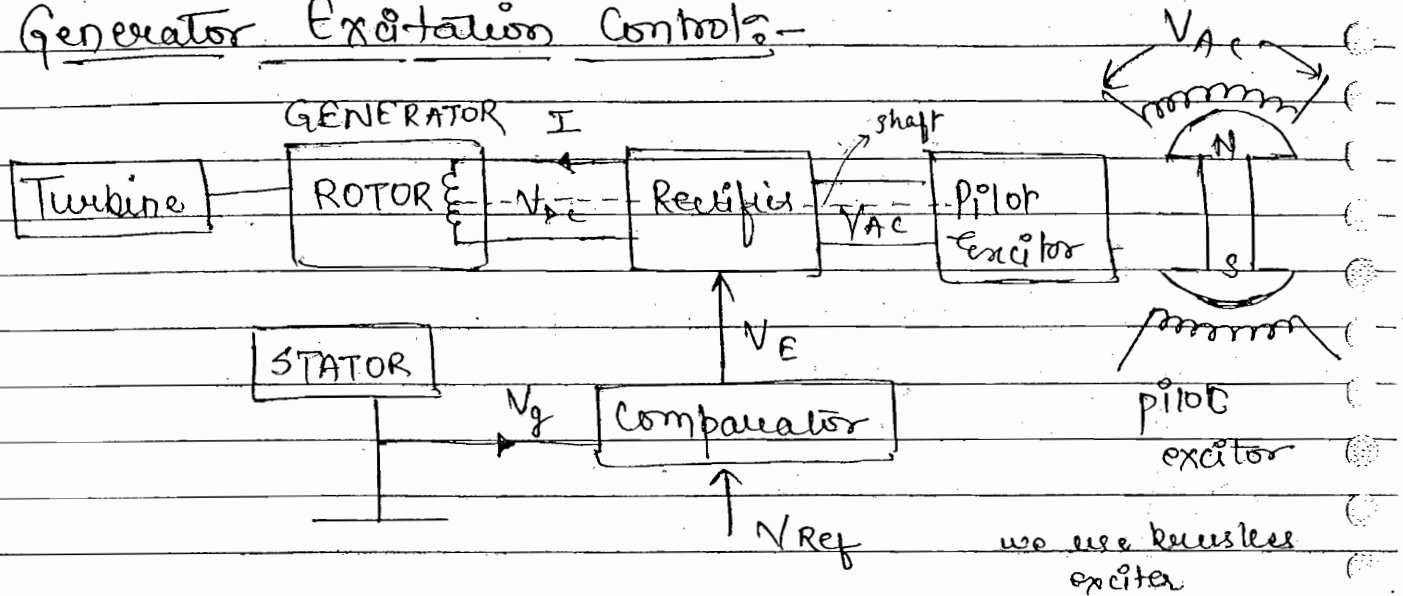
- tap changing at H.V. bus current value is small, small arcing, less heat produce.
- OLTC is most practically used for the voltage control in the substation.
- It is used in all voltage levels like 400/220, 220/132, 132/33 and 33/11 KV
- X-mers normally provided on the H.V. side where current is small so that the intensity of arcing is minimized which enhances the life of the X-mer.

• BOOSTER TRANSFORMER : - (for line side) previous decided are for load side

- (1) It is used to maintain uniform voltage throughout the Tr-line
- (2) It is practically used in remote substation and in traction applicatⁿ. for maintaining uniform voltage



Generator Excitation Control:-



$$V_E = V_g - V_{ref}$$

- ① If $V_g = V_{ref} \Rightarrow V_E = 0 \Rightarrow$ Constant excitation.
- ② If $V_g > V_{ref} \Rightarrow V_E > 0 \Rightarrow$ Reduce excitation until $V_E = 0$.
- ③ If $V_g < V_{ref} \Rightarrow V_E < 0 \Rightarrow$ Increase excitation until $V_E = 0$.

- Generator excitation control is most practically used for maintaining constant voltage at the terminals of the generator. This method is adopted after applying shunt capacitor and OLTC operation of the x-mtr. Because the consumer needs to be do not experience over voltage. The type of voltage control is called automatic voltage regulation.

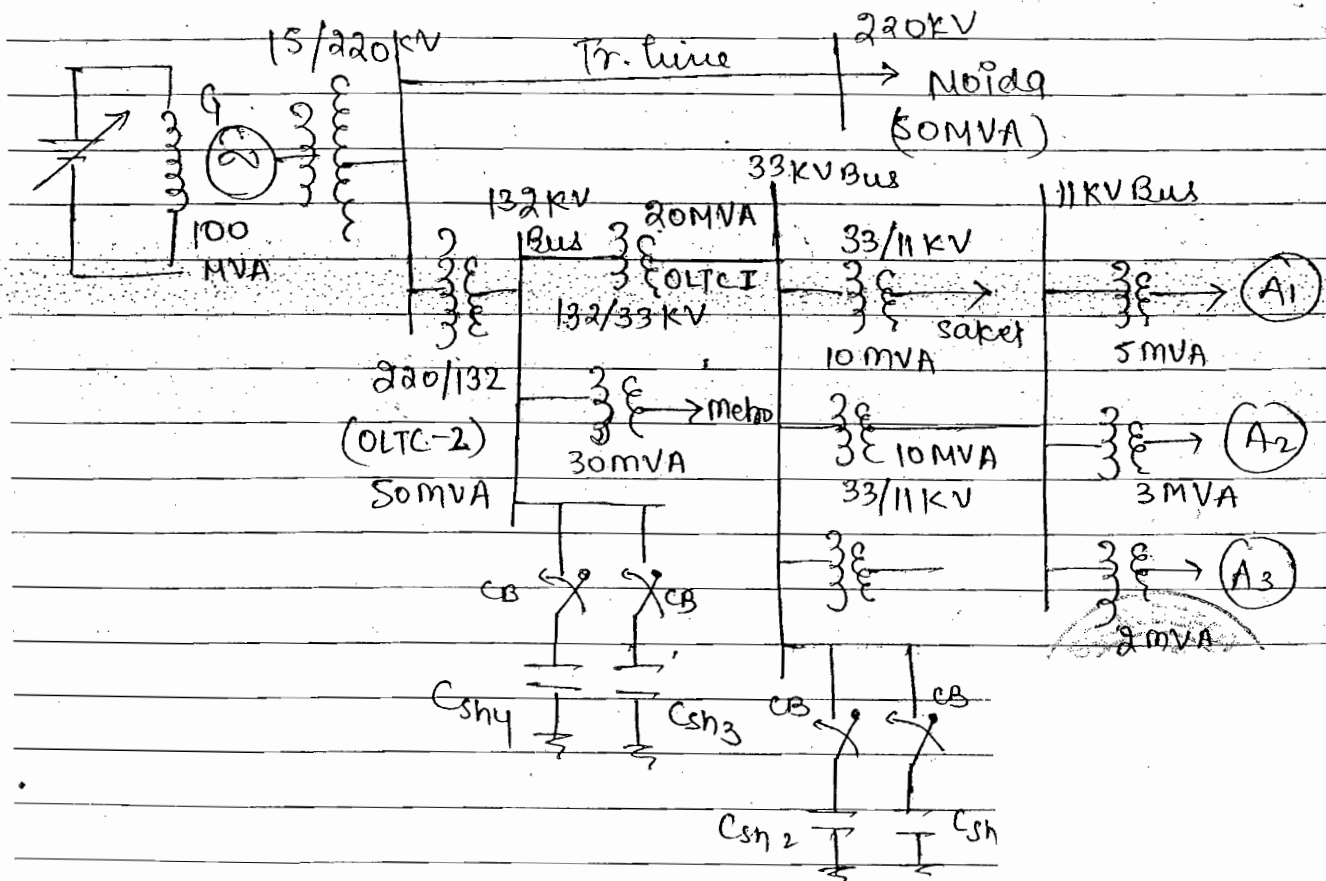
- C_{sh1} to C_{sh4} are capacitor Bank used to maintain the voltage.

- when there is a voltage drop in 33kV Bus, C_{sh2} or C_{sh1} or both are switch ON, when still there is not maintaining 33kV (ex:- 30kV) go for OLTC-1, when still OLTC-1 get fail to maintain voltage constant, C_{sh1} or C_{sh3} or both

are switch ON. Before switch ON these two capac. bank, first they check, wheather incoming voltage is 132 kV or not. Then they switch ON the the cap. Bank when not maintaining 132 kV, go for OLTC-2. When is it not also fail to maintain 220, check the incoming voltage is 220 kV or not, then finally go for generator exciter case.

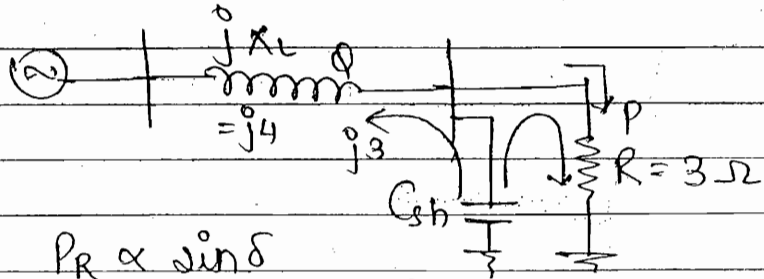
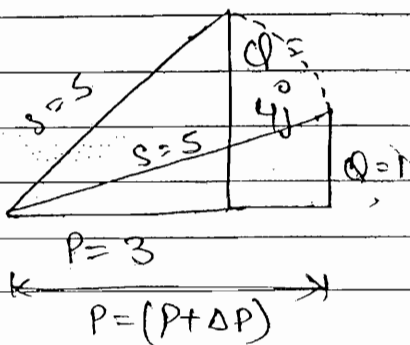
- When there is over voltage same sequence will follow, in this case cap. Banks are removed.

Sequence:-
 1> Cap. Bank
 2> OLTC
 3> Gen. Excitator.



• Power Flow through Tr-line:-

- When install C_{sh} , burden of reactive power on generator will reduce and convert into active power.
- Gen $\rightarrow$ only active power, reactive power by other means.
- Aim $\rightarrow$ transfer maximum active power through X-line.
- Compensator deliver reactive power to X-line as well as load.



$$P_R \propto \sin \delta$$

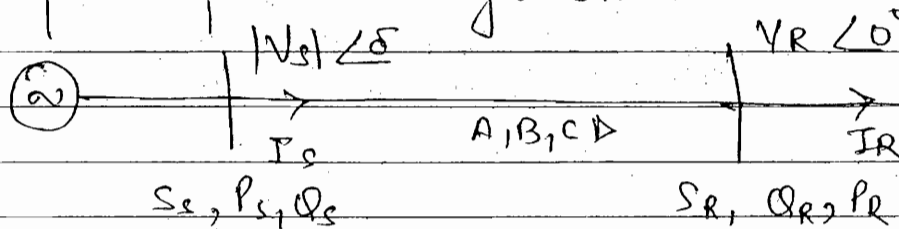
$$Q_R = \frac{V_s V_R \cos \delta - V_R^2}{X_L}$$

$$V_R \& X_L = \text{constant}$$

$$\cos \delta \approx 1$$

$$Q_R \propto (V_s - V_R)$$

- Relation between ABCD parameters, voltage and power flow through the X-line.



Let $A = |A| \angle \alpha$ $B = |B| \angle \beta$ $C = |C| \angle \gamma$ $D = |D| \angle \delta$
 $V_s = |V_s| \angle \delta$ $V_R = |V_R| \angle 0$

$$AD - BC = 1$$

Receiving End power :-

$$V_s = AV_R + BI_R$$

$$I_R = \frac{V_s}{B} - \frac{AV_R}{B} \quad \text{--- (1)}$$

$$= \frac{|V_s| \angle \delta}{|B| \angle \beta} - \frac{|A| \angle \alpha \cdot |V_R| \angle 0^\circ}{|B| \angle \beta}$$

$$I_R = \frac{|V_s|}{|B|} \angle \delta - \beta - \frac{|A| |V_R|}{|B|} \angle \alpha - \beta$$

$$I_R^* = \frac{|V_s|}{|B|} \angle \beta - \delta - \frac{|A| |V_R|}{|B|} \angle \beta - \alpha \quad \text{--- (2)}$$

$$S_R = P_R + j Q_R = V_R \cdot I_R^* \quad \text{--- (3)}$$

Substitute (2) in (3).

$$P_R + j Q_R = \frac{|V_s| |V_R|}{|B|} \angle \beta - \delta - \frac{|A| |V_R|^2}{|B|} \angle \beta - \alpha$$

Separate Real and Imaginary terms.

$$\left[\begin{array}{l} P_R = \frac{|V_s| |V_R|}{|B|} \cos(\beta - \delta) - \frac{|A| |V_R|^2}{|B|} \cos(\beta - \alpha) \\ Q_R = \frac{|V_s| |V_R|}{|B|} \sin(\beta - \delta) - \frac{|A| |V_R|^2}{|B|} \sin(\beta - \alpha) \end{array} \right]$$

Sending End powers:-

$$I_s = C V_R + D I_R \quad \text{--- (4)}$$

Substitute (1) in (4)

$$I_s = C V_R + D \left(\frac{|V_s|}{|B|} - \frac{|A| |V_R|}{|B|} \right)$$

$$= \frac{D V_s}{|B|} + \frac{(BC - AD)}{|B|} V_R$$

$$= \frac{D V_s}{|B|} - \frac{V_R}{|B|} = \frac{|D| \angle \alpha |V_s| \angle \delta}{|B| \angle \beta} - \frac{|V_R| \angle 0^\circ}{|B| \angle \beta}$$

$$I_s = \frac{|D V_s|}{|B|} \angle \alpha + \delta - \beta - \frac{|V_R|}{|B|} \angle -\beta$$

$$I_s^* = \frac{|D V_s|}{|B|} \angle \beta - \alpha - \delta - \frac{|V_R|}{|B|} \angle \beta \quad \text{--- (5)}$$

$$S_s = P_s + jQ_s = V_s I_s^*$$

$$= V_s \angle \delta \cdot I_s^* \quad \text{--- (5)}$$

Substitute (5) in (6)

$$S_s = P_s + jQ_s = \left| \frac{DV_s^2}{B} \right| \angle (\beta - \alpha) - \left| \frac{V_s V_R}{B} \right| \angle (\beta + \delta)$$

Separate Real and Imaginary terms.

$$P_s = \left| \frac{DV_s^2}{B} \right| \cos(\beta - \alpha) - \left| \frac{V_s V_R}{B} \right| \cos(\beta + \delta)$$

$$Q_s = \left| \frac{DV_s^2}{B} \right| \sin(\beta - \alpha) - \left| \frac{V_s V_R}{B} \right| \sin(\beta + \delta)$$

• Condition for Receiving Maximum Active Power :-

$$P_R = \left| \frac{V_s V_R}{B} \right| \cos(\beta - \delta) - \left| \frac{AV_R^2}{B} \right| \cos(\beta - \alpha)$$

δ is variable.

For Receiving end Maximum P_R .

$$\frac{dP_R}{d\delta} = 0$$

$$d\delta$$

$$\Rightarrow - \left| \frac{V_s V_R}{B} \right| \sin(\beta - \delta) = 0 \quad \left| \frac{V_s V_R}{B} \right| \neq 0$$

$$\text{At } \beta = \delta$$

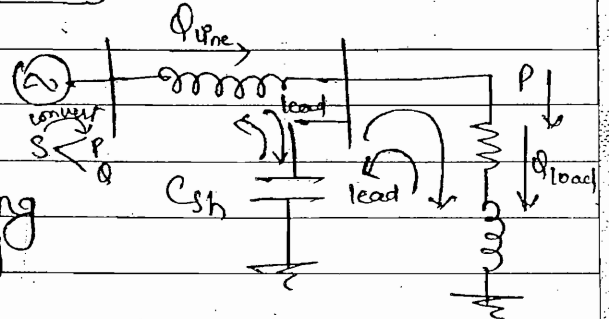
$$P_{R\max} = \left| \frac{V_s V_R}{B} \right| - \left| \frac{AV_R^2}{B} \right| \cos(\beta - \alpha)$$

$$\text{At } \delta = \beta$$

$$Q_R = \left| \frac{V_s V_R}{B} \right| \sin(\beta - \beta) - \left| \frac{AV_R^2}{B} \right| \sin(\beta - \alpha)$$

$$Q_R = - \left| \frac{V_R^2 A}{B} \right| \sin(\beta - \alpha)$$

NOTE: - $Q_R = -ve$ indicates leading nature of load and for this leading load leading VARs have to be supplied for receiving P_{max} .



• LOCUS OF POWER:-

$$P_R + \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha) = \left| \frac{V_s V_R}{B} \right| \cos(\beta - \delta) \quad \text{--- (1)}$$

$$Q_R + \left| \frac{A V_R^2}{B} \right| \sin(\beta - \alpha) = \left| \frac{V_s V_R}{B} \right| \sin(\beta - \delta) \quad \text{--- (2)}$$

Squaring and adding eqⁿ (1) & (2)

$$\left[P_R + \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha) \right]^2 + \left[Q_R + \left| \frac{A V_R^2}{B} \right| \sin(\beta - \alpha) \right]^2 = \left(\frac{V_s V_R}{B} \right)^2$$

eqⁿ (3) represents circle equatⁿ.

$$(x-a)^2 + (y-b)^2 = r^2$$

r = Radius of circle $\left| \frac{V_s V_R}{B} \right|$

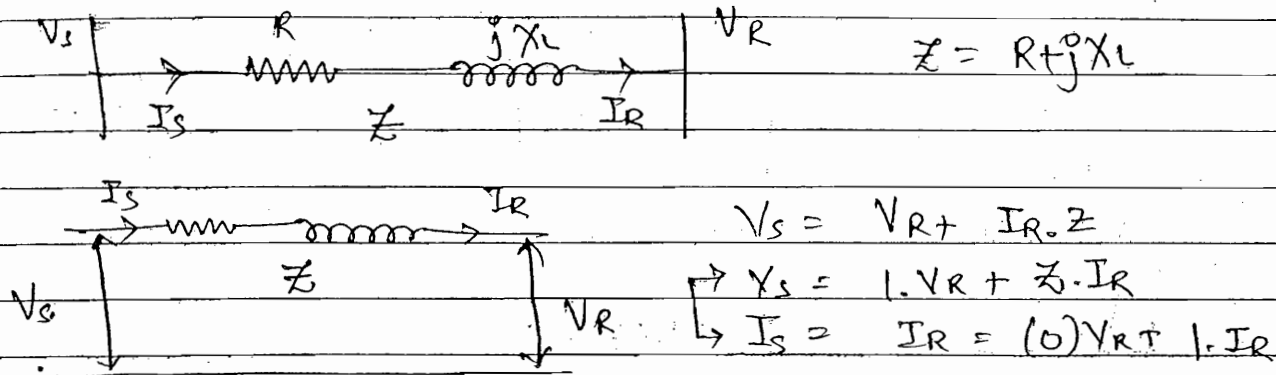
Center of circle

$$(a, b) = \left[- \left| \frac{V_R^2 A}{B} \right| \cos(\beta - \alpha), - \left| \frac{A V_R^2}{B} \right| \sin(\beta - \alpha) \right]$$

NOTE: - locus of P_R, Q_R is a circle at constant $|V_s|, |V_R|$. Similarly locus of P_s, Q_s is a circle at constant $|V_s|, |V_R|$.

Generalised Equation of Power :-

Assume short Tr- line : (C, G are neglected)



$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

Assume $R \ll X_L$

$$Z = jX_L = X_L \angle 90^\circ = \beta \angle \beta \quad A \angle \alpha = 1 \angle 0^\circ = \gamma, \quad c = 0$$

— eqn (1)

Receiving End power :-

Use when
A, B, C, D parameters
are given

$$P_R = \left| \frac{V_s V_R}{B} \right| \cos(\beta - \delta) - \left| \frac{V_R^2 A}{B} \right| \cos(\beta - \alpha) \quad (2)$$

Substitute (1) in (2)

$$P_R = \left| \frac{V_s V_R}{X_L} \right| \cos(90^\circ - \delta) - \left| \frac{1 \times V_R^2}{X_L} \right| \cos(90^\circ - 0)$$

Use when
only X_L
are given

$$P_R = \left| \frac{V_s V_R}{X_L} \right| \sin \delta \quad P_R \propto \sin \delta$$

Use when
parameters are
given

$$Q_R = \left| \frac{V_s V_R}{B} \right| \sin(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \sin(\beta - \alpha) \quad (3)$$

Substitute (1) in (3)

when only
XL is given

$$P_R = \frac{V_S V_R}{X_L} \cos \delta = \frac{V_R^2}{X_L}$$

If δ is small, $\cos \delta \approx 1$

$$P_R = \frac{V_R (V_S - V_R)}{X_L}$$

$$P_R \propto (V_S - V_R)$$

• Sending End power: -

Substitute (1) in P_S, Q_S

Average Real Power: -

$$P_S = \frac{V_S V_R}{X_L} \sin \delta = P_R$$

$$P_{avg} = \frac{P_R + Q_S}{2}$$

$$Q_S = \frac{V_S^2}{X_L} - \frac{V_S V_R}{X_L} \cos \delta$$

$$P_{avg} = \frac{V_S^2 - V_R^2}{2X_L}$$

Q From the following N/W calculate the active power and reactive power flow through the x-line.



Solution $V_S = 10 \angle 30^\circ$ $V_R = 10 \angle 0^\circ$

$$P_R = \frac{V_S V_R}{X_L} \sin \delta$$

$$= \frac{10 \times 10}{2} \sin(30-0) = 25 \text{ W}$$

$$Q_R = \frac{V_S V_R}{X_L} \cos \delta - \frac{V_R^2}{X_L} = \frac{10 \times 10 \cos(30-0)}{2} - \frac{10^2}{2}$$

$$= 6.07 \text{ VAR}$$

$$Q_S = \frac{V_S^2}{X_L} - \frac{V_S V_R}{X_L} \cos \delta = 6.07 \text{ VAR}$$

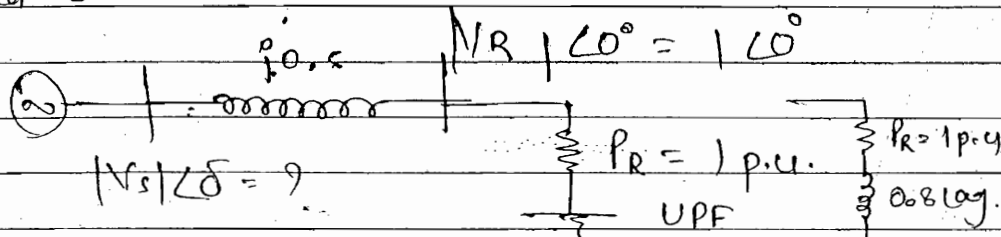
- the sequence of Impedance of equipment is equal to the equipment original equipments impedance.

$$Z_{p.u} = \frac{Z_{\Omega} (MVA)_b}{(KV_b)^2}$$

$$X_{p.u.}, R_{p.u}$$

Q A Tr-line impedance of $j0.5$ p.u is connected to a load of 1 p.u UPF. If $V_R = 1 \angle 0^\circ$. Calculate V_s and δ .

Solution



$$P_R = \frac{V_s V_R}{X_L} \sin \delta$$

$$P_{load} = P \tan \phi = 1 \times \tan \cos^{-1} 0.8 = 0.75 \text{ p.u.}$$

$$1 = \frac{V_s \times 1}{0.5} \sin \delta$$

$$V_s \sin \delta = 0.5 \quad \text{--- (1)}$$

$$Q_R = \left| \frac{V_s V_R}{X_L} \right| \cos \delta - \left| \frac{V_R^2}{X_L} \right|$$

load is resistive UPF $Q_R = 0$

$$Q_R = 0.75 \text{ p.u.}$$

$$0 = \left| \frac{V_s \times 1}{0.5} \right| \cos \delta - \frac{1^2}{0.5}$$

$$V_s \cos \delta = 1 \quad \text{--- (2)}$$

Solving (1) & (2)

$$\frac{V_s \sin \delta}{V_s \cos \delta} = \frac{0.5}{1}$$

$$\tan \delta = 0.5$$

$$\delta = 26.56^\circ$$

$$V_s \sin 26.56^\circ = 0.5$$

$$V_s = 1.011823 = 1.012 \text{ p.u.}$$

- $V_s = 1.012$ $V_R = 1$ Maintain the voltage for inductive.

when shunt capacitor is connected to the system, the power factor will be improved, which is diff.

Date: _____

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Q In the previous problem if $V_s = V_R = 1 \text{ pu}$ is maintain by using compensator, Find the rating of compensator required for

- 1 pu of UPF load
- 1 pu 0.8 lag load.
- 1 pu 0.6 leading load.
- 1 p.u. 0.995 leading load.

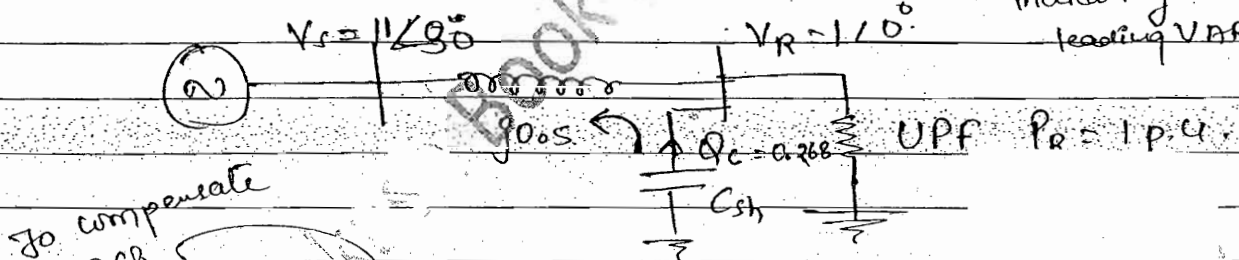
Solution:- (i) $P_R = 1 \text{ p.u.}$ UPF: , $|V_s| = |V_R| = 1$
 $P_R = \frac{|V_s - V_R|}{X_L} \sin \delta$

$$1 = \frac{|X_L|}{0.5} \sin \delta \quad \sin \delta = 0.5 \quad \delta = 30^\circ$$

$$Q_R = \frac{|V_s V_R|}{X_L} \cos \delta - \frac{|V_R|^2}{X_L}$$

$$= \frac{|X_L|}{0.5} \cos 30^\circ - \frac{1^2}{0.5} = -0.268 \text{ p.u.}$$

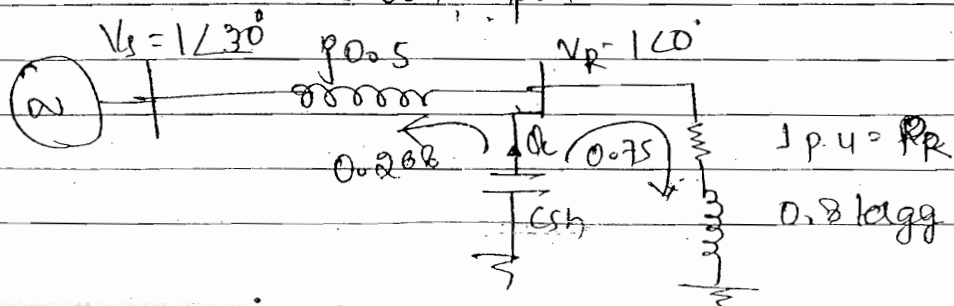
demanding
 ↓
 indicating delivering leading VAR



$$Q_c = -Q_R = -(-0.268) = 0.268 \text{ p.u.} \quad \text{is } Q_{\text{line}}$$

(ii) $P_R = 1 \text{ p.u.}$ 0.8 lagging load.

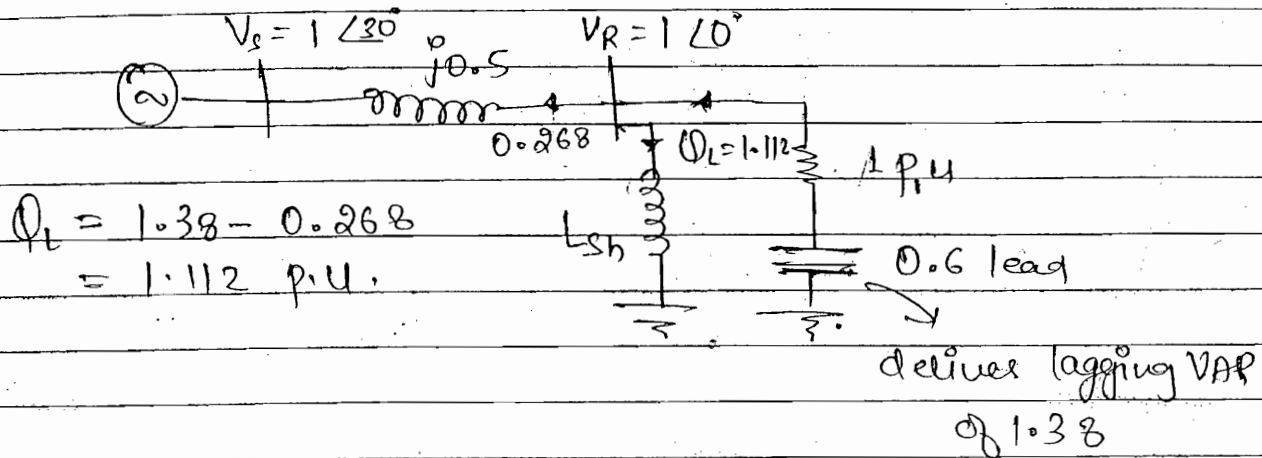
$$Q_{\text{load}} = P_R \times \tan \phi = 1 \times \tan \cos^{-1} 0.8 = 0.75 \text{ p.u.}$$



$$Q_c = Q_{\text{line}} + Q_{\text{load}} = 0.268 + 0.75 = 1.018 \text{ p.u.}$$

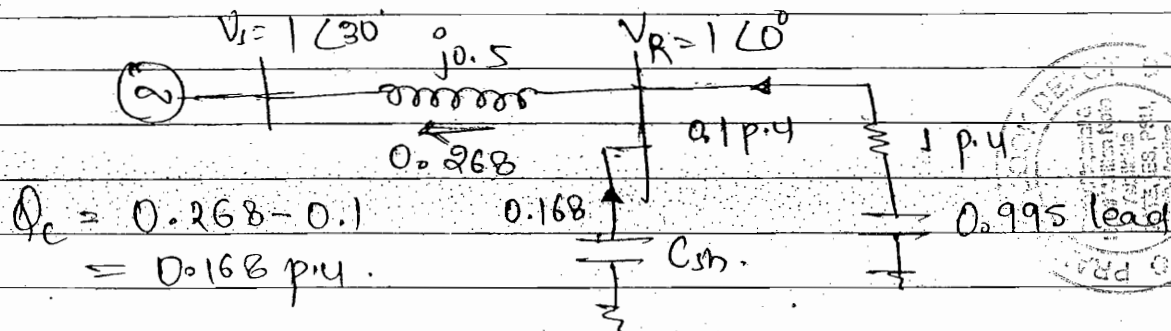
(3) $P_R = 1 \text{ p.u.}, 0.6 \text{ load.}$

$$Q_{\text{load}} = 1 \times \tan(\cos^{-1} 0.6) = 1.38 \text{ p.u.}$$



(4) $P_R = 1 \text{ p.u.}, 0.995 \text{ load.}$

$$Q_{\text{load}} = 1 \times \tan(\cos^{-1} 0.995) = 0.1 \text{ p.u.}$$



- Refer 1 p.u. $\rightarrow 0.995 \rightarrow$ Near to unity leading $\rightarrow$ Resistive more, capacitive less.

$\rightarrow 0.6 \text{ leading} \rightarrow$ far to unity

$\rightarrow$ less resistive, capacitive more

we require more reactive power.

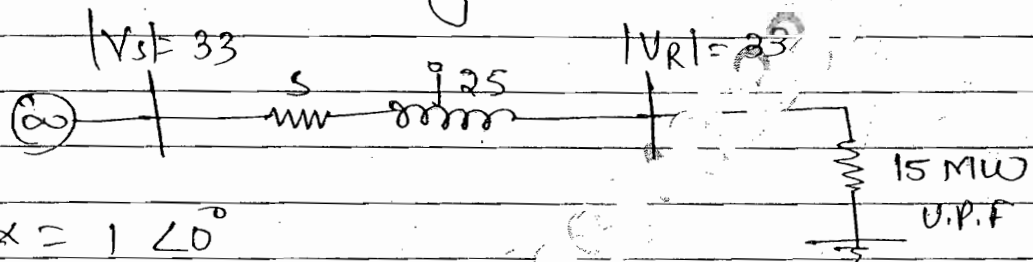
① A - Tr - line has an impedance of $5 + j25 \Omega/\text{phase}$ is operating at $V_s = V_R = 33 \text{ kV}$, find rating of compensator required for a load of

- ① 15 MW U.P.F.
- ② 15 MW 0.8 lagging
- ③ 15 MW 0.8 leading
- ④ 15 MW 0.95 leading

$$\delta = 21.7$$

$$Q_{line} = 6.13$$

Solution :-



$$A \angle \alpha = 1 \angle 0^\circ$$

$$B \angle \beta = Z = 5 + j25 = 25.55 \angle 78.7^\circ$$

$$P_R = \left| \frac{V_s V_R}{B} \right| \cos(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha)$$

$$15 = \frac{33^2}{25.55} \cos(78.7^\circ - \delta) - \left| \frac{1 \times 33^2}{25.55} \right| \cos(78.7^\circ - 0)$$

$$8.3516$$

$$15 + 8.3516 = \frac{33^2}{25.55} \cos(78.7^\circ - \delta) \quad 1 + 8.3516 = \frac{33^2}{25.55} \cos(78.7^\circ - \delta)$$

$$\frac{230.75 \times 25.55}{33^2} = \cos(78.7^\circ - \delta) \quad \cos(78.7^\circ - \delta) = 0.9478$$

$$\cos^{-1} 0.9478 = 78.7^\circ - \delta$$

$$\delta = 78.7^\circ - 56.77^\circ = 21.9^\circ$$

$$Q_R = \left| \frac{V_s V_R}{B} \right| \sin(\beta - \delta) - \left| \frac{V_R^2 A}{B} \right| \sin(\beta - \alpha)$$

$$Q_c = -Q_R = \dots = Q_{line}$$

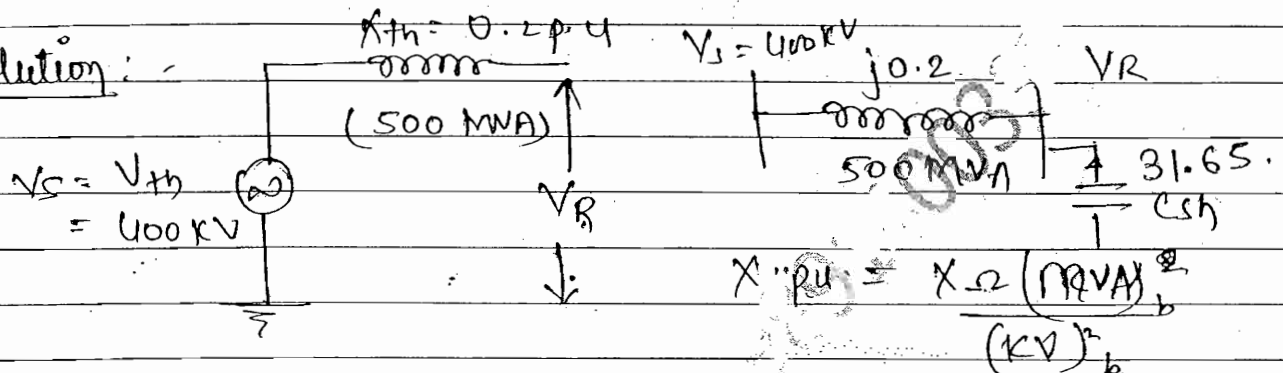
Date _____

① The Thevenin's equivalent imped. of a Bus Bar with 3- ϕ 400kV sys. is 0.2 p.u at a base of 500MVA. Calculate the reactive power needed.

① To Boost the voltage by 5kV at the Bus Bar

② Reduce the voltage by 4kV at the Bus Bar. What equipment is needed in each case.

Solution:



① Boost by 5kV

$$0.2 = X_{\Omega} \times \frac{500}{(400)^2}$$

$$V_R = 400 + 5 = 405kV$$

$$X_{\Omega} = 64 \Omega$$

No. δ parameter line so.

$$Q_R = \frac{V_s V_R}{X_L} - \frac{V_R^2}{X_L} = \frac{400 \times 405}{64} - \frac{405^2}{64}$$

$$= -31.65 \text{ MVAR}$$

$$Q_c = -(-31.65) = +31.65$$

② Reducing by 4kV

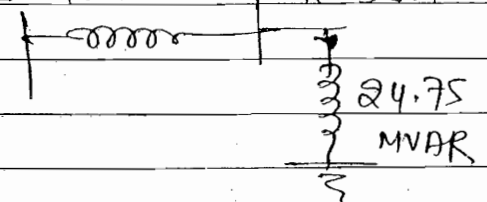
$$V_R = 400 - 4 = 396kV$$

$$V_s = 400kV$$

$$V_R = 396kV$$

$$Q_R = \frac{400 \times 396}{64} - \frac{396^2}{64}$$

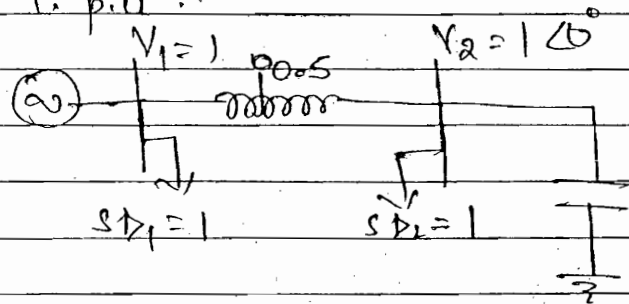
$$= +24.75 \text{ MVAR}$$



$$Q_R = -(24.75) = -24.75 \text{ MVAR}$$

Q A complex power flow are represent on the N/w.
Find the compensator rating required for
maintaining $V_1 = V_2 = 1$ p.u.

Solution $V_s = 1 \angle 0^\circ$



$$S_{D2} = 1 = P_R$$

$$= \frac{V_1 V_2}{X_L} \sin \delta$$

$$1 = \frac{1 \times 1}{0.5} \sin \delta \quad \Rightarrow \quad \sin \delta = 0.5 \quad \boxed{\delta = 30^\circ}$$

$$Q_R = \left| \frac{V_1 V_2}{X_L} \cos \delta - \frac{V_2^2}{X_L} \right|$$

$$= \frac{1 \times 1}{0.5} \cos 30 - \frac{1^2}{0.5} = -0.268$$

$$Q_c = -(-0.268) = 0.268 \text{ compensate}$$

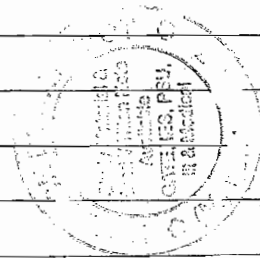
Q Page No. $\rightarrow 52$ Q: 39, 40, 41, 42, 43, 44, 45, 51, 53, 54

(53) $\rightarrow$ Correctly $200 \text{ (K}\Omega\text{)} 7 \text{ kW}$

(39) $\rightarrow$ List I

(d) Reduce Ferranti Effect

Pg No. $\rightarrow 43$ Q: 41, 42, 43



★ imp

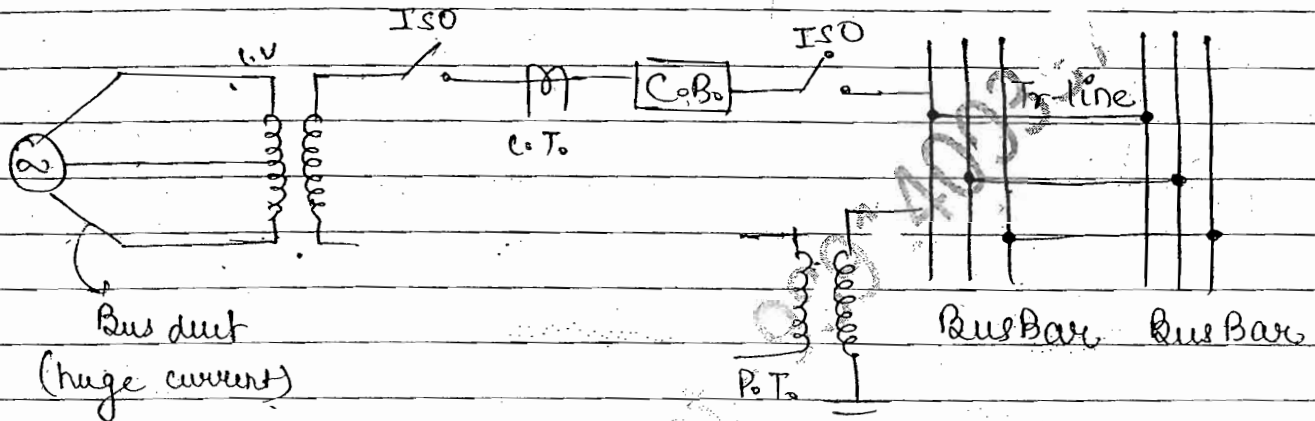
Transmission-line Parameters

Types of Conductor

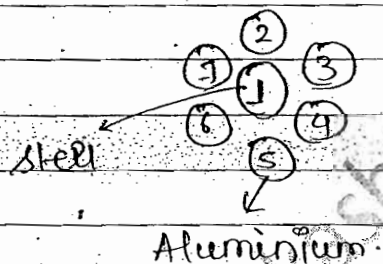
(1) SOLID → Copper → CB, CT, PT terminals

(2) HOLLOW → Copper → Isolators, Bus Duct

(3) STRANDED → ACSR → Tr-lines, Bus Bars



ACSR:- Steel Cored Reinforced Aluminium



$$\text{NO. of strands} = N = (3x^2 - 3x + 1)$$

Total Diameter of conductor

$$= D = (2x - 1)d$$

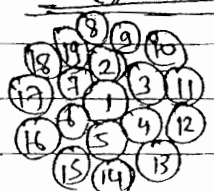
x = layer Number

d = diameter of each strand

7-strand ACSR conductor

x	N	D	Arrangement
1	1	d	(1) $\updownarrow D = d$

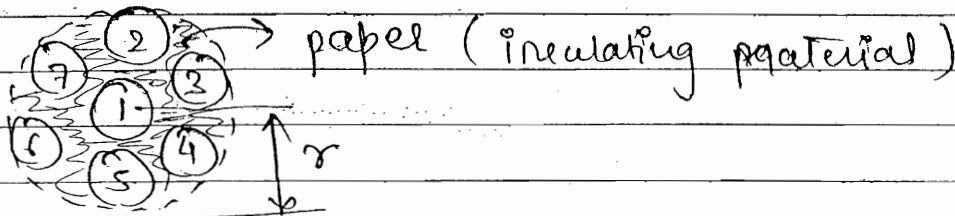
2	7	$3d$	 $\updownarrow D = 3d$
---	---	------	--

3	19	$5d$	 $\updownarrow D = 5d$
---	----	------	--

• Tech. Name of ACSR:-

Zebrua, Panther, Moose, Fox, Dog

Expanded ACSR :- In expanded ACSR, insulating material is kept b/w the strands so that effective radius will be increase and hence inductance and inductive reactance reduce, power transfer capacity $\uparrow$



8/7/2014

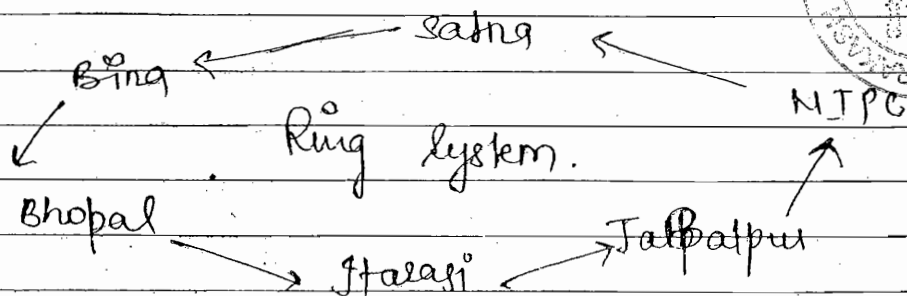
Ring System :- Ad. ① Uniform voltage maintain.

(close loop) ② Reliable.. (Alternate supply possible)

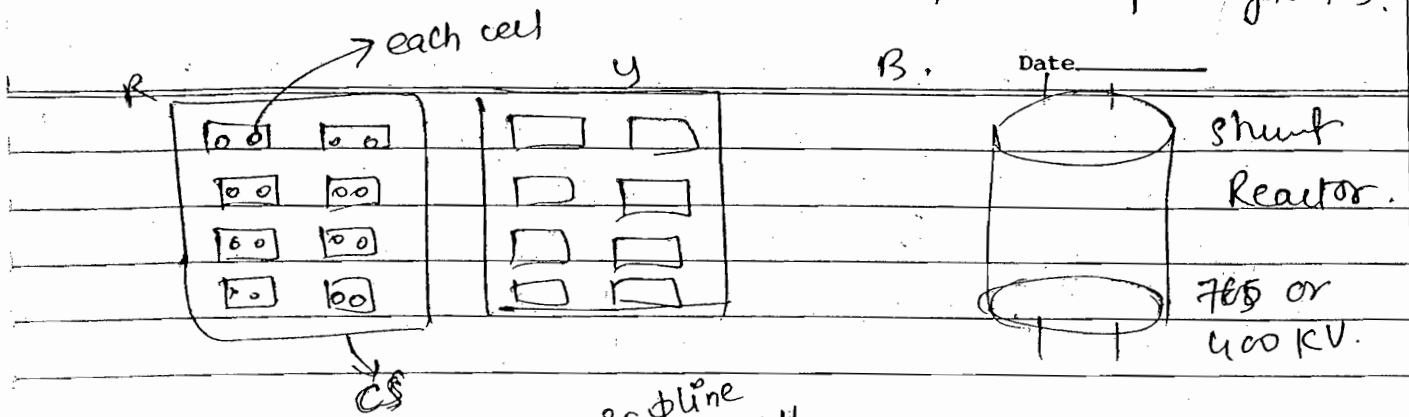
(Open loop) $\rightarrow$ Radial feeder :- Alternate supply not possible

Ad :- Gen-less, demand more, freq. will fall then load will isolates, CB open, so freq. $\uparrow$

$\downarrow$
for isolate work carrier are used

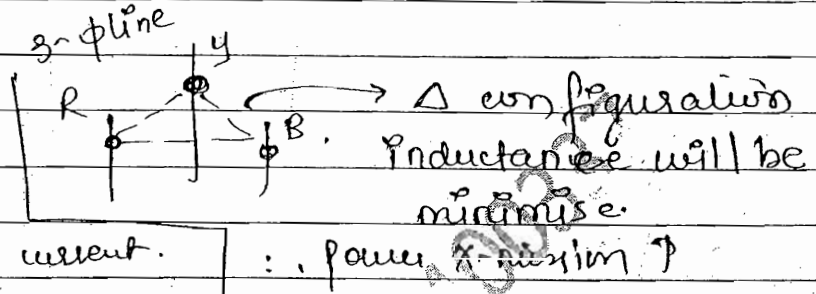


Isolates $\rightarrow$ open when maintenance required

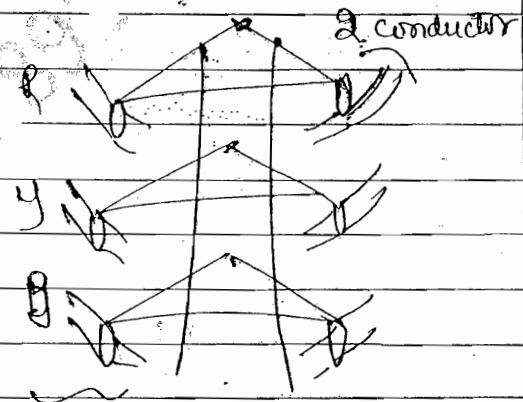
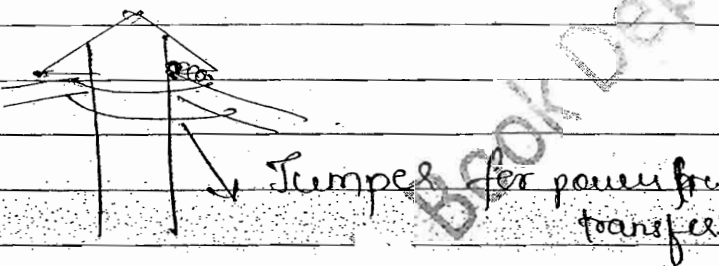
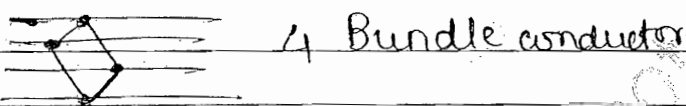


Moose $\rightarrow$ 54

R $\equiv$ $\equiv$ ACSR each
same phase
carrying $\frac{R}{2}$ current.



B $\equiv$ $\equiv$ 2-Bundle Tr-Line

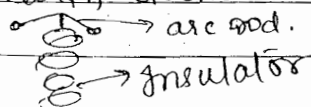


1 circuit 2 circuit
2-Bundle - Double circuit

Coloured ball used in Tr-line which are crossing the river, when fault occur, line will fall into river, for floating the line we use Ball, or for indicator also.

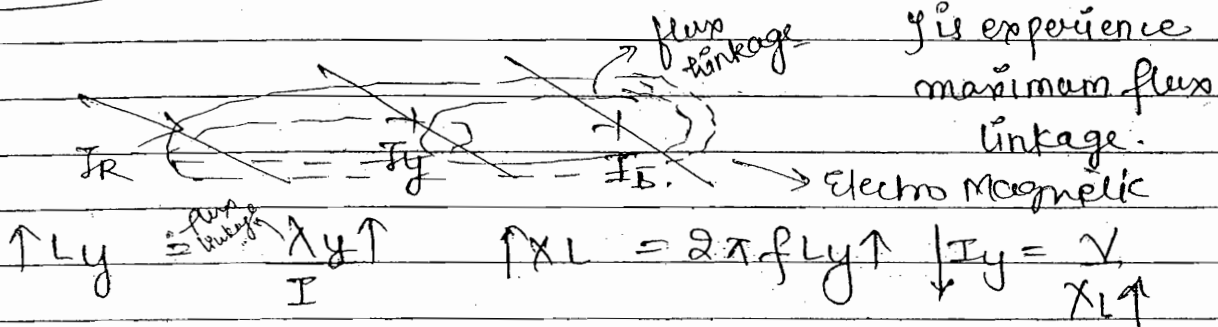
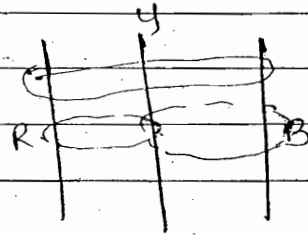
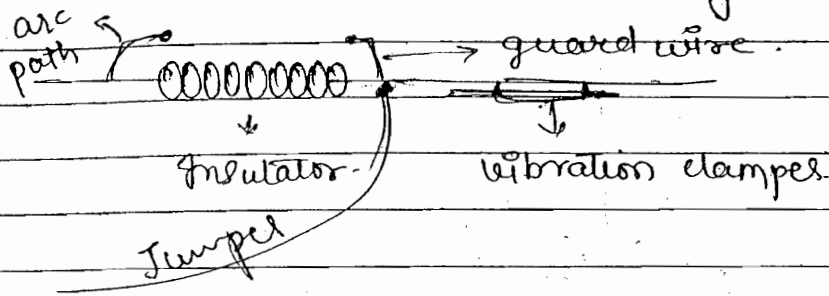
Corona $\rightarrow$ Voltage greater than air dielectric strength

Counter poise $\rightarrow$ discharging the lightning.
Earth electrode $\rightarrow$ deeper length, fastly discharge



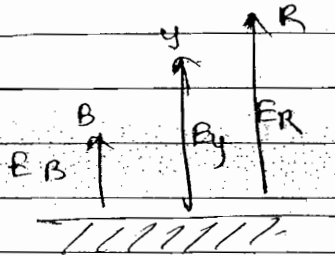
Guard Ring. uniform voltage maintain

- strain Insulator → used in river and road crossing reducing the sag.



$|I_R| \neq |I_Y| \neq |I_B| \Rightarrow I_R + I_Y + I_B \neq 0$ unbalanced fault

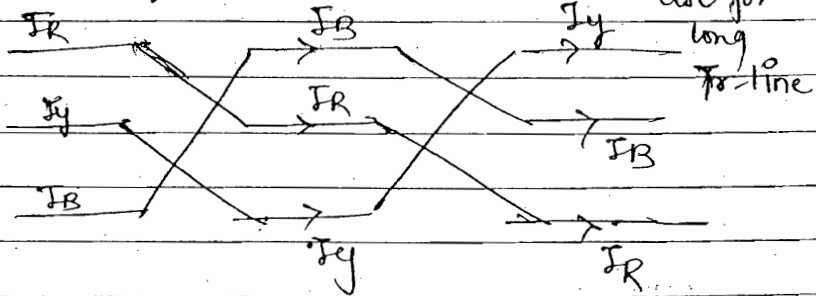
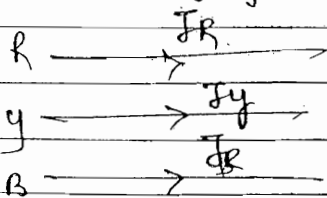
Radio Interference. bcz of Magnetic interference.



$\uparrow E \propto \frac{1}{d^2} \downarrow$
 $|V_R| \neq |V_Y| \neq |V_B|$

Electro static

Nullify by the Radio Interference Transposition



(Done for Balancing).

$V_R + V_Y + V_B \neq 0$
 $I_R + I_Y + I_B \neq 0$

Earth

• Parameters of Tr-line :-

- (1) Inductance (L)
- (2) Capacitance (C)
- (3) Resistance (R)
- (4) Conductance (G)

(1) Inductance (L) :-

$$P_R \propto \frac{1}{\chi_L}$$

Steps :-

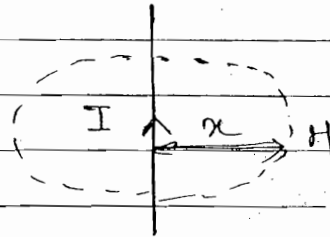
$$(1) \oint H \cdot d\mathbf{x} = I$$

$$(2) B = \mu_0 \mu_r \cdot H$$

$$(3) \phi = B \cdot A$$

$$(4) \lambda = n\phi$$

$$(5) L = \frac{\lambda}{I}$$



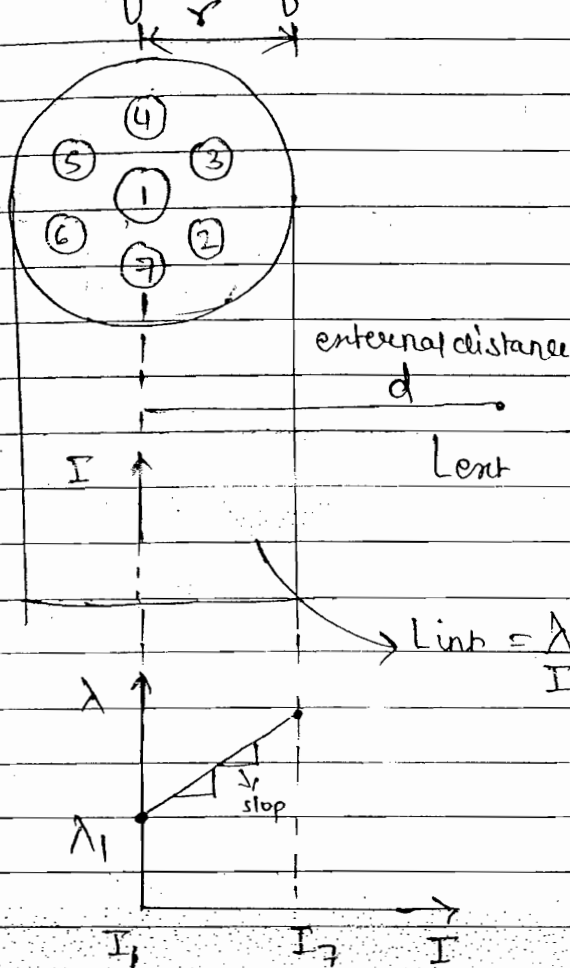
• Inductance of Single Conductor :-

- Assumption :-
- (1) ACSR are solid conductor is considered.
 - (2) Skin and Proximity effect are neglected
 - (3) ACSR are solid conductor consisting of.
 - (a) Internal inductance
 - (b) External inductance

INTERNAL INDUCTANCE :- Internal inductance is due to flux linkage occurs within the conductor areas due to the current flowing in the strands of the conductor.

- This internal inductance proportional to the relative permeability of the conductor material and it is independent of radius or size of conductor use. It is mainly because flux linkage or the flux density increases linearly is proportional

to the current from the centre of conductor to the surface of conductor.



• Internal Inductance: (L_{int})

$$L_{int} = \frac{\mu_r}{2} \times 10^{-7} \text{ H/m}$$

$$L_{int} \propto \mu_r$$

If $\mu_r = 1$

$$L_{int} = \frac{1}{2} \times 10^{-7} \text{ H/m}$$

$$= 0.05 \text{ mH/km}$$

• Independent of value of radius.

• External Inductance: (L_{ext})

$$L_{ext} = \frac{\mu_0}{2\pi} \ln\left(\frac{d}{r}\right) \text{ H/m}$$

$$\mu_0 = 4\pi \times 10^{-7}$$

• Total Inductance (L) :-

$$L = L_{int} + L_{ext}$$

$$L = 0.05 + 0.2 \ln\left(\frac{d}{r}\right) \text{ mH/km}$$

$$L_{ext} = 2 \times 10^{-7} \ln\left(\frac{d}{r}\right) \text{ H/m}$$

$$= 0.2 \ln\left(\frac{d}{r}\right) \text{ mH/km}$$

(OR)

$$L = \frac{1}{2} \times 10^{-7} + 2 \times 10^{-7} \ln\left(\frac{d}{r}\right)$$

$$= 2 \times 10^{-7} \left[\frac{1}{4} + \ln\left(\frac{d}{r}\right) \right]$$

$$= 2 \times 10^{-7} \left[\ln_e e^{1/4} + \ln\left(\frac{d}{r}\right) \right]$$

for hollow conductors

$$L = 2 \times 10^{-7} \ln \frac{d}{r} \text{ H/m.}$$

Date _____

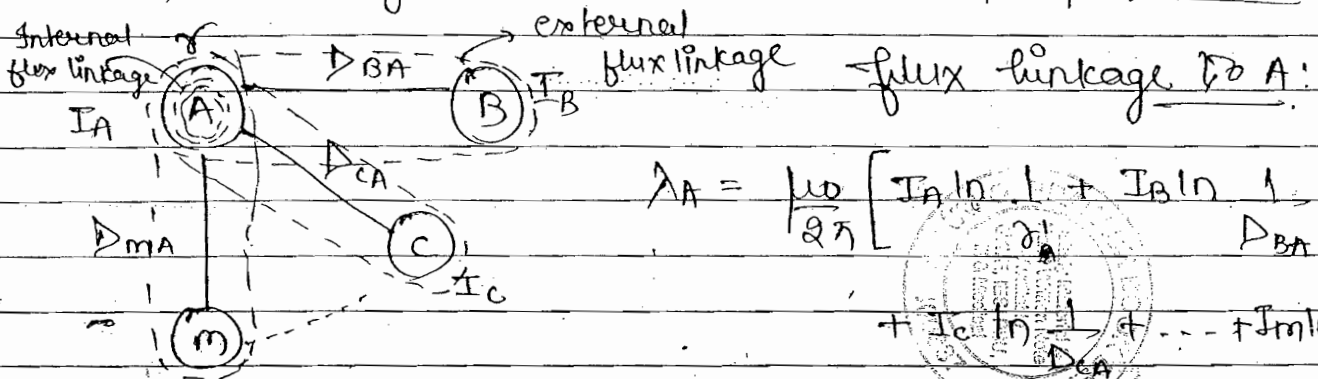
$$L = 2 \times 10^{-7} \ln \left[\frac{de^{1/4}}{r} \right] = 2 \times 10^{-7} \ln \left[\frac{d}{re^{-1/4}} \right]$$

$$L = 2 \times 10^{-7} \ln \left(\frac{d}{0.7788r} \right) \text{ H/m.} \quad \text{where } e^{-1/4} = 0.7788.$$

$$r' = 0.7788r$$

$$L = 2 \times 10^{-7} \ln \frac{d}{r'} \text{ H/m.}$$

• Flux linkage to a conductor in a group of conductors:



At Balance:

$$I_A + I_B + \dots + I_m = 0$$

CASE I:- Inductance of a single ϕ or 2 wire line

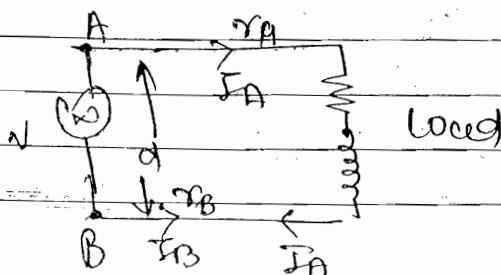
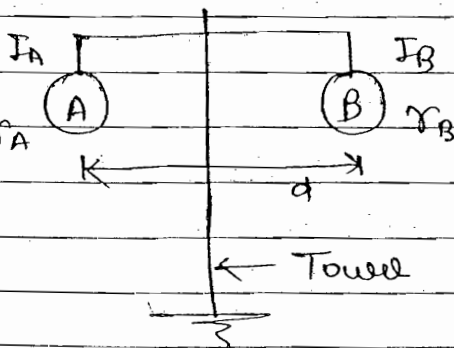
Inductance of A [L_A]:-

Flux linkage to A:-

$$\lambda_A = \frac{\mu_0}{2\pi} \left[I_A \ln \frac{1}{r'_A} + I_B \ln \frac{1}{d} \right]$$

At Balance:-

$$I_A + I_B = 0 \Rightarrow I_A = -I_B$$



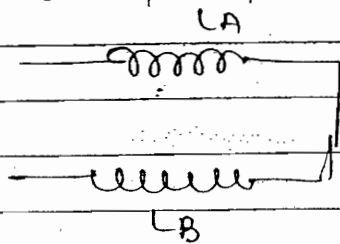
$$\lambda_A = \frac{\mu_0 I_A}{2\pi} \ln \left(\frac{d}{r'_A} \right)$$

$$L_A = \frac{\lambda_A}{I_A} = \frac{\mu_0}{2\pi} \ln \left(\frac{d}{r'_A} \right) \text{ H/m.}$$

- Inductance of B (L_B):-

$$L_B = \frac{\lambda_B}{I_B} = \frac{\mu_0}{2\pi} \ln \left(\frac{d}{r'_B} \right) \text{ H/m.}$$

- Total / loop / circuit Inductance:-



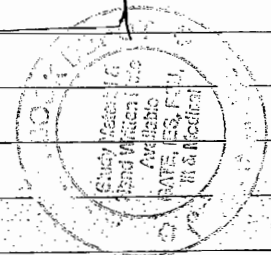
$$L = L_A + L_B = \frac{\mu_0}{\pi} \ln \left(\frac{d}{\sqrt{r'_A r'_B}} \right) \text{ H/m.}$$

If $r'_A = r'_B = r$ $L = \frac{\mu_0}{\pi} \ln \left(\frac{d}{r} \right) \text{ H/m}$

l = length of line (meters)

$$L = L \cdot l \text{ (Henry)}$$

$$X_L = 2\pi f L \quad \Omega$$



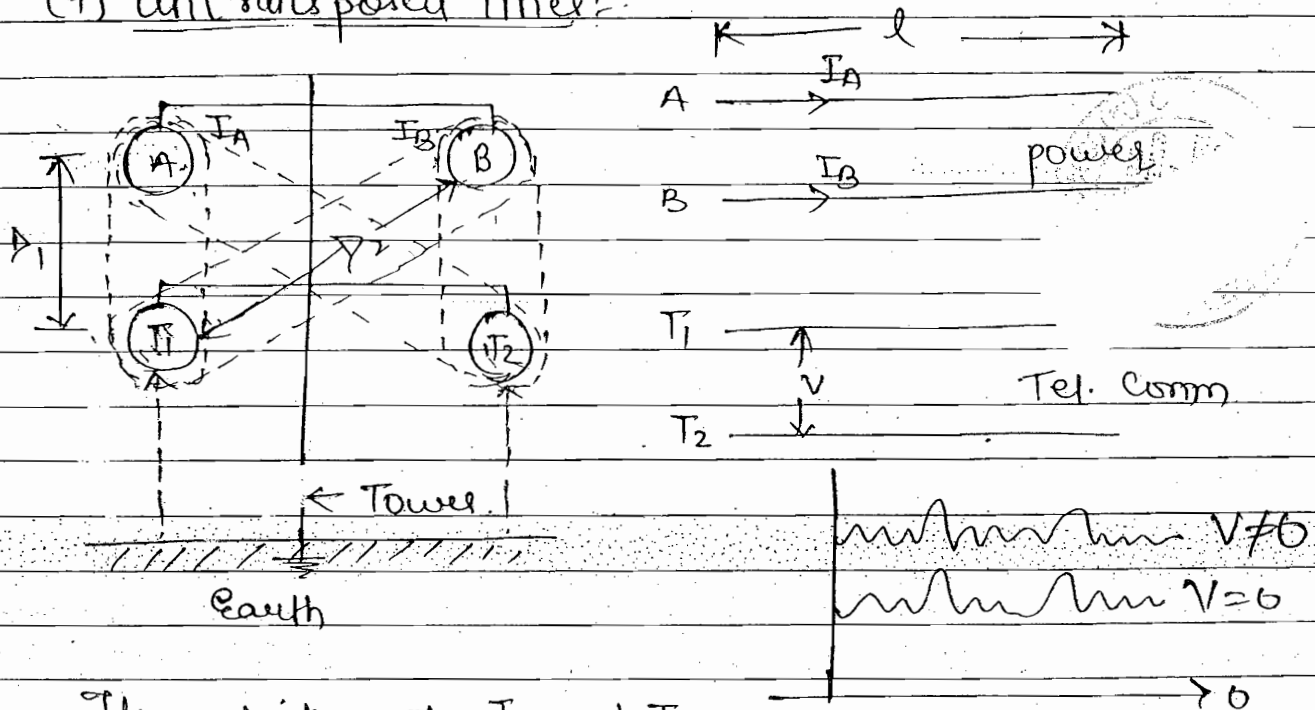
CASE II:- Radio Interference in telecommunication line due to power line

- If the power and telecommunication line are running close to each other. The current flowing in the power line reduces the magnetic flux linkage with the communication line. This will induce an emf in the communication line conductors. Similarly due to earth charges produces electric field on the communication line conductor which will induce emf between the communication line conductor which is called electro static Inductance.

Both this electrostatic and electromagnetic produces interference for the communication signals passing through the communication line. This is called RADIO INTERFERENCE in the communication line. To reduce this effect, if

- (i) either power and both, power and communication line are transposed at regular intervals of length of the Tr-line.

(9) Untransposed lines:



Flux linkage to T_1 and T_2

$$\lambda_{T_1} = \frac{\mu_0}{2\pi} \left[I_A \ln \frac{1}{D_1} + I_B \ln \frac{1}{D_2} \right]$$

$$\lambda_{T_2} = \frac{\mu_0}{2\pi} \left[I_A \ln \frac{1}{D_2} + I_B \ln \frac{1}{D_1} \right]$$

$$\text{Net } \lambda_T = \lambda_{T_1} - \lambda_{T_2}$$

$$= \frac{\mu_0}{2\pi} \left[I_A \ln \frac{D_2}{D_1} + I_B \ln \frac{D_1}{D_2} \right]$$

At Balance $I_A + I_B = 0$, $I_B = -I_A$

$$\lambda_T^{\infty} = \frac{\mu_0 I_A}{2\pi} \ln \left(\frac{D_2}{D_1} \right)^2$$

$$= \frac{\mu_0 I_A}{\pi} \ln \left(\frac{D_2}{D_1} \right)$$

$$L = \frac{\lambda_A}{I_A} = \frac{\mu_0}{\pi} \ln \left(\frac{D_2}{D_1} \right)$$

Voltage induced b/w communication line due to I_A is

$$V = (2\pi f L) I_A$$

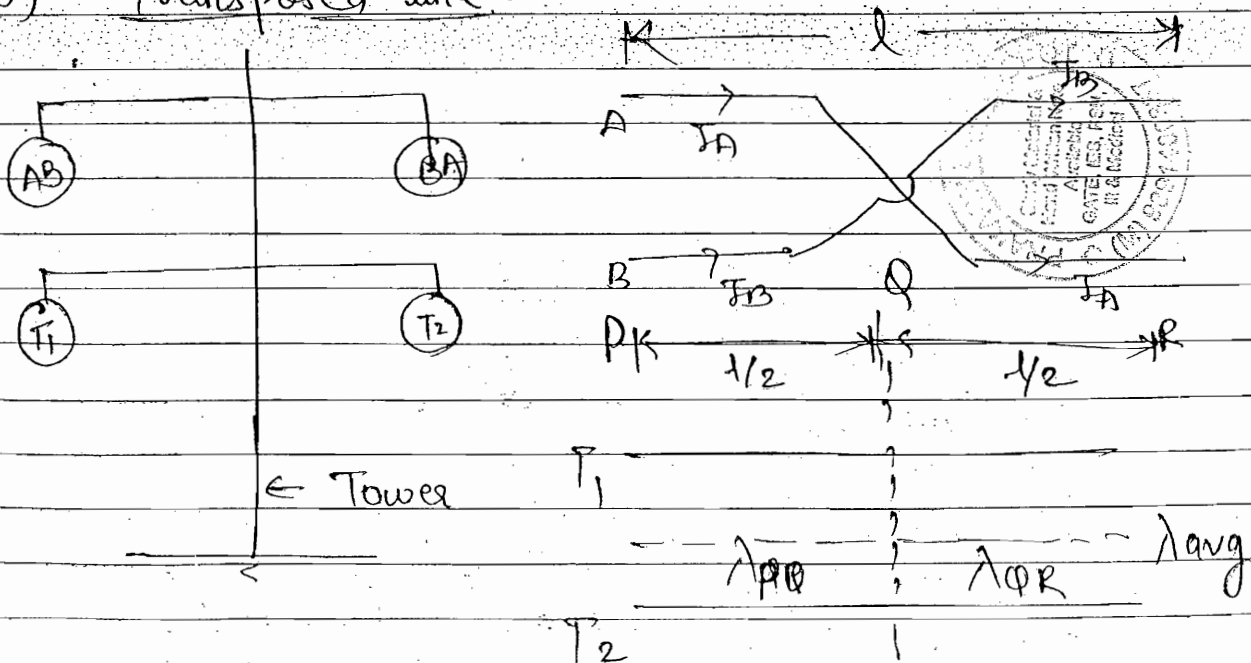
$$= 2\pi f I_A \cdot \frac{\mu_0}{\pi} \ln \left(\frac{D_2}{D_1} \right)$$

$$V = 2\mu_0 f I_A \ln \left(\frac{D_2}{D_1} \right) \quad \text{V/m.}$$

D_1 = shortest Distance

D_2 = longest distance

(b) Transposed line:



Flux linkage b/w PQ and QR.

$$\lambda_{PQ} = \frac{\mu_0}{2\pi} \left[I_A \ln \left(\frac{D_2}{D_1} \right) + I_B \ln \left(\frac{D_1}{D_2} \right) \right]$$

$$\lambda_{QR} = \frac{\mu_0}{2\pi} \left[I_B \ln \left(\frac{D_2}{D_1} \right) + I_A \ln \left(\frac{D_1}{D_2} \right) \right]$$

$$\lambda_{avg} = \frac{\lambda_{PQ} \times l/2 + \lambda_{QR} \times l/2}{l} = \frac{1}{2} [\lambda_{PQ} + \lambda_{QR}]$$

$$\lambda_{avg} = \frac{1}{2} \cdot \frac{\mu_0}{2\pi} \left[(I_A + I_B) \ln \frac{D_2}{D_1} + (I_A + I_B) \ln \frac{D_1}{D_2} \right]$$

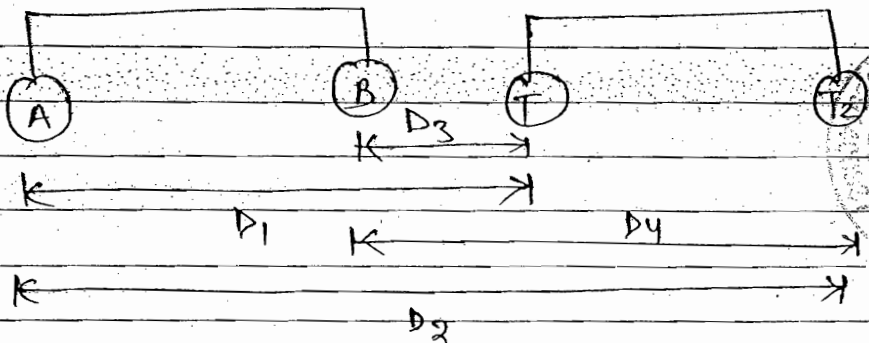
At Balance $(I_A + I_B) = 0$

$$\bullet \lambda_{avg} = 0$$

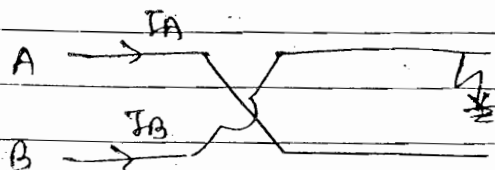
$$\bullet L = \frac{\lambda_{avg}}{I_A} = 0$$

$$\bullet V = 2\pi f L \cdot I_A = 0$$

practical case:

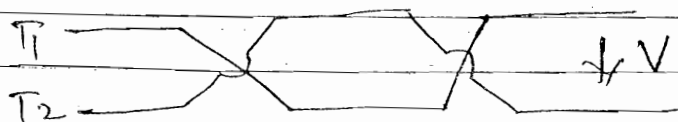


• Through distance we can't make $\lambda_{avg} = 0$. In this case $(I_A + I_B)$ help in making $\lambda_{avg} = 0$



$L_{g1}, L_{L2}, L_{L3} (I_A + I_B) \neq 0$

$$\therefore V \neq 0$$



for making voltage = 0
Telecommunication line
used

at regular interval

Date _____

are also transposed, so that V can be reduced.

Case III:- Radio Interference in 3 ϕ power Tr-line

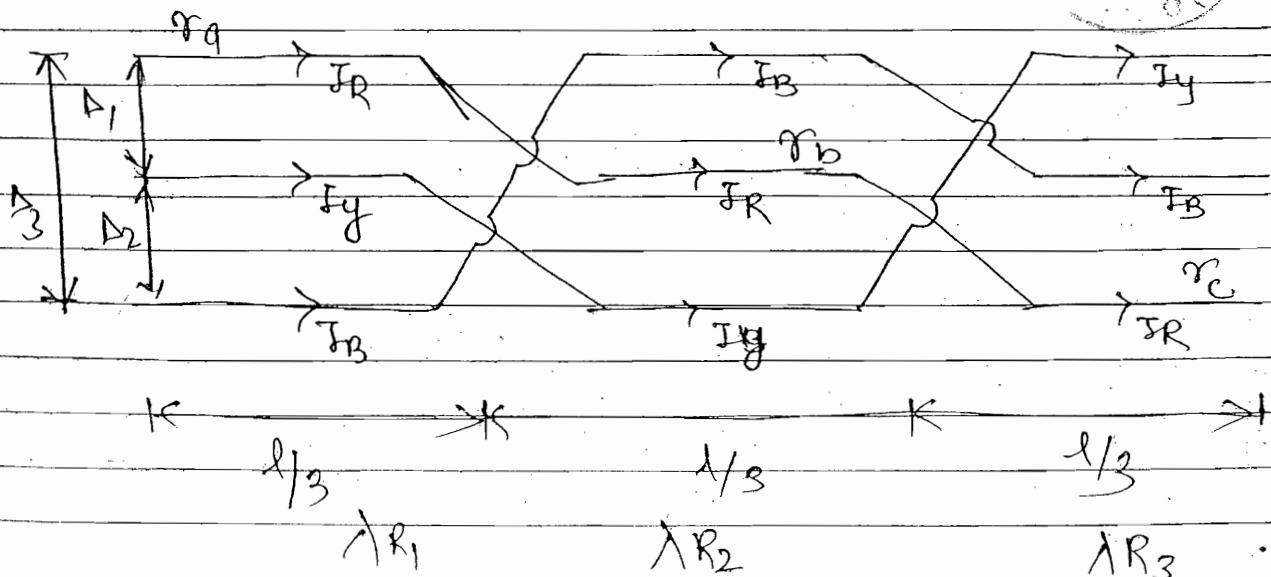
In case of 3- ϕ Tr-line due to electromagnetic induction the middle conductor experiences maximum flux linkage so that X_L & L increase so that current reduce. This will produce unbalance in the system currents that is $I_R + I_Y + I_B \neq 0$ occurs.

- The bottom most conductor which is nearest to the earth experience maximum electric field stress compare to the other conductors causing unbalance in the voltage i.e. $V_R + V_Y + V_B \neq 0$ occurs. This is called electrostatic induction.

Both electrostatic and electromagnetic produces unbalance to sys which is called radio interference in the 3 ϕ line.

- To reduce this effect and maintain balanced in voltages and currents Tr-line is transposed at regular intervals of length of the line.

- Consider transposed line for untransposed it is mentioned.



Flux linkage to R-phase:-

$$\lambda_{R1} = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r'_a} + I_Y \ln \frac{1}{D_1} + I_B \ln \frac{1}{D_3} \right]$$

$$\lambda_{R2} = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r'_b} + I_Y \ln \frac{1}{D_2} + I_B \ln \frac{1}{D_1} \right]$$

$$\lambda_{R3} = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r'_c} + I_Y \ln \frac{1}{D_3} + I_B \ln \frac{1}{D_2} \right]$$

$$\lambda_{avg} = \frac{\lambda_{R1} + \lambda_{R2} + \lambda_{R3}}{3}$$

$$\lambda_{avg} = \frac{1}{3} \cdot \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r'_a r'_b r'_c} + (I_Y + I_B) \ln \frac{1}{D_1 D_2 D_3} \right]$$

At Balance $I_Y + I_B = -I_R$

$$\lambda_{avg} = \frac{\mu_0}{2\pi} I_R \ln \left(\frac{D_1 D_2 D_3}{r'_a r'_b r'_c} \right)^{1/3}$$

$$L_R = L_{ph} = \frac{\lambda_{avg}}{I_R} = \frac{\mu_0}{2\pi} \ln \left(\frac{D_1 D_2 D_3}{r'_a r'_b r'_c} \right)^{1/3}$$

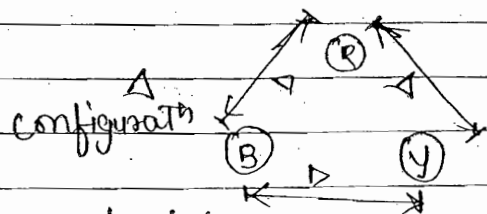
H/m/phase.

(1) If $r'_a = r'_b = r'_c = r'$

$$L_{ph} = \frac{\mu_0}{2\pi} \ln \left(\frac{D_1 D_2 D_3}{r'} \right)^{1/3} \text{ H/m/phase}$$

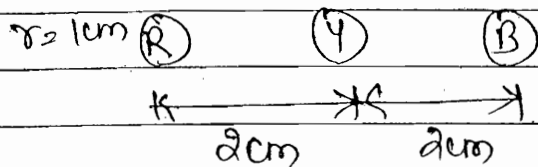
(2) If $D_1 = D_2 = D_3 = D$

$$L_{ph} = \frac{\mu_0}{2\pi} \ln \left(\frac{D}{r'} \right) \text{ H/m/phase}$$

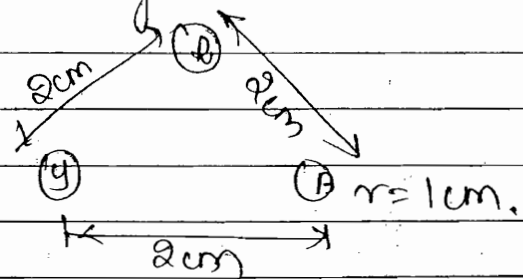


Q Find the inductance / phase for the following configuration.

① Horizontal



② Triangular



Solution

$$L_{ph} = \frac{2}{2\pi} \times 10^{-7} \ln \left(\frac{2 \times 2 \times 2}{0.7788 \times 1 \times 10^{-2}} \right)^{1/3}$$

$$= 1.15 \times 10^{-6} \text{ H/m}$$

$$= 1.15 \text{ mH/km}$$

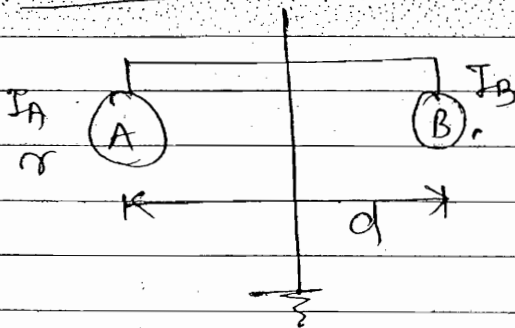
$$L_{ph} = \frac{2}{2\pi} \times 10^{-7} \ln \left(\frac{2}{0.7788 \times 10^{-2}} \right)$$

$$= 1.10 \text{ mH/km}$$

$$L_{\Delta} < L_H$$

$$P_{\Delta} > P_H$$

Case IV Bundle Conductor:-



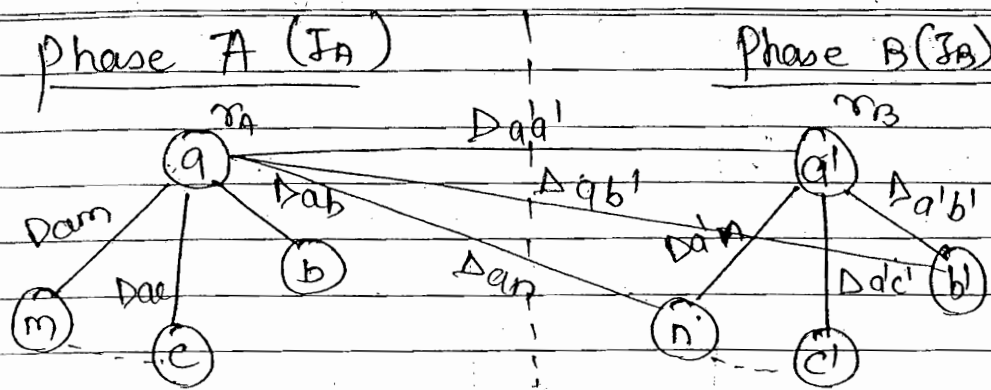
$$L_A = L_B = 2 \times 10^{-7} \ln \frac{d}{r}$$

$$L_A = L_B = 2 \times 10^{-7} \ln \frac{D_m}{D_s}$$

D_m = Mutual geometric Mean Distance (GMD)

D_s = Self GMD (or)

= GMR [Geometric Mean Radius]



m = No. of Conductor Bundle of phase A

n = No. of Conductor Bundle of phase B.

$$L_A = 2 \times 10^{-7} \ln \left(\frac{D_{MAB}}{D_{sA}} \right)$$

$$L_B = 2 \times 10^{-7} \ln \left(\frac{D_{MBA}}{D_{sB}} \right)$$

$$D_{MAB} = D_{MBA} = \left[(D_{aa'} D_{ab'} \dots D_{an}) (D_{ba'} D_{bb'} \dots D_{bn}) \dots (D_{ma'} D_{mb'} \dots D_{mn}) \right]^{\frac{1}{m \times n}}$$

$$D_{sA} = \left[(D_{aa} D_{ab} \dots D_{am}) (D_{ba} D_{bb} \dots D_{bm}) \dots (D_{ma} D_{mb} \dots D_{mm}) \right]^{\frac{1}{m^2}}$$

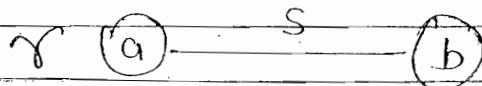
where $D_{aa} = D_{bb} = \dots = D_{mm} = r'_A = 0.7788 r_A$

$$D_{sB} = \left[(D_{a'a'} D_{a'b'} \dots D_{a'n}) (D_{b'a'} D_{b'b'} \dots D_{b'n}) \dots (D_{n'a'} D_{n'b'} \dots D_{nn}) \right]^{\frac{1}{n^2}}$$

where $D_{a'a'} = D_{b'b'} = \dots = D_{nn} = r'_B = 0.7788 r_B$

Q Find the self GMD for the following conductor configⁿ

(i) Bundle of 2 :-

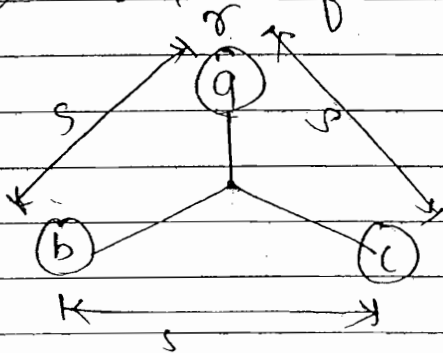


$$D_s = \left[(D_{aa} D_{ab}) (D_{bb} D_{ba}) \right]^{1/2 \times 2}$$

$$= \left[(r' \cdot s) (r' \cdot s) \right]^{1/4}$$

$$D_s = (r' \cdot s)^{1/2}$$

(2) Bundle of Conductor 3.

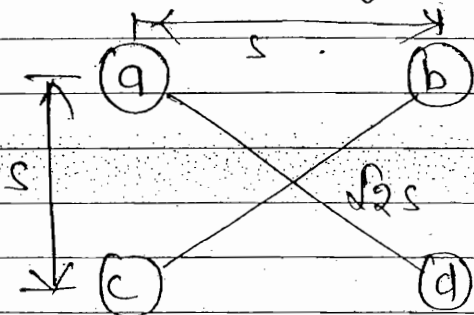


$$D_s = \left[(D_{aa} D_{ab} D_{ac}) (D_{bb} D_{ba} D_{bc}) (D_{cc} D_{ca} D_{cb}) \right]^{1/3 \times 3}$$

$$= \left[(r' \cdot s \cdot s) (s \cdot s \cdot r') (s \cdot r' \cdot s) \right]^{1/9}$$

$$= \left[r' s^2 \right]^{1/3}$$

(3) Bundle of Conductor 4.



$$D_s = \left[(D_{aa} D_{ad} D_{ab} D_{ac}) (D_{bb} D_{ba} D_{bc} D_{bd}) (D_{cc} D_{ca} D_{cb} D_{cd}) (D_{dd} D_{dc} D_{da} D_{db}) \right]^{1/4 \times 4}$$

$$= (\sqrt{2} r' \cdot s^3)^{1/4}$$

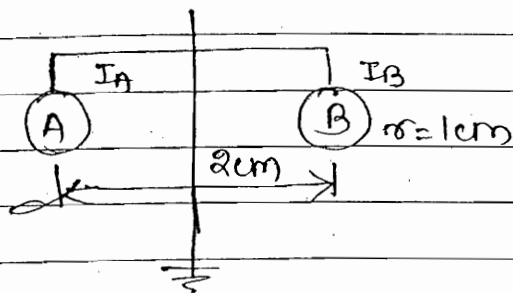
$$> 1.09 (r' \cdot s^3)^{1/4}$$

Phap:- 1 $\rightarrow$ 1 to 2.

Qmp Comparison of Bundle or Without Bundle 9/7/2014.

for the following configuration Calculate inductance per phase

(1) without Bundle conductor.

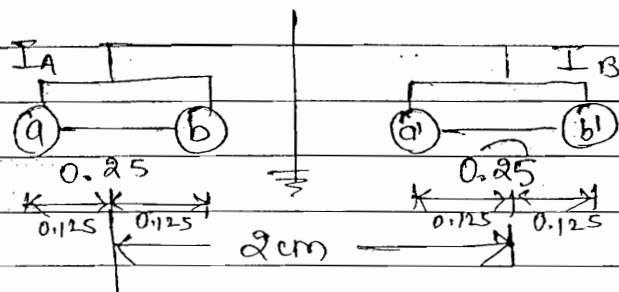


$$L_A = L_B = 2 \times 10^{-7} \ln \left(\frac{d}{r'} \right)$$

$$= 2 \times 10^{-7} \ln \frac{2}{0.7788 \times 10^{-2}}$$

$$= 1.109 \text{ mH/km}$$

(2) With Bundle Conductor.



$$L_A = L_B = 2 \times 10^{-7} \ln \frac{D_m}{D_s}$$

$$D_s = (D_{aa'} D_{ab} D_{ba} D_{bb'})^{1/2}$$

$$= \sqrt{(0.7788 \times 10^{-2})^2 \times (0.25)^2}$$

$$= 0.044 \text{ m}$$

$$D_m = (D_{aa'} D_{ab} D_{ba} D_{bb'})^{1/4}$$

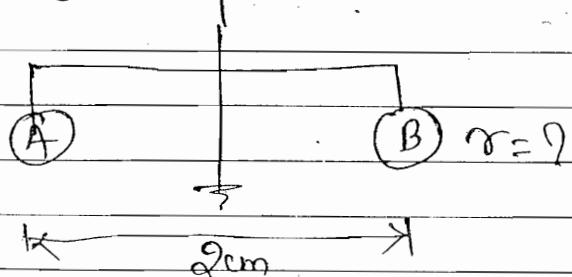
$$= [2 \times 2.25 \times 1.75 \times 2]^{1/4}$$

$$= 1.99 \approx 2 \text{ m}$$

$$L_A = L_B = 2 \times 10^{-7} \ln \left(\frac{2}{0.044} \right) = 0.768 \text{ mH/km}$$

• With Bundle conductor power transfer is more.

Q To get $L_A = 0.768 \text{ mH/km}$ without Bundle how much λ required?



$$L_A = 0.768 \times 10^{-6} \text{ H/m}$$

$$= 2 \times 10^{-7} \ln \frac{\lambda}{0.7788 \times r}$$

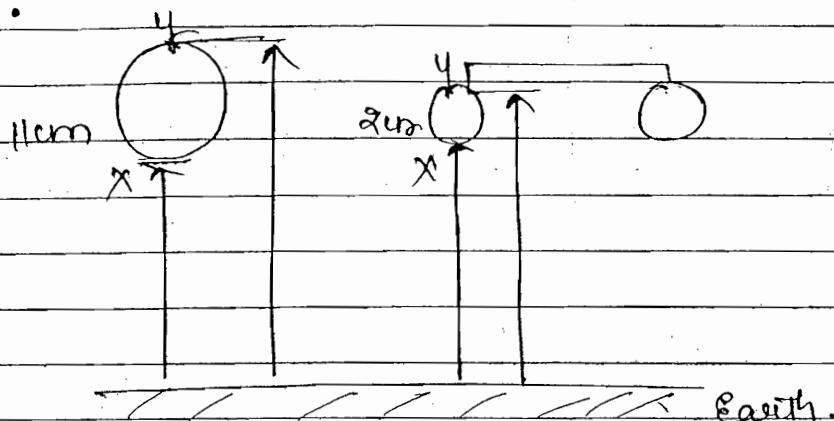
$$r = 5.6 \text{ cm}$$

$$\Rightarrow A = \pi r^2 = \pi \times (5.6)^2$$

$$\approx 100 \text{ cm}^2$$

Bundle $\therefore r = 1 \text{ cm} \Rightarrow 2\pi r^2 = 2\pi (1)^2 = 6.28 \text{ cm}^2$.

- More area will required without bundle, cost will $\uparrow$.



- Corona and radio interference is less in Bundle conductor.

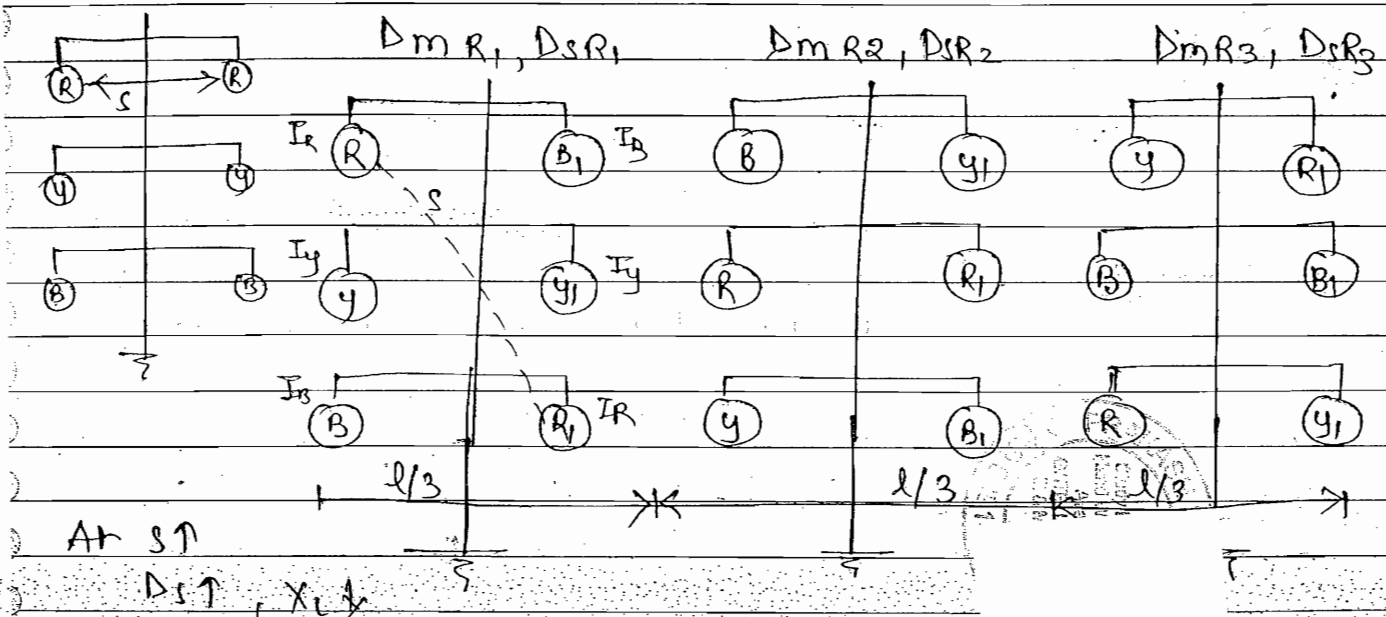
• Advantages of Bundle conductor:-

- (1) Effective Radius of conductor D_e will increase.
- (2) Inductance and inductive reactance are reduced.
- (3) Power transferred capability is increased.
- (4) Volume of the conductor is reduce, so that No. of towers will minimise.
- (5) Electrical field stress on the conductor are minimised.
- (6) Surge impedance is reduce.
- (7) Surge impedance loading is increased.
- (8) Corona power loss is reduce.
- (9) Interference b/w adjacent line is minimised.

Because of above advantage Bundle conductors are practically used for power transfer of higher rating in 220 kV and above voltage level.

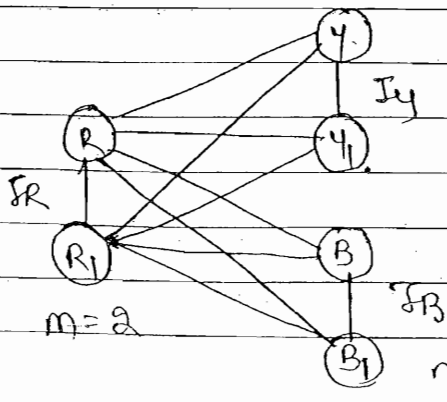
Case IV Double Circuit line :- In case of two conductor bundle $D_s = (r' s)^{1/2}$ that is $D_s \propto s^{1/2}$ by $\uparrow s$, $D_s \uparrow$ so that L and X_L are reduced. Power transferred is $\uparrow$. This principle is used in case of double circuit line.

- It consists of two circuit each has R,Y,B. phases kept one on one side of tower.



$$L_R = L_{ph} = 2 \times 10^{-7} \ln \left(\frac{D_{mR_1} D_{mR_2} D_{mR_3}}{D_{sR_1} D_{sR_2} D_{sR_3}} \right)^{1/3} \text{ H/m/phase}$$

Calculation of D_{mR}



$$D_{mR_1} = \left[(D_{RY_1} D_{RY_2} D_{RB_1} D_{RB_2}) (D_{R_1Y_1} D_{R_1Y_2} D_{R_1B_1} D_{R_1B_2}) \right]^{1/4}$$

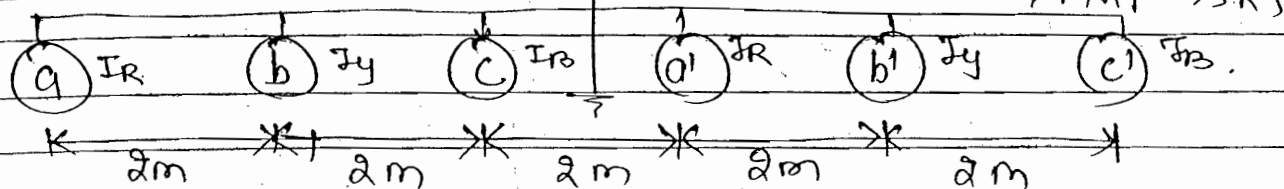
Similarly calculate D_{mR_2} , D_{mR_3}

Calculation of D_{sR}

$$D_{sR_1} = \left[D_{RR} D_{RR_1} D_{R_1R} D_{R_1R_1} \right]^{1/2}$$

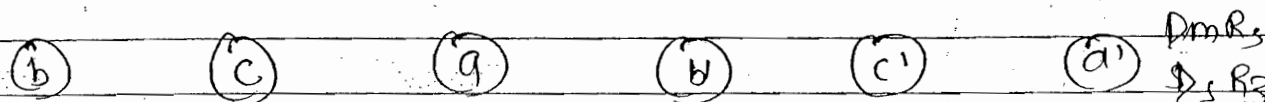
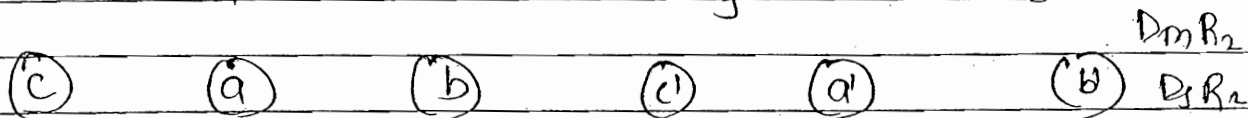
Similarly calculate D_{sR_2} , D_{sR_3}

Conventional L:- Conductor radius = 12 mm.

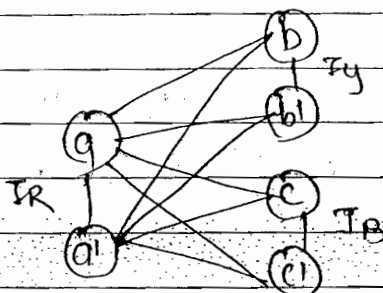


Assumption $\rightarrow$ Transposition

$a a' \rightarrow I_R$ $b b' \rightarrow I_Y$ $c c' \rightarrow I_B$



Calculate the D_{mR}



$$D_{mR1} = \left([D_{ab} D_{ab'} D_{ac} D_{ac'}] [D_{a'b} D_{a'b'} D_{a'c} D_{a'c'}] \right)^{1/8 \times 4}$$

$$= [2 \times 8 \times 4 \times 10 \times 4 \times 2 \times 2 \times 4]^{1/8}$$

$$= 8.77 \text{ m}$$

$$m=2 \quad n=4 \quad D_{mR2} = [2 \times 8 \times 2 \times 4 \times 4 \times 2 \times 8 \times 2]^{1/8}$$

$$= 3.36 \text{ m}$$

$$D_{mR3} = [4 \times 2 \times 2 \times 4 \times 10 \times 4 \times 6 \times 2]^{1/8}$$

$$= 3.77 \text{ m}$$

$$D_{SR1} = (D_{aa} D_{aa'} D_{a'a} D_{a'a'})^{1/2}$$

$$= [(0.7788 \times 12 \times 10^{-3})^2 \times 6^2]^{1/4} = 0.236$$

$$= D_{SR2} = D_{SR3}$$

$$L_R = l_{ph} = 2 \times 10^{-7} \ln \left(\frac{D_{mR1} D_{mR2} D_{mR3}}{D_{SR1} D_{SR2} D_{SR3}} \right)^{1/3}$$

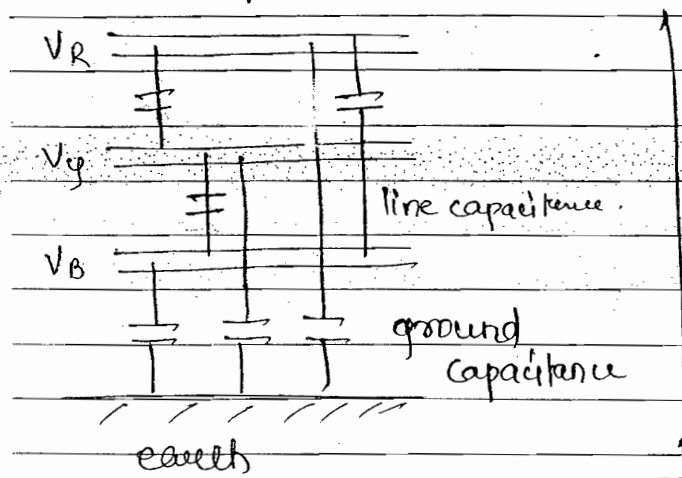
$$= 2 \times 10^{-7} \ln \left[\frac{3.97 \times 3.36 \times 3.97}{(0.236)^3} \right]^{1/3}$$

$$= 0.546 \text{ mH/km/phase}$$

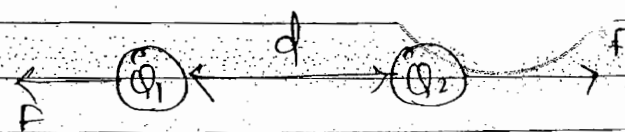
CAPACITANCE:

In case of NO-load or light load condition of a Tr-line charging current flows through the line due to capacitance exist b/w the conductors and conductors to the ground.

Due to capacitance effect under NO load $V_R > V_S$ (Ferranti effect occurs) for compensating this ferranti effect shunt reactor capacitor has to be used for designing proper value of shunt reactor line capacitance has to be calculated According to the configuration of the Tr-line



Columb's law



$$F = \frac{Q_1 Q_2}{4\pi\epsilon_0\epsilon_r d^2}$$

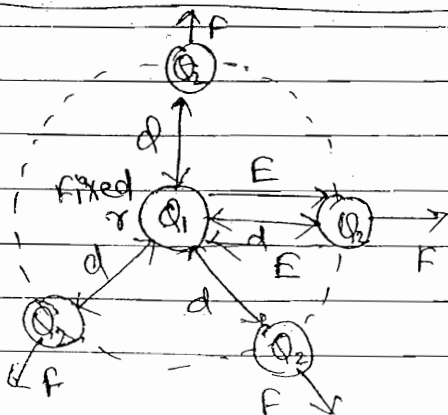
$$E = \frac{F}{Q_2} = \frac{Q_1}{4\pi\epsilon_0\epsilon_r d^2}$$

$$\text{Voltage} = dV = \frac{\text{work done}}{\text{charge}} = \frac{\text{Force} \times \text{Distance}}{\text{Charge}}$$

$$= \frac{F}{Q} \cdot dx$$

$$dV = - E \cdot dx$$

bcuz E is working in opp. direct



$$V = - \int_d^r E \cdot dr$$

$$C = \frac{Q}{V}$$

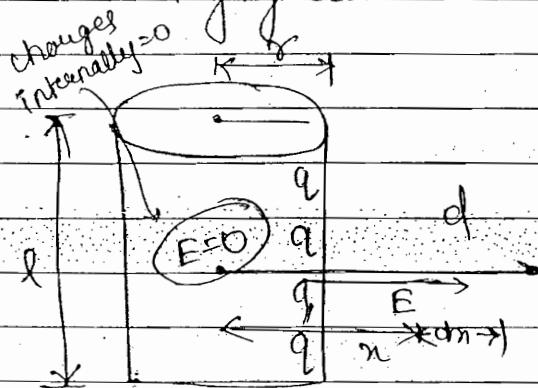
where r = smaller distance

d = longer distance, it may be ∞

• Capacitance due to Single Conductor -

Assumption: ① Tr-line is of ACSR conductor having line charge configuration.

② Charge is accumulating on the surface of the conductor bcoz the conductivity is higher so that the electrical field at the center of the conductor is negligible. $\therefore$ charge is neglected at the center.



$$\sigma = \infty$$

$$J = \sigma \cdot E$$

$$E = \frac{J}{\sigma} = \frac{J}{\infty} = 0$$

$E=0$ inside so charges are at surface, E is not axially, it is radially.

q = line charge c/m.

$$E = \frac{q}{2\pi \epsilon_0 \epsilon_r r}$$

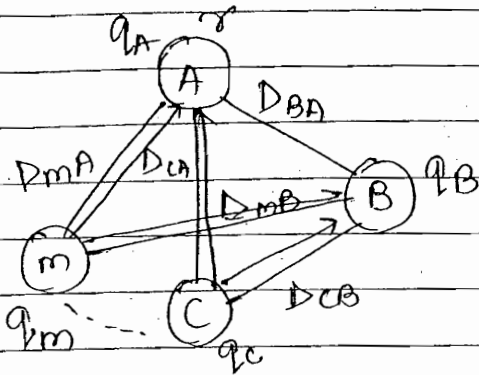
$$V = - \int_d^r E \cdot dr$$

$$= - \int_d^r \frac{q}{2\pi \epsilon_0 \epsilon_r r} \cdot dr$$

$$V = \frac{q}{2\pi \epsilon_0 \epsilon_r} \ln \left(\frac{d}{r} \right)$$

$$C = \frac{Q}{V} = \frac{2\pi \epsilon_0 \epsilon_r}{\ln(d/r)} \text{ f/m}$$

• Voltage Between 2 Conductors in a group of Conductors

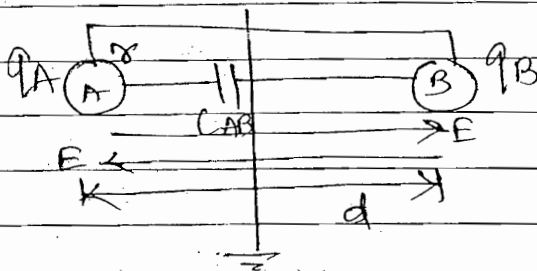


Voltage Between AB: -

$$V_{AB} = \frac{1}{2\pi\epsilon_0\epsilon_r} \left[q_A \ln \frac{D_{AB}}{r} + q_B \ln \frac{D_{BA}}{r} + q_C \ln \frac{r}{D_{CA}} + q_B \ln \frac{r}{D_{CB}} + q_m \ln \frac{D_{mA}}{D_{mB}} \right]$$

At Balance $q_A + q_B + \dots + q_m = 0$

Capacitance Between Conductors of single phase 2-wire line



$$C_{AB} = \left| \frac{q_A}{V_{AB}} \right| = \left| \frac{q_B}{V_{AB}} \right|$$

$$V_{AB} = V_A - V_B = \frac{q_A}{2\pi\epsilon_0\epsilon_r} \ln \left(\frac{d}{r} \right) - \frac{q_B}{2\pi\epsilon_0\epsilon_r} \ln \left(\frac{d}{r} \right)$$

$$V_{AB} = \frac{1}{2\pi\epsilon_0\epsilon_r} \left[q_A \ln \frac{d}{r} - q_B \ln \frac{d}{r} \right]$$

$$= \frac{1}{2\pi\epsilon_0\epsilon_r} \left[q_A \ln \frac{d}{r} + q_B \ln \frac{r}{d} \right]$$

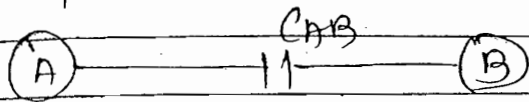
at Balance $q_B = -q_A$

$$V_{AB} = \frac{q_A}{2\pi\epsilon_0\epsilon_r} \ln \left(\frac{d}{r} \right)^2$$

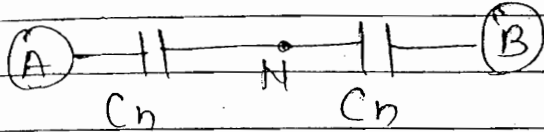
$$V_{AB} = \frac{q_A}{\pi\epsilon_0\epsilon_r} \ln \left(\frac{d}{r} \right)$$

$$C_{AB} = \frac{q_A}{V_{AB}} = \frac{\pi\epsilon_0\epsilon_r}{\ln(d/r)} \text{ F/m}$$

- Capacitance to Neutral (C_n) or Capacitance / phase:-



$$C_{AB} = \frac{C_n \cdot C_n}{C_n + C_n} = \frac{C_n}{2}$$



$$C_n = 2C_{AB}$$

$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln(d/r)}$$

F/m/phase

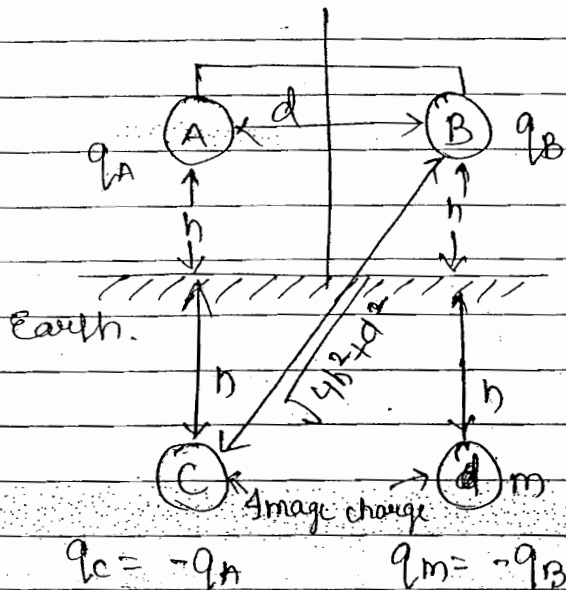
- Effect of Earth on capacitance b/w conductors

Earth consisting of ∞ No. of charge carrier of Both +ve and -ve. These charge carrier produces addition electrical field on the charges existing in the Tr-line conductor. Due to this capacitance b/w the conductors is increased which causes $\uparrow$ in charging current and Reactive power so that over voltage occurs in the system which causes insulation failure and some times, initiates corona. If the voltage of the system is higher than critical insulating disruptive voltage. To avoid this abnormality and reduce the capacitance, earth effect the height of tower is $\uparrow$ as the operating voltage is $\uparrow$.

KV	h (meters)
11	7
33	11
132	20
220	35
400	50
765	65

- Methods of Images :- For calculation of earth effect b/w the conductors of Tr-line method of images is used. It is a mathematical technique adopted from electromagnetic fields. In this method image charges are assumed below the ground which are opposite in sign and have equal magnitude with the charges existing on the conductors of Tr-line.

- No. of image Charges = No. of Conductors existing above the earth.



Voltage b/w AB :-

$$V_{AB} = \frac{1}{2\pi\epsilon_0\epsilon_r} \left[q_A \ln \frac{D_{AB}}{r} + \right.$$

$$\left. q_B \ln \frac{r}{D_{BA}} + q_C \ln \frac{D_{CB}}{D_{CA}} + \dots \right]$$

$$+ q_M \ln \frac{D_{MB}}{D_{MA}}$$

At Balance $q_A + q_B = 0$, $q_B = -q_A$, $q_C = -q_A$, $q_M = -q_B = q_A$

$$D_{AB} = D_{BA} = d, \quad D_{CA} = D_{MB} = 2h$$

$$D_{MA} = D_{CB} = \sqrt{4h^2 + d^2}$$

$$V_{AB} = \frac{q_A}{2\pi\epsilon_0\epsilon_r} \ln \left[\frac{2h \cdot d}{r \sqrt{4h^2 + d^2}} \right]^2$$

$$V_{AB} = \frac{q_A}{\pi\epsilon_0\epsilon_r} \ln \left(\frac{d}{r \sqrt{1 + \frac{d^2}{4h^2}}} \right)$$

$$C_{AB} = \frac{q_A}{V_{AB}} = \frac{\pi \epsilon_0 \epsilon_r}{\ln \left(\frac{d}{r \sqrt{1 + d^2/h^2}} \right)}$$

With Earth effect.

NOTE :- If height of tower (h) is $\uparrow$. $h \gg d$

$$\Rightarrow \frac{d^2}{4h^2} \approx 0$$

$$C_{AB} = \frac{\pi \epsilon_0 \epsilon_r}{\ln \left(\frac{d}{r} \right)}$$

Without Earth Effect.

• As $h \downarrow$, $\sqrt{1 + \frac{d^2}{h^2}} \downarrow$, $\ln \left(\frac{d}{r \sqrt{1 + d^2/h^2}} \right) \downarrow$, $C_{AB} \uparrow$.

• Generalised Equation:-

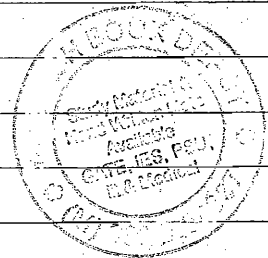
(1) 3 ϕ Transposed line :-

$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln \left[\frac{(D_1 D_2 D_3)^{1/3}}{r} \right]}$$

F/m/phase

(2) If $D_1 = D_2 = D_3 = D$

$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln (D/r)}$$



(3) Bundled Conductors:-

$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln \left(\frac{D_m}{D_s} \right)}$$

(4) Double ckt line :-

$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln \left(\frac{D_{MR1} D_{MR2} D_{MR3}}{D_{SR1} D_{SR2} D_{SR3}} \right)^{1/3}}$$

(5) Capacitance Reactance.

$$X_c = \frac{1}{2\pi f C_n} \quad \Omega/\text{m}/\text{phase}.$$

(6) Capacitance Susceptance.

$$B = \frac{1}{X_c} = 2\pi f C_n \quad \text{S}/\text{m}/\text{phase}$$

(7) Charging Current.

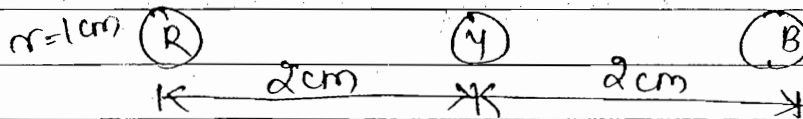
$$I_c = 2\pi f C_n V_{ph} \quad \text{A}/\text{m}/\text{phase}$$

(8) Reactive Power:-

$$Q_c = 2\pi f C_n V_{ph}^2 \quad \text{VARs}/\text{m}/\text{phase}$$

Q Find the capacitance / phase for the following configuration

(1) Horizontal

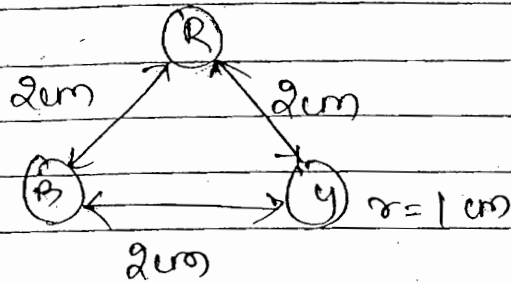


$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln \left(\frac{(2 \times 2 \times 4)^{1/3}}{1} \right)}$$

$$= \frac{2 \times 3.14 \times 8.854 \times 10^{-12} \times 1}{\ln \left(\frac{(2 \times 2 \times 4)^{1/3}}{1 \times 10^{-2}} \right)} = 10 \text{ pF}/\text{m}/\text{phase}$$

= CH

② Triangular :-



$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln\left(\frac{D}{r}\right)}$$

$$= \frac{2\pi \times 8.854 \times 10^{-12} \times 1}{\ln\left(\frac{2}{1 \times 10^{-2}}\right)}$$

$$= 10.5 \text{ pF/m/phase}$$

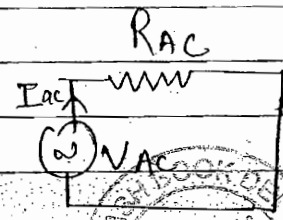
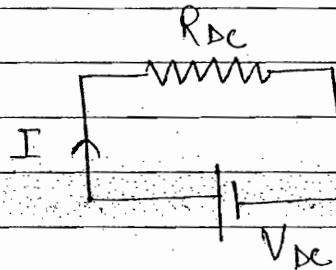
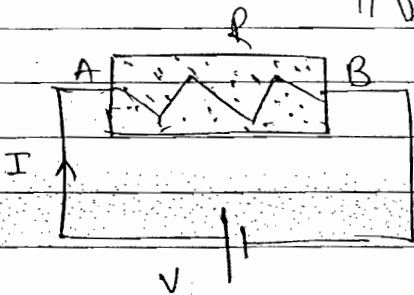
$$= C_\Delta$$

$$C_\Delta > C_H$$

$$L_\Delta < L_H$$

Prefer Δ one even C_n has disadv.

RESISTANCE :-

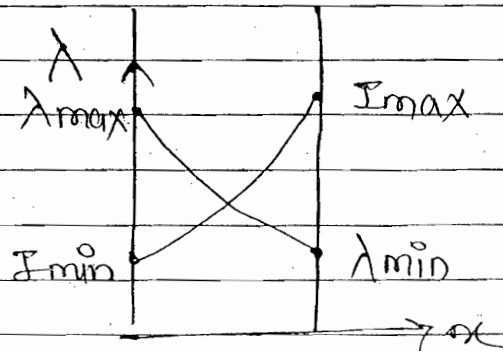
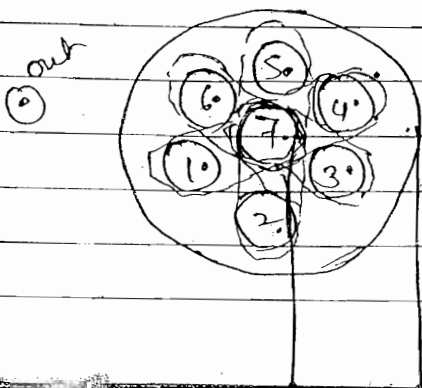


$$R_{AC} > R_{DC}$$

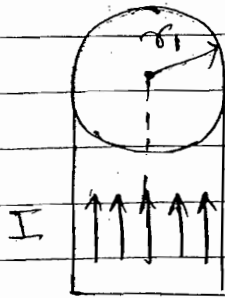
$$\approx 1.5 R_{DC}$$

- ① Skin effect
→ ② Proximity effect

① Skin Effect :-



HVDC



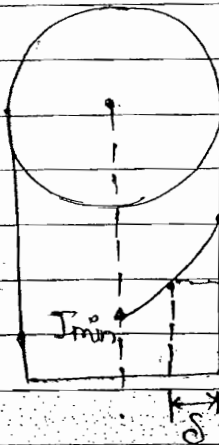
$$R_{DC} = \frac{\rho \cdot l}{\pi r_1^2}$$

HVAC



$$R_{AC} = \frac{\rho l}{\pi(r_1^2 - r_2^2)}$$

$$R_{AC} > R_{DC}$$

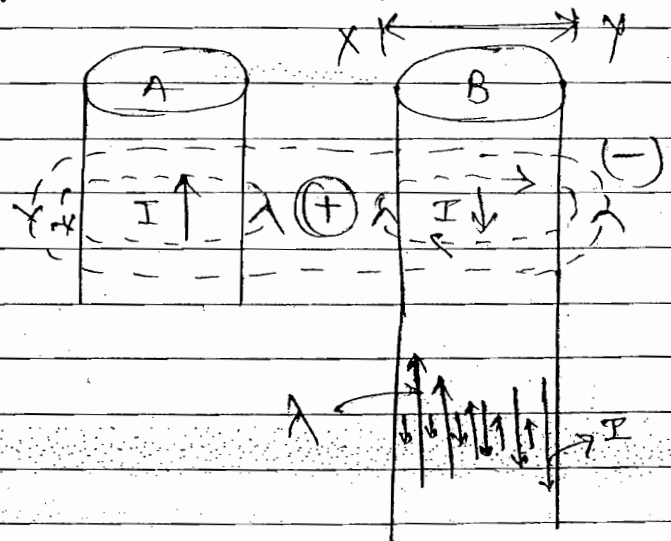
Skin depth:

$$J_{max} = 27.18 A$$

$$\frac{J_{max}}{e} = \frac{27.18}{2.718} = 10.4$$

$$\delta = \frac{1}{\sqrt{\pi f \mu_0 \mu_r \sigma}}$$

$$\text{Skin effect} \propto \frac{1}{\delta}$$

Proximity Effect:

B/w $\rightarrow$ flux in same dir $\rightarrow +$
 Surf $\rightarrow$ flux in opp dir $\rightarrow -$

- Accumulation of current on the surface of conductor is called skin effect.

- Due to skin effect effective area of current flowing path is $\downarrow$ which causes $R_{AC} > R_{DC}$.

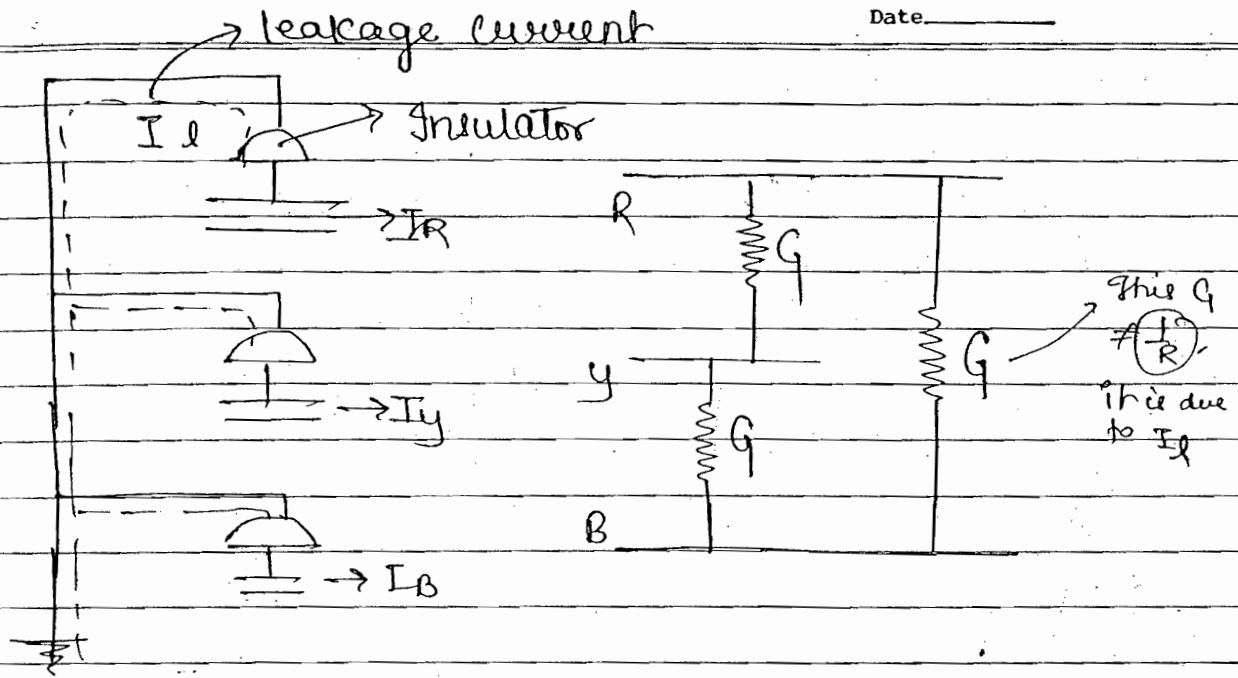
- Skin Depth :- The depth of the conductor at which the surface current is reduced to $\frac{1}{e}$ times the surface value. As the skin depth is $\uparrow$ skin effect is $\downarrow$. In case of communication lines frequency is very high so that skin depth is small skin effect is larger.
- Skin effect depends on
 - (1) frequency
 - (2) Conductivity
 - (3) μ_r
 - (4) Size of the conductor

- Proximity Effect :- It is occur due to current flowing in the adjacent conductor produces Non-uniform flux linkage so that non-uniform current flows and the effective area of current flowing path is reduced which causes $R_{ac} > R_{dc}$.

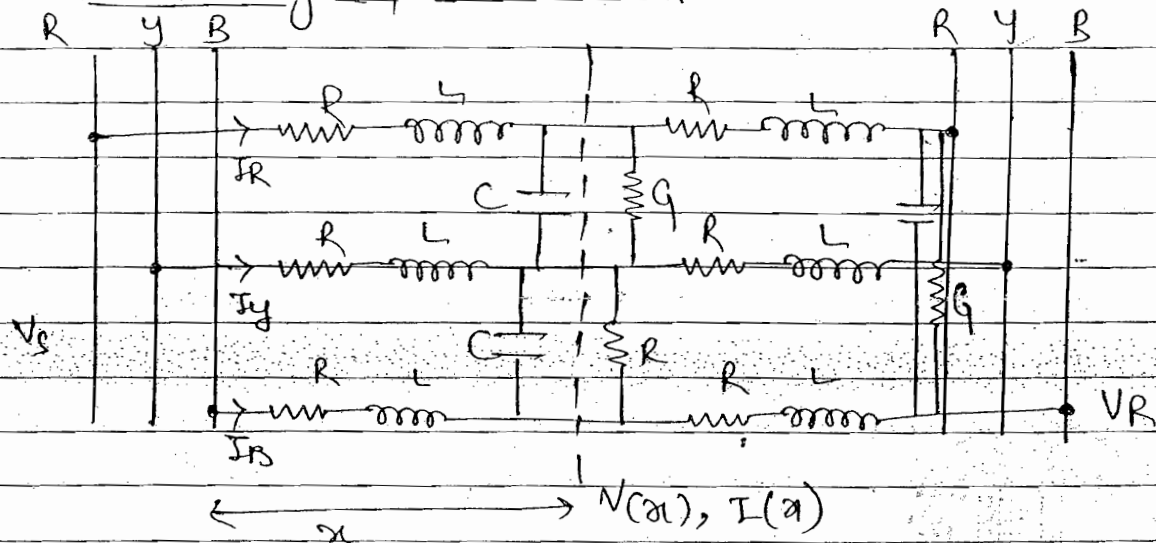
- Proximity effect depends on:-
 - (1) frequency
 - (2) σ
 - (3) μ_r
 - (4) Distance b/w the conductors

- Proximity effect is more if the distance is small b/w the conductor ex:- power cables. In overhead lines distance b/w the conductors is larger so that proximity effect is negligible.

- (4) Conductance :- The leakage current flowing b/w conductor and the insulation is represented with electrical equivalence of conductor parameter G . Its value is neglected in case of short and medium lines and it is considered in case of long lines.

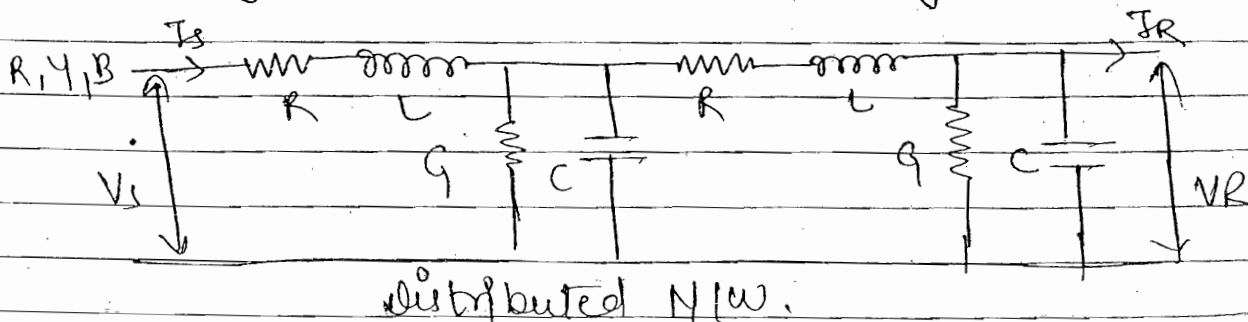


• Modelling Of Tr-line:-



Assumption:-

- ① System is balanced ($|I_R| = |I_y| = |I_B|$)



distributed N/w.

(2) Lumped Nlw:-

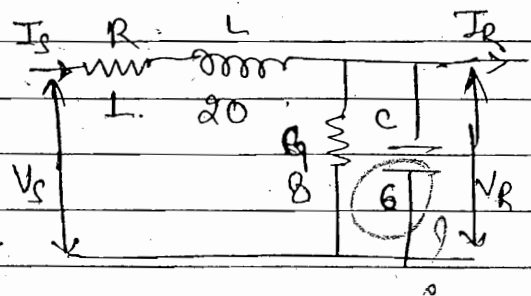
$$l = 100 \text{ km}$$

$$R = 0.01 \times 100 = 1 \Omega$$

$$L = 0.2 \times 100 = 20 \text{ mH}$$

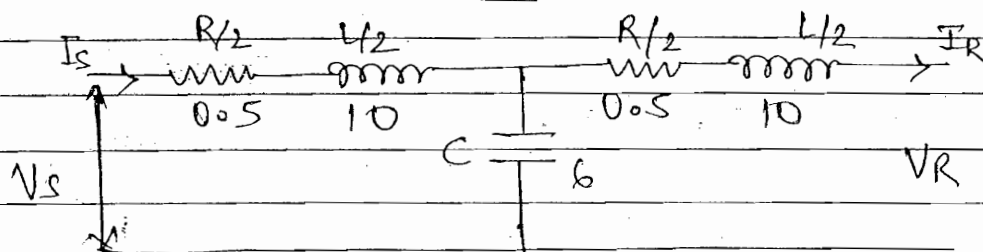
$$C = 0.04 \times 100 = 4 \text{ mF}$$

$$G = 0.08 \times 100 = 8 \text{ nS}$$

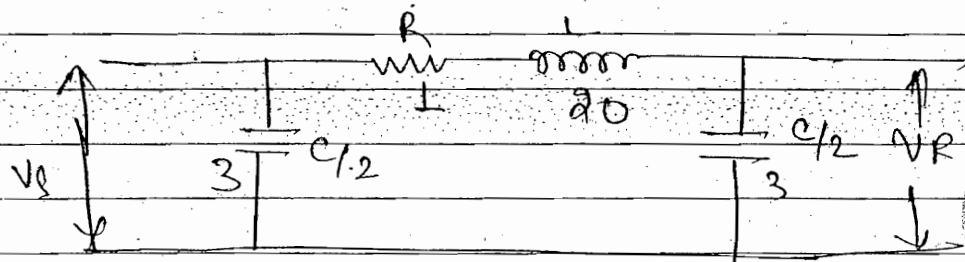


(3) Medium line:- [G is neglected]

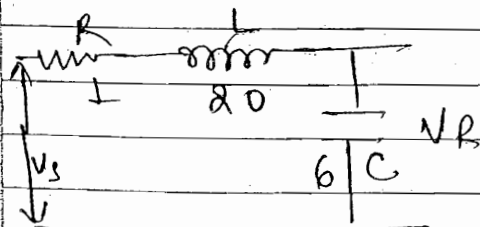
(a) Nominal T Nlw:-



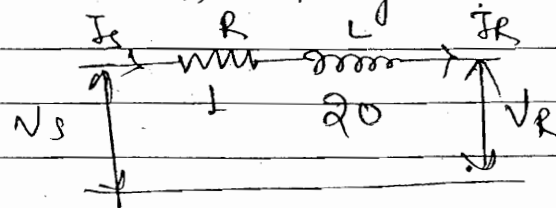
(b) Nominal π Nlw:-



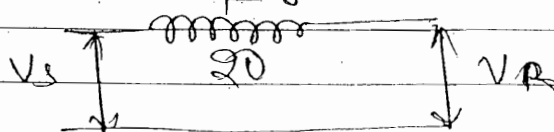
(c) End Condense:-



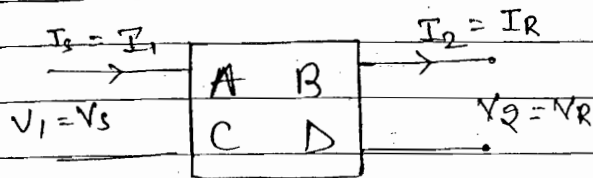
(d) Short line
(G, C neglected)



(5) Fault analysis Eq. (kth) ($R \ll X_L$)



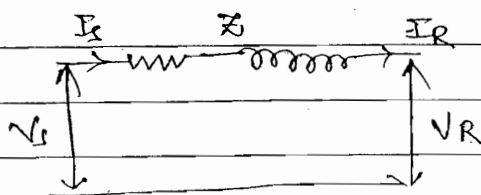
ABCD or T₂ LINE PARAMETERS



$$\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_2 \\ I_2 \end{bmatrix}$$

• $A = D \Rightarrow$ Symmetrical w, $AD - BC = 1 \Rightarrow$ Reciprocal

(1) Z Network :- (Short Tr line)



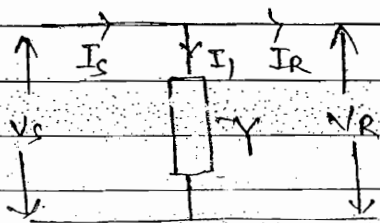
$$V_S = V_R + I_R \cdot Z$$

$$V_S = 1 \cdot V_R + Z \cdot I_R$$

$$I_S = I_R = (0) V_R + 1 \cdot I_R$$

$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

(2) Y Network :-

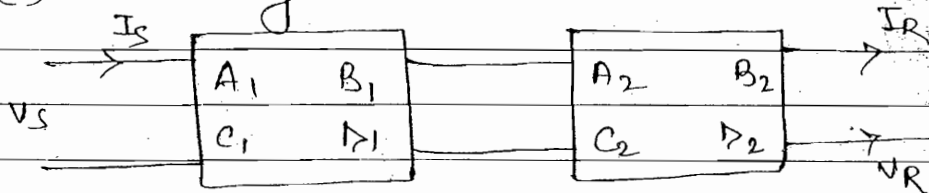


$$V_S = V_R = 1 \cdot V_R + (0) I_R$$

$$I_S = I_1 + I_R = Y V_R + 1 \cdot I_R$$

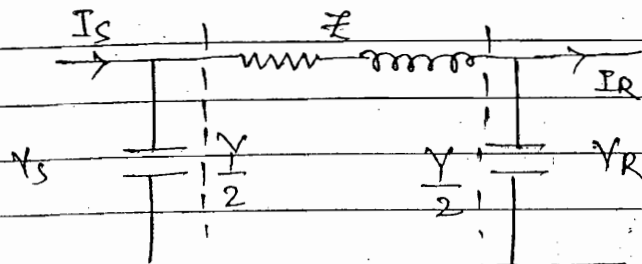
$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ Y & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

(3) Cascading N/w :-



$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} A_1 & B_1 \\ C_1 & D_1 \end{bmatrix} \begin{bmatrix} A_2 & B_2 \\ C_2 & D_2 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

• Reciprocal :- By reversing - value will remain same.
ex:- V_S, V_R are reversed, values remain same.

(4) Nominal π N/w:-

where

$$Z = R + j\omega L$$

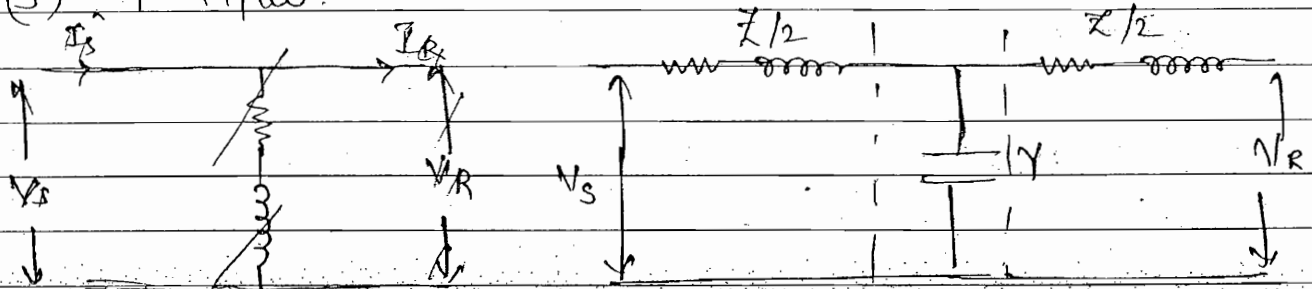
$$Y = j\omega C$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ Y/2 & 1 \end{bmatrix} \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ Y/2 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \left(1 + \frac{YZ}{2}\right) & Z \\ Y\left(1 + \frac{YZ}{4}\right) & \left(1 + \frac{YZ}{2}\right) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

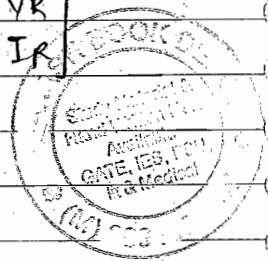
Nominal

(5) T N/w:-

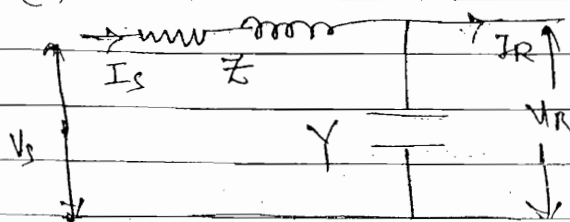


$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & Z/2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ Y & 1 \end{bmatrix} \begin{bmatrix} 1 & Z/2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \left(1 + \frac{YZ}{2}\right) & Z\left(1 + \frac{YZ}{4}\right) \\ Y & \left(1 + \frac{YZ}{2}\right) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$



(6) End Condenser N/w:-



$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ Y & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} (1+YZ) & Z \\ Y & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad A \neq D$$

unsymmetrical.

• Transmission Line Performance Parameter:-

(1) Transmission η :-

$$\begin{aligned} \% \eta &= \frac{P_R \times 100}{P_s} = \left| \frac{V_R I_R}{V_s I_s} \right| \frac{\cos \phi_R \times 100}{\cos \phi_s} \\ &= \frac{P_R}{P_R + P_L} \times 100 \end{aligned}$$

$$P_L = \text{Tr line loss} = P_s - P_R$$

↳ Ideal: $\eta = 100\%$

↳ practical $\eta \geq 90\%$

• Calculation of I_R if V_R , P_R are given:-

$$|I_R| = \frac{P_R}{V_R \cos \phi_R}$$

V_R = phase voltage

P_R = 1- ϕ power

$$|I_R| = \frac{P_R}{\sqrt{3} V_R \cos \phi_R}$$

$V_R = V_L$ = line voltage

P_R = 3- ϕ power

(2) Voltage Regulation:-

$$\% V_{REG} = \frac{|V_{RNL}| - |V_{RFL}|}{|V_{RFL}|} \times 100$$

V_{RNL} = No load Receiving End Voltage

$$V_s = A V_R + B I_R$$

At NO load $I_R = 0 \Rightarrow V_s = A V_{RNL}$

$$|V_{RNL}| = \left| \frac{V_s}{A} \right|$$

V_{RFL} = Full load or Rated Receiving End Voltage
= $|V_R|$

$$\% V_{REG} = \frac{\left| \frac{V_s}{A} - V_R \right|}{|V_R|} \times 100$$

for short line
A=1

valid for short / Medium / long lines

↳ Ideal V_{REG} : 0% , ↳ Practical $V_{REG} = \pm 5\%$

• Classification of Transmission line:-

- (1) Short Tr. line $\rightarrow l < 80 \text{ km}, lf < 4000$
- (2) Medium Tr. line $\rightarrow 80 \leq l \leq 200 \text{ km}, 4000 \leq lf \leq 10,000$
- (3) Long Tr. line $\rightarrow l > 200 \text{ km}, lf > 10,000$

ex:- $l = 80 \text{ km} ; f = 50 \text{ Hz}$
 $lf = 80 \times 50 = 4000$

- Communication lines are operation in MHz range so that they are considered long line equivalent ckt

- All the parameters R, L, C, G are distributed ~~through out~~ the length of line

Q A Tr line has a length of 10 km is excited by

- (i) 50 Hz (ii) 500 Hz (iii) 5 KHz.

Find the type of Tr line.

Solution

$l = 10 \text{ km}$

(i) $f = 50 \text{ Hz}$
 $lf = 10 \times 50$
 $= 500$

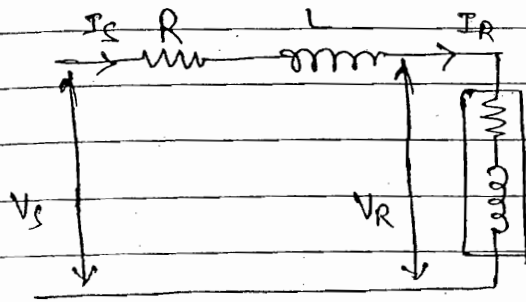
Short

(ii) $f = 500$
 $lf = 10 \times 500$
 $= 5000$

Medium

(iii) $f = 5 \times 10^3$
 $lf = 10 \times 5 \times 10^3$
 $= 5 \times 10^4$

Long

(1) Short Tr-line:-

$$(Z) = (R + j\omega L)$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\text{(1) \% VEG} = \frac{\left| \frac{V_s}{A} \right| - |V_R|}{|V_R|} \times 100$$

For short line $A = 1$

$$\text{\% VEG} = \frac{|V_s| - |V_R|}{|V_R|} \times 100$$

$$\text{(2) \% } \eta = \frac{P_R}{P_R + P_L} \times 100$$

$$\bullet \frac{1 - \phi}{P_L = R \cdot I_R^2}$$

$$\bullet \frac{3 - \phi}{P_L = 3 R I_R^2}$$

Pg NO. → 45

Conventional 2

$l = 40 \text{ km}$

$220 \text{ kV}, 3\phi$

$R = 0.15 \Omega/\text{km}$

$\rho = 5042$

$lf = 40 \times 50$

$L = 1.5923 \text{ mH/km}$

$= 2000 \text{ short}$

$S_R = 381 \text{ MVA}$

$\cos \phi_R = 0.8$

(1) Convert into lumped Nwo.

default = lagging

$$R = 0.15 \times 40 = 60 \Omega$$

$$L = (2\pi f L) \cdot l = 2\pi \times 50 \times 1.5923 \times 10^{-3} \times 40$$

$$= 20 \Omega$$

$$Z = 60 + j20 = 20 \angle 73.3^\circ \Omega$$

For short line $B = Z = 60 + j20$

$$A = D = 1$$

$$I_R = \frac{P_R}{\sqrt{3} V_R \cos \phi_R} = \frac{B S_R \cos \phi_R}{\sqrt{3} V_R \cos \phi_R}$$

$$= \frac{381 \times 10^6 \times 0.8}{\sqrt{3} \times 220 \times 0.8 \times 10^3}$$

$$|I_R| = 1000 \text{ A}$$

$$\cos \phi_R = 0.8 \text{ lag}, \phi_R = 36.86^\circ$$

$$I_R = 1000 \angle -36.86^\circ \text{ A} = I_S$$

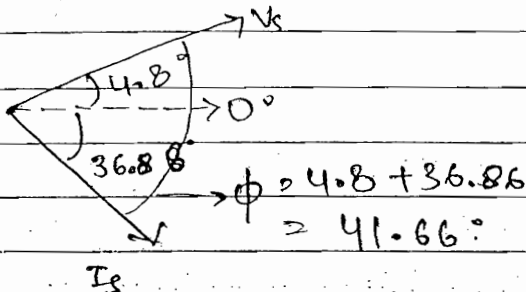
Remember
here

$$\begin{aligned} \text{(1) (a)} \quad V_S &= A V_R + B I_R \\ &= 1 \times 220 \times 10^3 + 20.8 \angle 73.3^\circ \times 1000 \angle -36.86^\circ \\ &= 144.8 \angle 4.8^\circ \text{ kV} \text{ phase.} \end{aligned}$$

$$\begin{aligned} V_{SL} &= \sqrt{3} \times 144.8 \angle 4.8^\circ \\ &= 250 \angle 4.8^\circ \text{ kV} \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad P_S &= \sqrt{3} |V_S I_S| \cos \phi \\ V_S &= 250 \angle 4.8^\circ \text{ kV.} \end{aligned}$$

$$\left. \begin{aligned} I_S &= I_R = 1000 \angle -36.86^\circ \text{ A} \end{aligned} \right\}$$



$$\begin{aligned} P_S &= \sqrt{3} \times 250 \times 10^3 \times 1000 \\ &\quad \times \cos (36.86^\circ + 4.8^\circ) \end{aligned}$$

$$P_S = 323 \text{ MW}$$

$$\begin{aligned} \text{(2) (a)} \quad \% \text{ VREG} &= \frac{|V_S| - |V_R|}{|V_R|} \times 100 \\ &= \frac{250 - 220}{220} \times 100 \\ &= \frac{30}{22} \times 100 \end{aligned}$$

$$V_{REG} \% = 13.67 \%$$

$$\text{(b) } \eta \% = \frac{P_R}{P_S} \times 100 = \frac{381 \times 0.8}{323} \times 100$$

$$\% \eta = 94\%$$

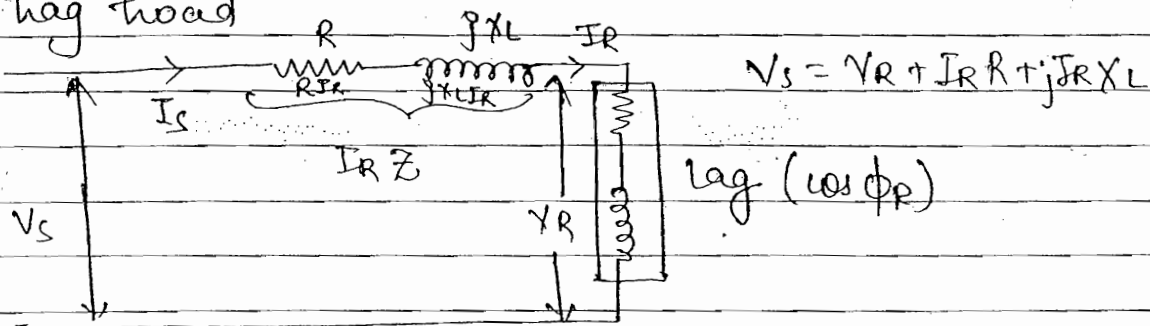
$$\text{(OR)} \quad P_L = 3 R I_R^2 = 3 \times 6 \times (1000)^2 = 18 \text{ MW}$$

$$\% \eta = \frac{P_R}{P_R + P_L} \times 100 = \frac{381 \times 0.8}{381 \times 0.8 + 18} \times 100 \approx 94\%$$

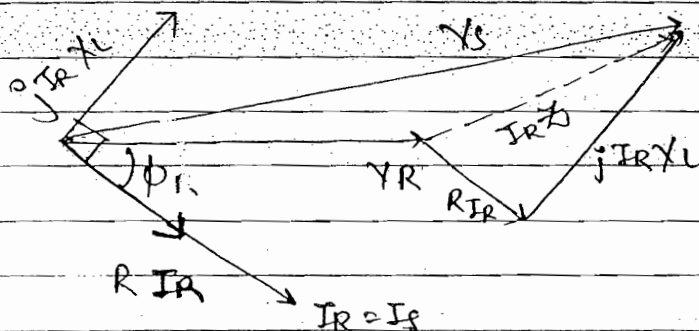
2.18

• Phasor Diagram:-

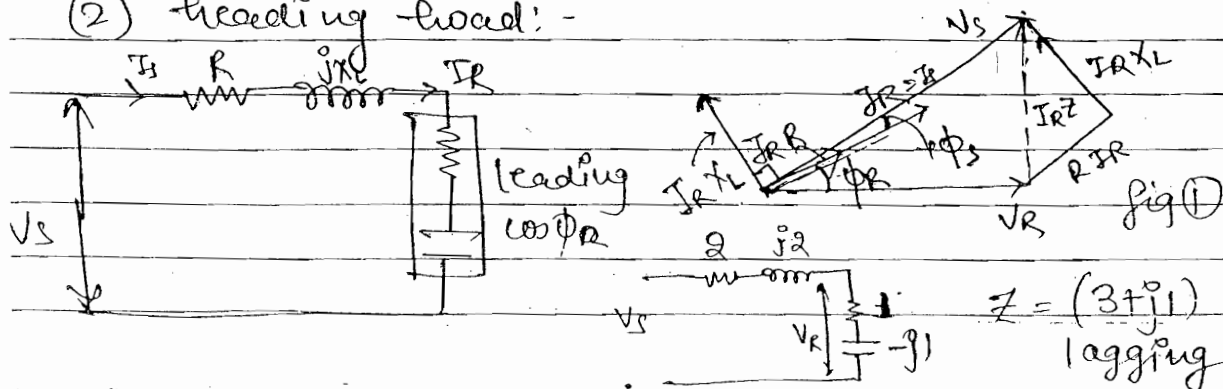
(1) lag load



• Start from Receiving end, add all drop, final reach to sending end



(2) leading load:-



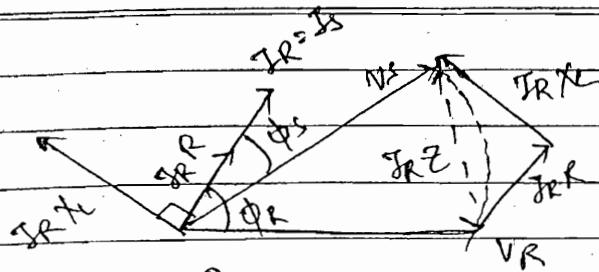
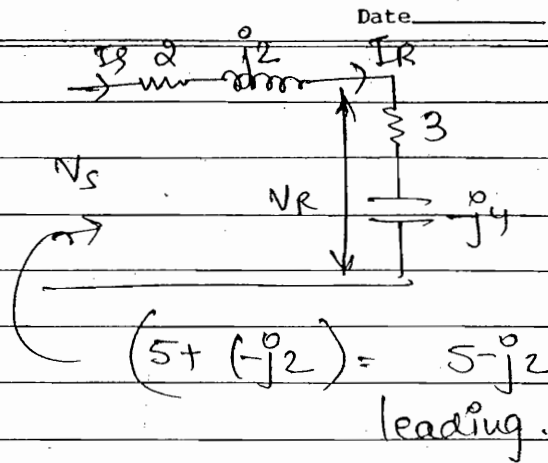
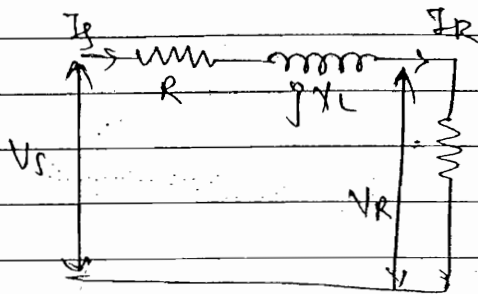


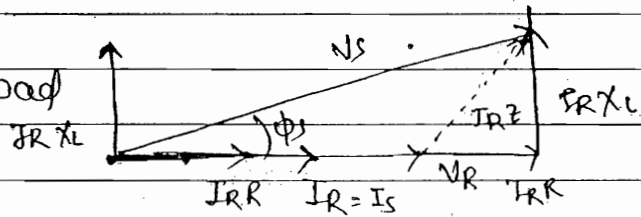
fig 2



- (3) UPF load.



UPF load



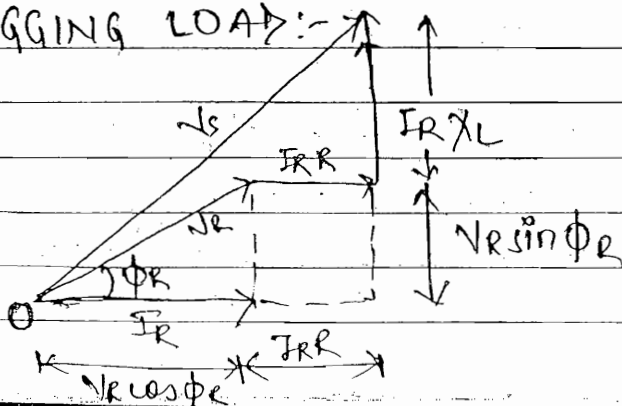
- In lagging load:- $\phi_s > \phi_R$. B/w More lagging load.
 $V_s > V_R$
 $+ve V_{REG}$ $V_{REG} \neq 0$

- UPF load:- $V_s > V_R$ $V_{REG} \neq 0$

- leading load:- possibility of $V_{REG} \approx 0$
 $V_s \approx V_R$

- Effect of load Power factor ON Voltage Regulation

- (1) LAGGING LOAD:-



$$V_s^2 = (V_R \cos \phi_R + I_R R)^2 + (V_R \sin \phi_R + I_R X_L)^2$$

$$= V_R^2 + I_R^2 (R^2 + X_L^2) + 2 V_R I_R (R \cos \phi_R + X_L \sin \phi_R)$$

Assume $I_R^2 (R^2 + X_L^2) \ll V_R^2$ (1)

$$V_s = \left[V_R^2 + 2 V_R I_R (R \cos \phi_R + X_L \sin \phi_R) \right]^{1/2}$$

$$= V_R \left[1 + \frac{2 I_R}{V_R} (R \cos \phi_R + X_L \sin \phi_R) \right]^{1/2}$$

use $(1+x)^{1/2} \approx 1 + \frac{x}{2}$

$$V_s = V_R \left[1 + \frac{2 I_R}{2 V_R} (R \cos \phi_R + X_L \sin \phi_R) \right]$$

$$V_s - V_R = I_R [R \cos \phi_R + X_L \sin \phi_R]$$

$$\% V_{REG} = \frac{V_s - V_R}{V_R} \times 100$$

$$\boxed{\% V_{REG} = \frac{I_R (R \cos \phi_R + X_L \sin \phi_R)}{V_R} \times 100}$$

Condition for Max. V_{REG} :-

$$\frac{d}{d\phi_R} [R \cos \phi_R + X_L \sin \phi_R] = 0$$

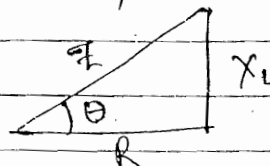
$$-R \sin \phi_R + X_L \cos \phi_R = 0$$

$$\boxed{\phi_R = \tan^{-1} \left(\frac{X_L}{R} \right)} \quad \text{condition for Max } V_{REG}$$

$R, X_L \rightarrow$ Tr line parameter, $\phi_R =$ load p.f. angle

$$\text{If } Z = (R + j X_L) = \text{Tr. line impedance.}$$

$$\theta = \tan^{-1} \left(\frac{X_L}{R} \right)$$

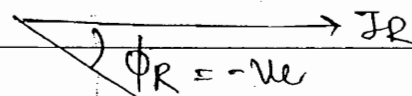


$$\theta = \phi_R = \tan^{-1} \left(\frac{X_L}{R} \right)$$

• p.f. of lag load for Max. V_{REG} .

$$\cos \phi_R = \cos \theta = \frac{R}{Z}$$

(2) lead load.



$$\% V_{REG} = \frac{I_R (R \cos(\phi_R) + X_L \sin(\phi_R))}{V_R} \times 100$$

$$\% V_{REG} = \frac{I_R (R \cos \phi_R - X_L \sin \phi_R)}{V_R} \times 100$$

Condition for $V_{REG} = 0\%$

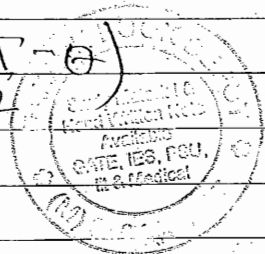
$$R \cos \phi_R - X_L \sin \phi_R = 0$$

$$\phi_R = \tan^{-1} \frac{R}{X_L}$$

If $\theta = \tan^{-1} \left(\frac{X_L}{R} \right)$ Then $\left(\phi_R = \frac{\pi}{2} - \theta \right)$

p.f. of lead load for $V_{REG} = 0\%$

$$\cos \phi_R = \sin \theta = \frac{X_L}{Z}$$



$$(3) \frac{V_{REG}(\text{lead})}{V_{REG}(\text{lag})} = \frac{R \cos \phi_R - X_L \sin \phi_R}{R \cos \phi_R + X_L \sin \phi_R}$$

↑ head
↓ lag

(4) Cal. of I_R , P_R if $V_{REG} = 0\%$ or $|V_S| = |V_R|$ gives from (1)

$$V_S^2 = V_R^2 + I_R^2 (R^2 + X_L^2) + 2 V_R I_R [R \cos \phi_R + X_L \sin \phi_R]$$

$$\text{If } |V_R| = |V_S|$$

$$|I_R| = \frac{2 V_R (R \cos \phi_R + X_L \sin \phi_R)}{(R^2 + X_L^2)}$$

lag load

$$|I_R| = \frac{2 V_R (R \cos \phi_R - X_L \sin \phi_R)}{(R^2 + X_L^2)}$$

lead load

where V_R , R , $X_L \Rightarrow$ phase values

$$P_R = \sqrt{3} V_R I_R \cos \phi_R$$

where $V_R = V_L =$ line voltage

Q A π -line has an impedance of $3+j4 \Omega$ /phase p.f. of load required for maintaining maximum and zero voltage regulation or 0 respectively

(a) 0.3 lead, 0.6 lag.

(b) 0.6 lag, 0.8 lead

(c) 0.6 lead, 0.3 lag

(d) 0.3 lag, 0.8 lead

$$\text{Max: } \frac{3}{5} = 0.6 \text{ lag.}$$

$$\text{Zero: } \frac{4}{5} = 0.8 \text{ lead}$$

Q Tr-line impedance = 10 the load p.f. angle required for zero maximum voltage regulation is respectively.

Sol p.f. = zero. $\lambda - \theta = \theta$

Q Tr-line is an impedance of $2 + j8$ is connected with 0.8 lagging load produces 10% of voltage regulation find the voltage regulation for a leading load of 0.707.

Sol $Z = 2 + j8$ 0.8 lagging 10% VR.
leading =

$$\frac{V_{REG \text{ lead}}}{V_{REG \text{ lag}}} = \frac{2 \times 0.707 - 8 \times 0.707}{2 \times 0.8 + 8 \times 0.6}$$

$$\% = -5\%$$

Q A 3 ϕ Tr-line having $Z = 3 + j4$ connected with 0.8 lagging load and operating $V_s = V_R = 11 \text{ kV}$ find the active power drawn by load

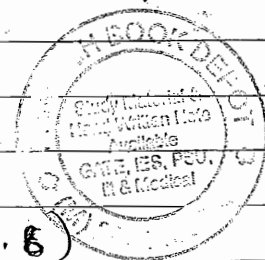
Sol $P = \frac{3 V_R I_R (R \cos \phi_R + X_L \sin \phi_R)}{X_L^2 + R^2}$

$$= \frac{2 \times 11 \times (3 \cos 0.8 + 4 \sin 0.8)}{(4^2 + 3^2)}$$

$$= 2.68$$

$$P_R = \sqrt{3} V_R I_R \cos \phi$$

$$= \sqrt{3} \times 2.68 \times 11 \times \cos 0.8$$

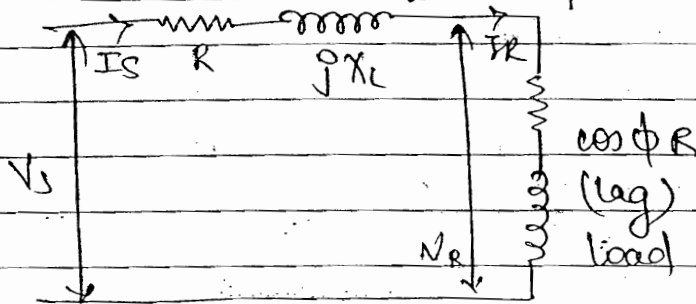


$$I_R = \frac{2 \times 11 \sqrt{3} \times 10^3 (3 \times 0.8 + 4 \times 0.6)}{(3^2 + 4^2)} = 2.4 \text{ kA}$$

$$P_R = \sqrt{3} V_R I_R \cos \phi_R$$

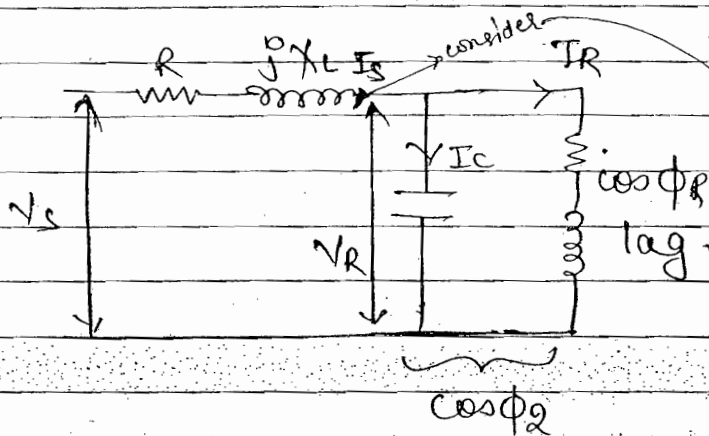
$$= \sqrt{3} \times 11 \times 10^3 \times 2.4 \times 10^3 \times 0.8 = 37.1 \text{ MW}$$

• Calculation of Compensator (Capacitor) for Reducing V_R :



$$\Rightarrow V_s - V_R = \text{Voltage drop}$$

$$= I_R (R \cos \phi_R + X_L \sin \phi_R)$$



$$\vec{V}_s - \vec{V}_R =$$

$$\Rightarrow I_s^2 (R \cos^2 \phi_2 + X_L \sin^2 \phi_2)$$

$$= \frac{P_R}{V_R \cos \phi_2} (R \cos \phi_2 + X_L \sin \phi_2)$$

$$V_s - V_R = \frac{R P_R}{V_R} + \frac{P_R X_L}{V_R} \tan \phi_2$$

$$\tan \phi_2 = \frac{|V_s V_R| - |V_R^2| - |R P_R|}{|P_R X_L|}$$

$$\phi_2 = \tan^{-1} \left(\frac{|V_s V_R| - |V_R^2| - |R P_R|}{|P_R X_L|} \right)$$

$$|I_s| = \frac{P_R}{V_R \cos \phi_2}$$

$$I_s \angle \phi_2 = I_R \angle -\phi_R + j I_c$$

$$I_c = I_s \angle \phi_2 - I_R \angle -\phi_R$$

check wheather
 I_c angle coming
 90° or not
 as it pure capact

$$2\pi f C V_R = I_c$$

$$C = \frac{I_c}{2\pi f V_R}$$

Q 1- ϕ Tr-line has an $Z = 3 + j4 \Omega$ operating at $V_R = 10kV$ connected with load of $10MW$ 0.8 lagging. Calculate

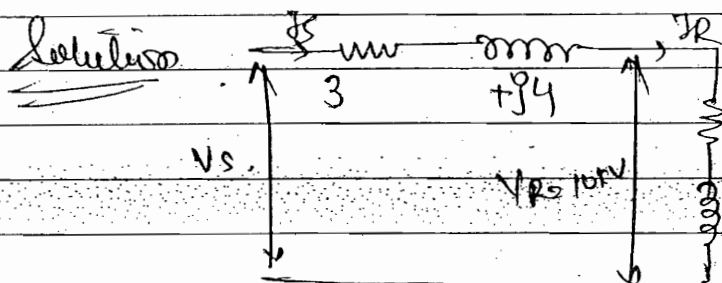
(1) Voltage Regulation

(2) How much capa. compensator required for reducing voltage regulatⁿ.

(a) 50%

(b) 25%

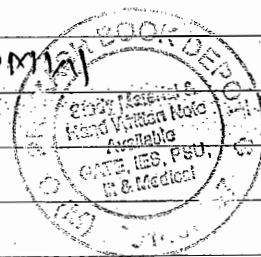
Assume $V_R = \text{const}$



0.8 lag. 10MW

$$I_R = \frac{P_R}{V_R \cos \phi_R} = \frac{10 \times 10^6}{10 \times 10^3 \times 0.8} = 1250 A$$

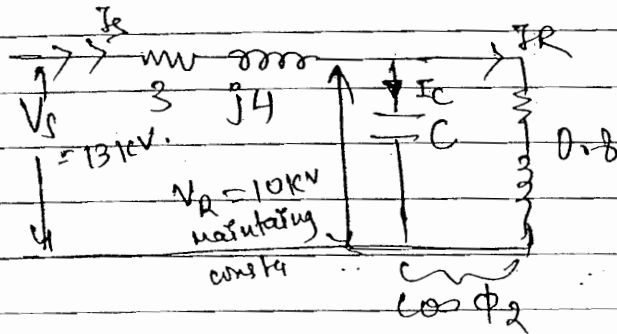
$$\begin{aligned} \%V_{REG} &= \frac{I_R (R \cos \phi_R + X_L \sin \phi_R)}{V_R} \times 100 \\ &= \frac{1250 (3 \times 0.8 + 4 \times 0.6)}{10 \times 10^3} \times 100 \\ &= 60 \% \end{aligned}$$



$$\Rightarrow \frac{V_s - V_R}{V_R} = 60\% = 0.6$$

$$\Rightarrow V_s = (0.6 \times 10 \times 10^3) + (10 \times 10^3) \\ = 16 \text{ kV}$$

(2) with compensator:-



(9) V_{REG} reduce of 50% of 60%

$$\frac{V_s - V_R}{V_R} \times 100 = \frac{0.6}{2} = 0.3$$

$$\frac{V_s - 10}{10} = 0.3$$

$$V_s = 13 \text{ kV}$$

$$\phi_2 = \tan^{-1} \left(\frac{|V_s| |V_R| - |V_R|^2 / (R R_L)}{|R_L \times L|} \right)$$

$$= \tan^{-1} \left(\frac{|13 \times 10| - [(10)^2] \times - (3 \times 10)}{10 \times 4} \right)$$

$$= 0^\circ$$

$$I_s = \frac{P_R}{V_R \cos \phi_2} = \frac{10 \times 10^6}{10 \times 10^3 \times 1} \Rightarrow 1000 \text{ A}$$

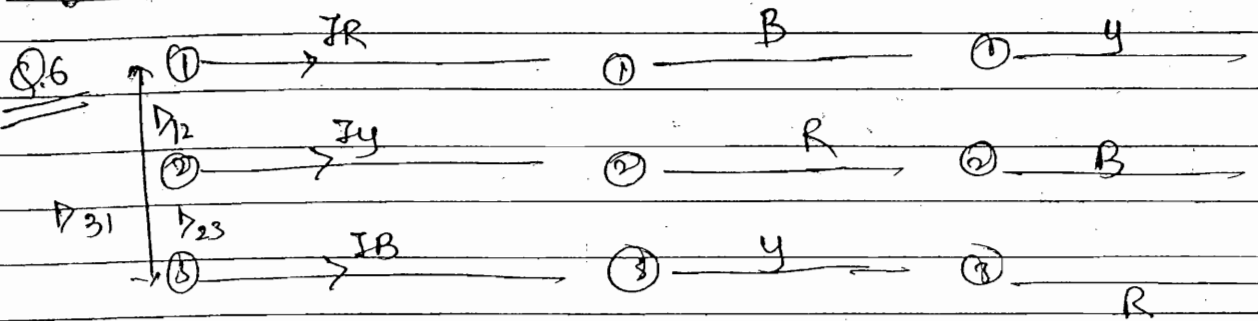
$$I_C = I_s \angle \phi_2 - I_R \angle -\phi_R$$

$$= 1000 \angle 0^\circ - 1250 \angle -36.86^\circ$$

$$= 750 \angle 90^\circ \text{ Amp.}$$

$$C = \frac{I_C}{2\pi f \times V_R} = \frac{750}{2\pi \times 50 \times 10 \times 10^3}$$

$$= 238 \mu\text{F}$$



$$\lambda_1 = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r_1} + I_Y \ln \frac{1}{D_{12}} + I_B \ln \frac{1}{D_{13}} \right]$$

$$\lambda_2 = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r_1} + I_Y \ln \frac{1}{D_{23}} + I_B \ln \frac{1}{D_{12}} \right]$$

$$\lambda_3 = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r_1} + I_Y \ln \frac{1}{D_{13}} + I_B \ln \frac{1}{D_{23}} \right]$$

$$I_Y = I_R \angle -120^\circ = -0.5 - j0.866 I_R$$

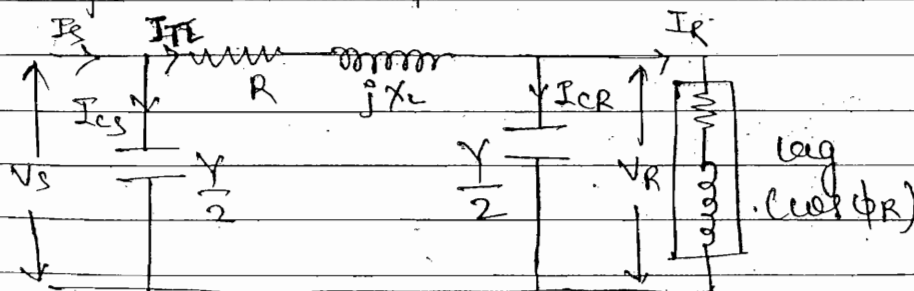
$$I_B = I_R \angle -240^\circ = -0.5 + j0.866 I_R$$

Take these avg. value. Real terms will cancel out only R will left.

11/7/2011

(2) Medium Tr-line:

(1) Nominal π Model:



$$Z = R + j\omega L$$

$$Y = j\omega C$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 + \frac{YZ}{2} & Z \\ Y(1 + \frac{YZ}{4}) & (1 + \frac{YZ}{2}) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$(1) \% V_{REG} = \frac{\left| \frac{V_S}{A} \right| - |V_R|}{|V_R|} \times 100$$

where $A = \left(1 + \frac{YZ}{2} \right)$

$$(2) \% \eta = \frac{P_R}{P_R + P_L} \times 100$$

where $P_L = R I_{TL}^2$ for 1- ϕ , $= 3 R I_{TL}^2$ for 3- ϕ
 $I_{TL} = I_R + I_{CR}$
 $= I_R + \frac{Y}{2} V_R$

Steps:

(1) V_R as Ref

(2) I_R lags V_R by ϕ_R

(3) $I_{CR} = V_R Y/2$

(4) $I_{TL} = I_R + I_{CR}$

I_{CR} leads V_R by 90°

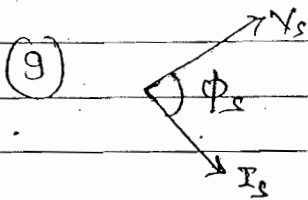
(5) $I_{TL} Z = R I_{TL} + j I_{TL} X_L$

(6) $V_S = V_R + I_{TL} Z$

(7) $I_{CS} = \frac{V_S Y}{2}$

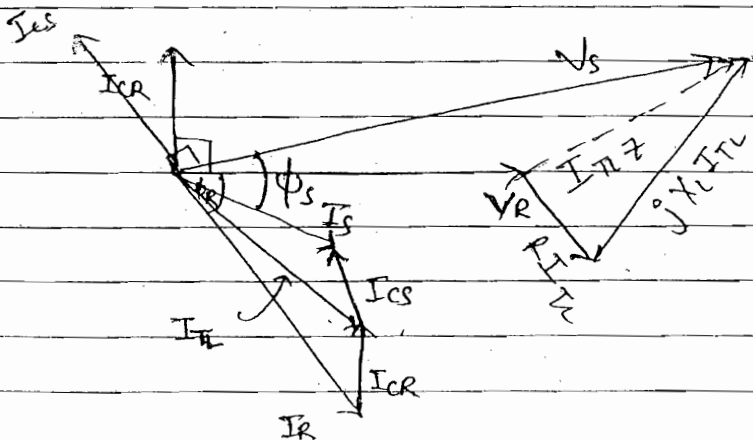
(8) $I_S = I_{CS} + I_{TL}$

I_{CS} leads V_S by 90°

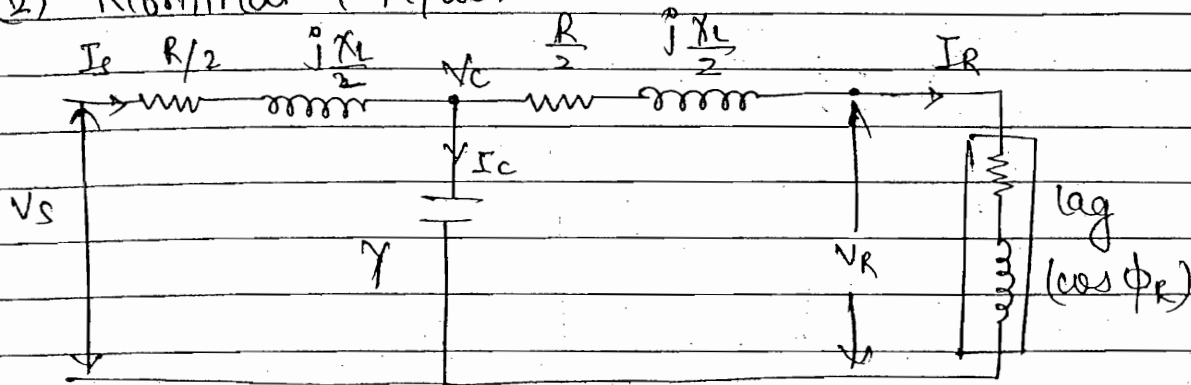


If the load current I_R and voltage is V_R lags by ϕ_R

PHASOR DIAGRAM



(2) Nominal T N/w:-



$$Z = R + jX_L \quad Y = j\omega C$$

Steps (1) V_R as Ref.(2) I_R lags V_R by ϕ_R

(3) $I_R Z = I_R \cdot \frac{R}{2} + j I_R \frac{X_L}{2}$

(4) $V_c = V_R + I_R \frac{Z}{2}$

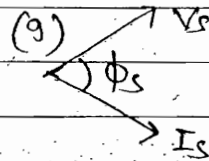
(5) $I_c = V_c Y$

(6) $I_s = I_c + I_R$

 I_c leads V_c by 90°

(7) $I_s Z = I_s \frac{R}{2} + j I_s \frac{X_L}{2}$

(8) $V_s = V_c + I_s \frac{Z}{2}$



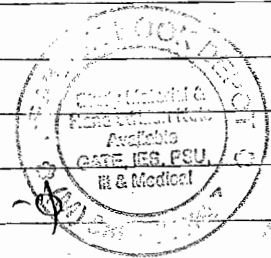
$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} (1 + Y \frac{Z}{2}) & Z(1 + Y \frac{Z}{4}) \\ Y & (1 + Y \frac{Z}{2}) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

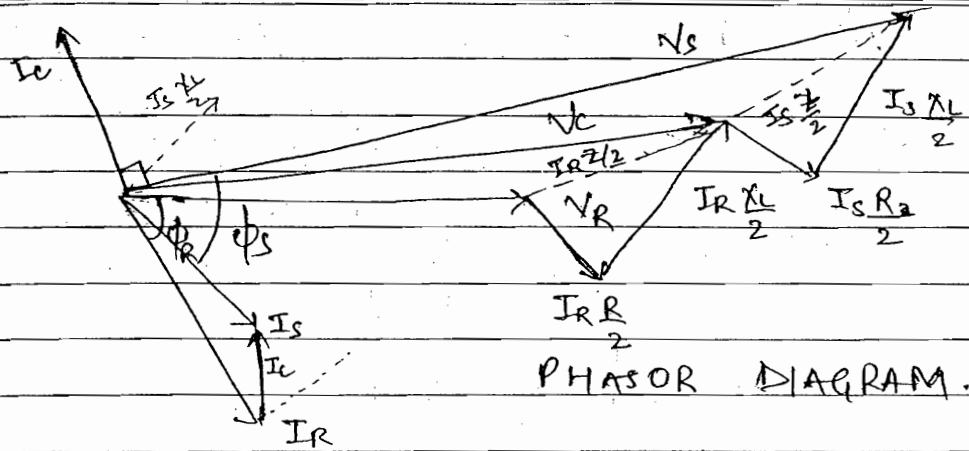
$$(1) \% V_{REG} = \frac{|V_s|}{|A|} - |V_R| \times 100 \quad \text{where } A = 1 + Y \frac{Z}{2}$$

$$(2) \% \eta = \frac{P_R}{P_R + P_L} \times 100$$

$$\text{where } P_L = \frac{R}{2} (I_R^2 + I_s^2) \quad \text{for 1-}\phi$$

$$= \frac{3R}{2} (I_R^2 + I_s^2) \quad \text{for 3-}\phi$$





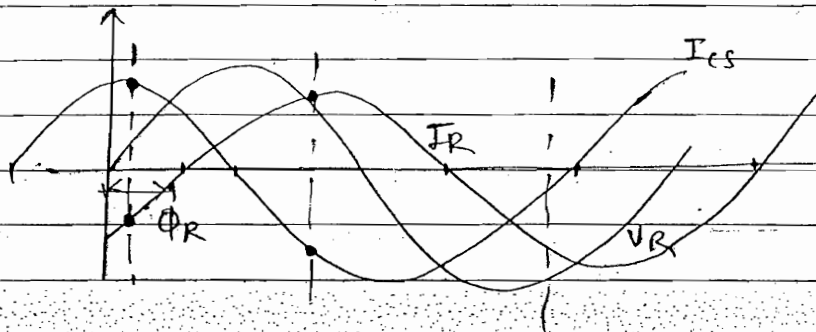
$$I_s = I_R + I_c = |I_R| \angle -\phi_R + |I_c| \angle 90^\circ$$

$$= I_R \cos \phi_R - j I_R \sin \phi_R + j I_c$$

$$I_s = I_R \cos \phi_R + j (I_c - I_R \sin \phi_R)$$

$$|I_s| < |I_R|$$

Imag part
is $\downarrow$ i.e. so
 I_c is $\downarrow$

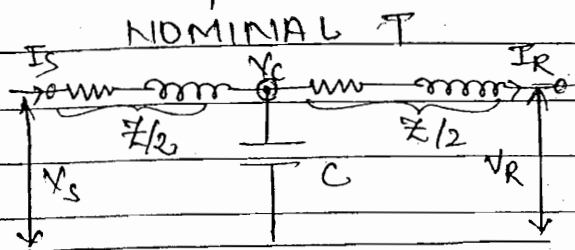


$$I_{TL} = I_R + I_{cs}$$

- Comparison B/w short & Medium Tr-line:-

PARAMETER	SHORT LINE	MEDIUM LINE
I_s	$ I_s = I_R $	$ I_s < I_R $ due to I_c
P_L	More	Less "
η	less	More "
% VREG	More	less "
P_s	More	less "

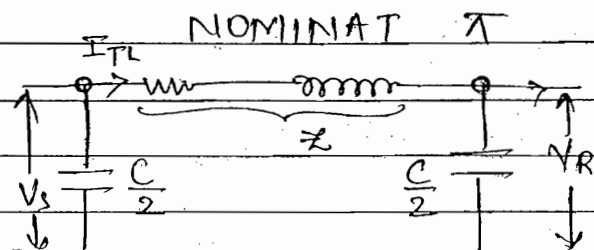
• Comparison b/w Nominal T and Nominal π N/w



$$I_S = \frac{V_S - V_C}{Z/2} \quad ; \quad I_R = \frac{V_C - V_R}{Z/2}$$

Node = 3 Eqⁿ = 2

- No. of Nodes are 3, so that No. of Eqⁿ are more



$$I_{TL} = \frac{V_S - V_R}{Z}$$

Node = 2 Eqⁿ = 1

- No. of Nodes are only 2 so that No. of eqⁿ are less

- The external shunt capacitor can't be easily combine with the line capacitance

- It is easily combine with the line capacitance

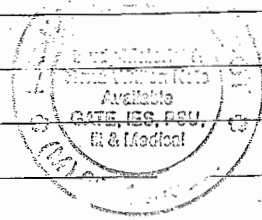
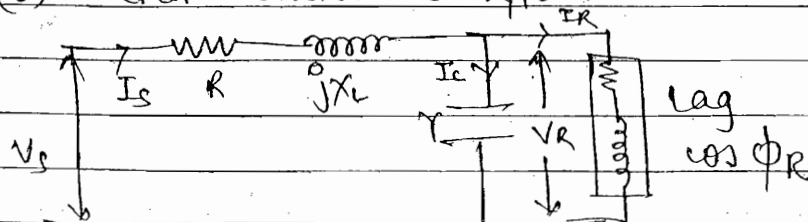
- The line capacitance is concentrated at the middle of the line

- Line capacitance is distributed at both sending and receiving end

- It is used for analyse the effect of capacitance at the middle of the line

- It is used in the load flow analysis as an equivalent ckt due to no. of eqⁿ are less so that faster calculation is possible

(3) End Condenser N/w



$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} (1 + YZ) & Z \\ Y & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$(1) \% V_{REG} = \frac{|V_s/A| - |V_R|}{|V_R|} \times 100$$

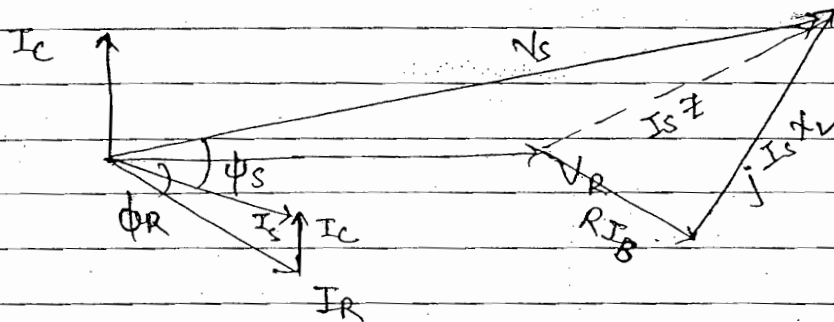
$$\text{where } A = (1 + YZ)$$

$$(2) \% \eta = \frac{P_R}{P_R + P_L} \times 100$$

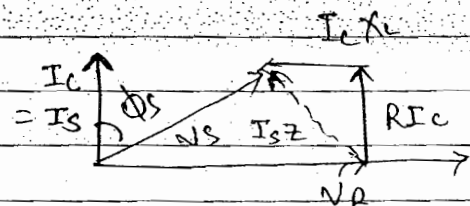
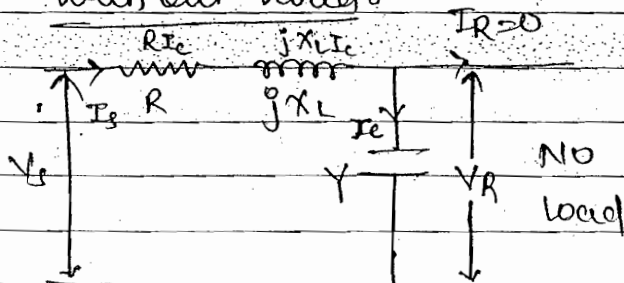
$$P_L = R I_s^2 \text{ for 1-}\phi$$

$$P_L = 3 R I_s^2 \text{ for 3-}\phi$$

PHASOR DIAGRAM:-



With out load:-



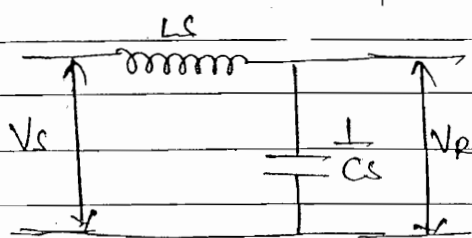
PHASOR DIAGRAM.

Ferranti effect.

$$|V_s| < |V_R|$$

- Ferranti effect occurs in case of Medium and long Tr-line under No load or light load condition.
- If the loading of line is more than surge impedance loading (SIL) then $V_R < V_s$ occurs.

- If the loading of line is equal to SIL Then $V_R = V_S$ occurs.
- If the loading of line is less than SIL Then $V_R > V_S$ i.e. Ferranti effect occurs. For compensation of this Ferranti effect shunt reactor is connected at the load end. The value of shunt reactor $X_{sh} = \frac{B}{(1-A)}$
- The overhead Tr-line can be loaded more than SIL
- In case of power cables, there should be operate less than SIL for safe operation of the power cable
- Increment of V_R (ΔV_R)



$$V_R = V_S + V_S \cdot \omega^2 LC$$

$$= V_S + (\Delta V_R)$$

$$\Delta V_R = V_S \cdot \omega^2 LC \quad \text{--- (1)}$$

- Velocity of signal (v):-

$$L_1 = \frac{\mu_0 \mu_r}{2\pi} \ln\left(\frac{d}{r}\right) \text{ H/m}$$

Assume $r' \approx r$

$$L_1 = \frac{\mu_0 \mu_r}{2\pi} \ln\left(\frac{d}{r}\right) \text{ H/m}$$

$$C_1 = \frac{2\pi \epsilon_0 \epsilon_r}{\ln(d/r)} \text{ F/m}$$

$$L_1 C_1 = \mu_0 \mu_r \epsilon_0 \epsilon_r$$

$$v = \frac{1}{\sqrt{L_1 C_1}} = \frac{3 \times 10^8}{\sqrt{\mu_r \epsilon_r}} \text{ m/sec} \quad \text{--- (2)}$$

l = length of line

$$X_L = \text{Total inductive reactance}$$

$$= 2\pi f L_1 l$$

$$L_1 = \frac{X_L}{2\pi f l} \quad (3)$$

B = Total capacitive susceptance

$$C_1 = \frac{B}{2\pi f l} \quad (4)$$

Substitute (3), (4) in (2)

$$V = \frac{2\pi f l}{\sqrt{B \cdot X_L}} \quad (5)$$

Substitute (2) in eqn (1)

$$\Delta V_R = V_s \omega^2 LC \Rightarrow V_s (2\pi f)^2 L_1 C_1 l$$

$$\Delta V_R = 4\pi^2 f^2 l^2 L_1 C_1 V_s$$

$$\Delta V_R = \frac{4\pi^2 f^2 l^2 V_s}{v^2} \quad (6)$$

Substitute (5) in (6)

$$\Delta V_R = V_s \cdot B \cdot X_L \quad V_R = V_s + \Delta V_R$$

(1) Ideal: $v = 3 \times 10^8 \text{ m/s} = 300 \text{ m}/\mu\text{s}$

(2) Practical: Overheadline $v = 200 - 250 \text{ m}/\mu\text{s}$

(3) cable ($\epsilon_r \gg 1$) $v = 40 - 50 \text{ m}/\mu\text{s}$

Q. A 300 km long line is operating at NO load at a freq. of 60 Hz at $V_s = 2 \text{ p.u.}$ Calculate receiving end voltage.

Solve
$$\Delta V_R = \frac{4 \times 3.14^2 \times 60^2 \times (300 \times 10^3)^2 \times 2}{(3 \times 10^8)^2}$$

$$= 0.98$$

$$V_R = V_s + \Delta V_R = 2.98 \text{ p.u.}$$

Q.13 $f = 50 \text{ Hz}$ $X_L = 0.045$ $B = 1.2 \mu\text{F}$
 $v = 3 \times 10^5$ $\lambda = ?$

$$v = \frac{2\pi f l}{\sqrt{B \cdot X_L}}$$

$$l = \frac{v \times \sqrt{B \cdot X_L}}{2\pi f} = \frac{3 \times 10^5 \times \sqrt{1.2 \times 0.045}}{2 \times 3.14 \times 50}$$

$$= 222.0 \text{ km} \quad \underline{\text{Ans}}$$

Q. A ~~for~~ 220 kV Tr-line operating at $V_s = 220 \text{ kV}$
 and $A = D = 0.9 \angle 0^\circ$ $B = 150 \angle 90^\circ \Omega$
 $C = 0.4 \times 10^{-6} \text{ pu}$ calculate

① V_R and I_C at No load

② Shunt reactor required for maintaining $V_s = V_R$

Solution

$$\textcircled{1} V_R = \frac{V_s}{A} = \frac{220}{0.9 \angle 0^\circ}$$

$$= 244.4$$

$$\textcircled{2} I_C = I_C = C V_R = 0.4 \times 10^{-6} \times 244.4 \times 10^3$$

$$= 0.056$$

$$\textcircled{3} X_{sh} = \frac{B}{(1-A)} = \frac{150 \angle 90^\circ}{(1 - 0.9 \angle 0^\circ)}$$

$=$

Commercial
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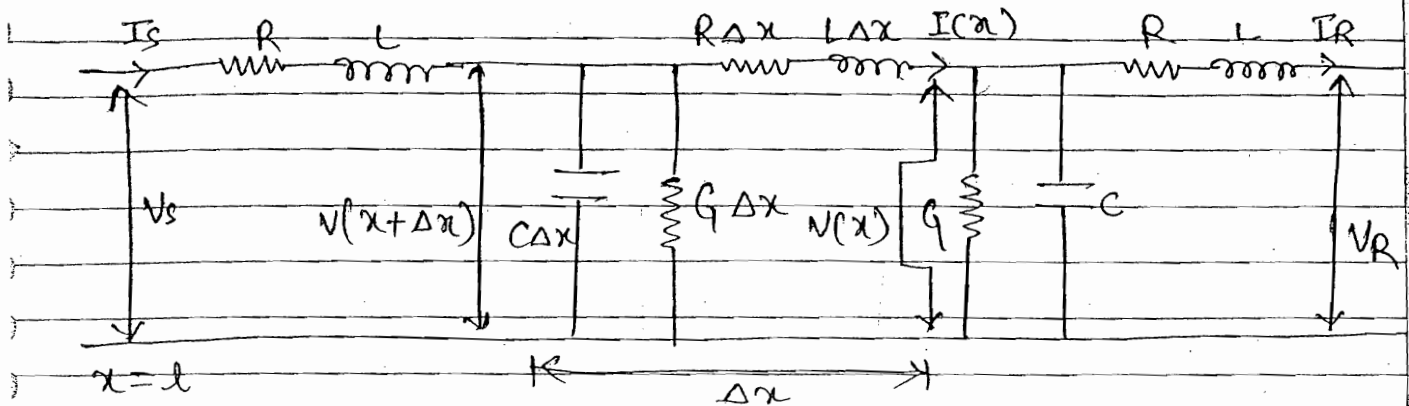
③ Long Tr-line :-

• ABCD parameter using Long Tr-line Rigorous solution Method :-

(Repeat and extend on both side)

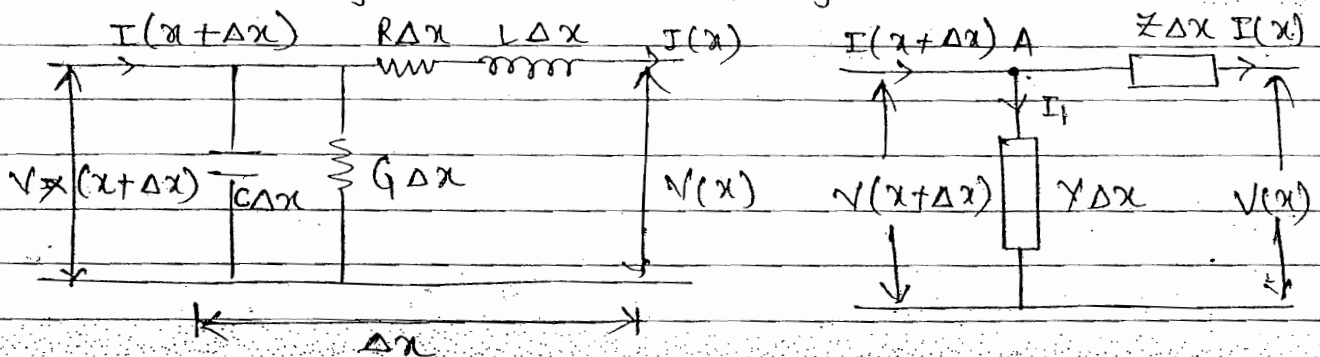
Boundary Condition :- At $x=0$ $V(x) = V_R$
 $I(x) = I_R$

$$x = l, \quad V(x) = V_s \quad I(x) = I_s$$



propagation Constant $= \gamma = \alpha + j\beta = \sqrt{ZY}$
 Characteristic Impedance $= Z_0 = \sqrt{\frac{Z}{Y}}$

$$Z = (R + j\omega L) \quad , \quad Y = (G + j\omega C)$$



Apply KVL $V(x + \Delta x) = V(x) + Z \Delta x \cdot I(x)$

$$\lim_{\Delta x \rightarrow 0} \frac{V(x + \Delta x) - V(x)}{\Delta x} = \lim_{\Delta x \rightarrow 0} Z I(x)$$

$$\frac{dV}{dx} = -Z I(x)$$

Apply KCL at Node A

$$I(x + \Delta x) = I_1 + I(x)$$

$$I(x + \Delta x) - I(x) = Y \Delta x \cdot V(x + \Delta x)$$

$$\lim_{\Delta x \rightarrow 0} \frac{I(x + \Delta x) - I(x)}{\Delta x} = \lim_{\Delta x \rightarrow 0} Y V(x + \Delta x)$$

$$\frac{dI}{dx} = -Y V(x) \quad \text{--- (2)}$$

from (1) :- $\frac{d}{dx} \left[\frac{dV}{dx} \right] = \frac{d}{dx} [Z I(x)]$

$$\frac{d^2 V}{dx^2} = Z \cdot \frac{d I(x)}{dx} = Z \gamma V(x)$$

$$\frac{d^2 V}{dx^2} = \gamma^2 V(x) \quad \text{--- (3)} \quad \left[\because \gamma = \sqrt{ZY} \right]$$

Solution of (3)

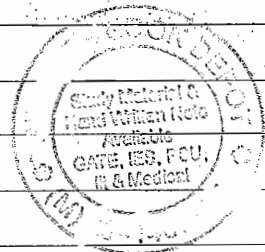
$$V(x) = A_1 e^{\gamma x} + A_2 e^{-\gamma x} \quad \text{--- (4)}$$

$$\frac{dV(x)}{dx} = Z I(x) = \gamma [A_1 e^{\gamma x} - A_2 e^{-\gamma x}]$$

$$I(x) = \frac{\gamma}{Z} [A_1 e^{\gamma x} - A_2 e^{-\gamma x}]$$

$$I(x) = \frac{1}{ZC} [A_1 e^{\gamma x} - A_2 e^{-\gamma x}]$$

$$\left[\because \frac{\gamma}{Z} = \frac{\sqrt{ZY}}{Z} = \sqrt{\frac{Y}{Z}} = \frac{1}{ZC} \right]$$



Apply at $x=0$

$$V(x) - V_R I(x) = I_R$$

in eqn (4) and (5)

$$V_R = A_1 + A_2 \quad \text{--- (6)}$$

$$I_R = \frac{1}{ZC} (A_1 - A_2)$$

$$I_R ZC = A_1 - A_2 \quad \text{--- (7)}$$

By solving (6) & (7)

$$A_1 = \frac{V_R + I_R ZC}{2} \quad \text{--- (8)}$$

$$A_2 = \frac{V_R - I_R ZC}{2} \quad \text{--- (9)}$$

Substitute (8) & (9) in (4)

$$V(x) = \left[\frac{V_R + I_R ZC}{2} \right] e^{\gamma x} + \left[\frac{V_R - I_R ZC}{2} \right] e^{-\gamma x} \quad \text{--- (10)}$$

$$= V_R \left[\frac{e^{\gamma x} + e^{-\gamma x}}{2} \right] + I_R ZC \left[\frac{e^{\gamma x} - e^{-\gamma x}}{2} \right]$$

$$= V_R \cosh \gamma x + I_R ZC \sinh \gamma x$$

--- (11)

Apply at $x=l$, $V(x) = V_l$ in (11)

$$V_s = \underbrace{V_R \cosh \gamma l}_A + \underbrace{I_R ZC \sinh \gamma l}_B \quad \text{--- (12)}$$

Substitute (8), (9) in (5)

$$I(x) = \frac{1}{ZC} \left[\frac{V_R + I_R ZC}{2} \right] e^{\gamma x} - \frac{1}{ZC} \left[\frac{V_R - I_R ZC}{2} \right] e^{-\gamma x} \quad \text{--- (13)}$$

$$= \frac{V_R}{Z_c} \left[\frac{e^{\gamma x} - e^{-\gamma x}}{2} \right] + I_R \left[\frac{e^{\gamma x} + e^{-\gamma x}}{2} \right]$$

$$= \frac{V_R}{Z_c} \sinh \gamma x + I_R \cosh \gamma x \quad \text{--- (14)}$$

Apply at $x=l$, $I(x) = I_s$ in (14).

$$I_s = \frac{V_R \sinh \gamma l + I_R \cosh \gamma l}{Z_c} \quad \text{--- (15)}$$

from (12) and (15)

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \cosh \gamma l & Z_c \sinh \gamma l \\ \frac{\sinh \gamma l}{Z_c} & \cosh \gamma l \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$A = D = \cosh \gamma l, \quad AD - BC = 1$$

$$(1) \% V_{REG} = \frac{|V_s/A| - |V_R|}{|V_R|} \times 100$$

$$\text{where } A = \cosh(\gamma l)$$

$$(2) \% \eta = \frac{P_R}{P_s} \times 100 = \frac{|V_R I_R \cos \phi_R|}{|V_s I_s \cos \phi_s|} \times 100$$

$$P_i = P_s - P_R$$

① Equivalent π Network of long line :-

From long line :-

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \cosh \gamma l & Z_c \sinh \gamma l \\ \frac{\sinh \gamma l}{Z_c} & \cosh \gamma l \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad \text{--- (1)}$$

From Nominal π Network :-

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \left(1 + \frac{YZ}{2}\right) & Z \\ Y\left(1 + \frac{YZ}{4}\right) & \left(1 + \frac{YZ}{2}\right) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad \text{--- (2)}$$

Comparing ① & ②

$$Z = Z_c \sinh(\gamma l)$$

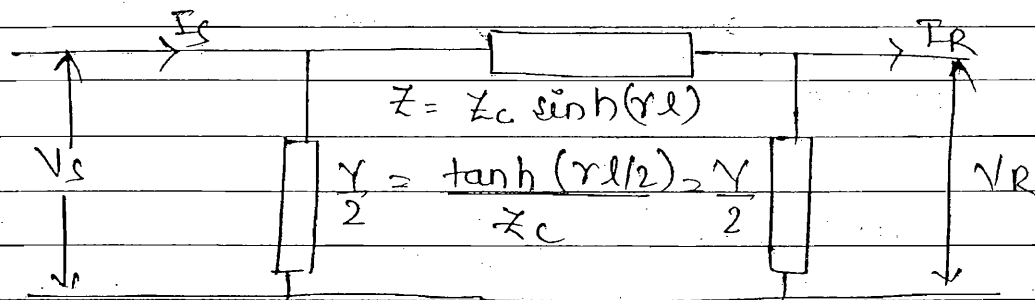
$$1 + \frac{Y}{2} \cdot Z = \cosh(\gamma l) \quad , \quad \frac{Y}{2} = \frac{\cosh(\gamma l) - 1}{Z}$$

$$\left| \frac{Y}{2} \right| = \frac{1 - 2 \sinh^2(\gamma l/2) - 1}{Z_c \sinh(\gamma l)}$$

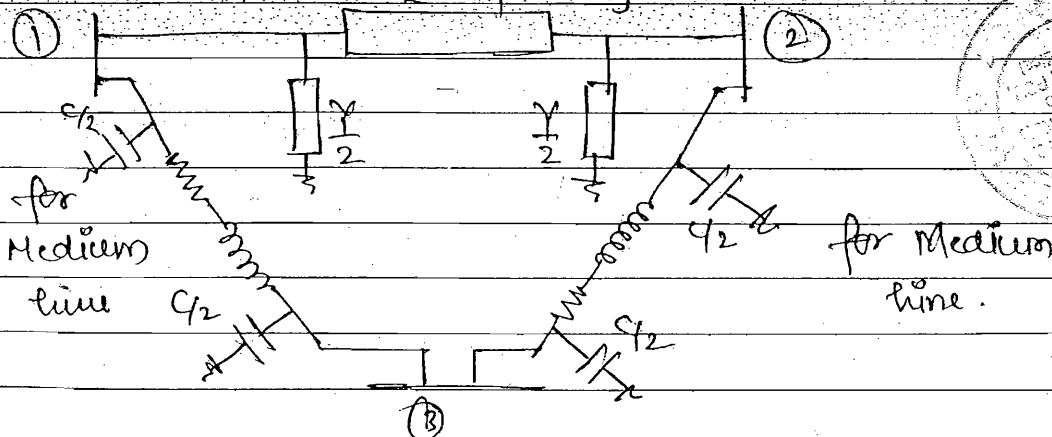
$$= \frac{2 \sinh^2(\gamma l/2)}{Z_c (2 \sinh(\gamma l/2) \cdot \cosh(\gamma l/2))}$$

$$= \frac{\sinh(\gamma l/2)}{Z_c \cosh(\gamma l/2)}$$

$$\left| \frac{Y}{2} \right| = \frac{\tanh(\gamma l/2)}{Z_c}$$



Z for long Tr-line.

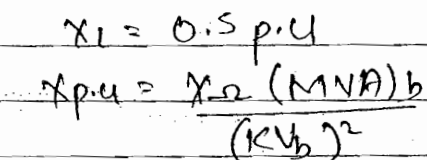


- for Representing the long Tr-line in the load flow analysis equivalent π N/w is used

(42)  $V_R = \frac{V_s}{2} + \sqrt{\frac{V_s^2}{4} - 4X_L R} = 1.49 \text{ p.u.}$

$$(43) \quad \frac{Q_2}{Q_1} = \left(\frac{V_2}{V_1} \right)^2 \cdot \left(\frac{f_1}{f_2} \right) \Rightarrow \frac{Q_2}{100} = \left(\frac{0.98 V_1}{V_1} \right)^2 \times \frac{f_1}{0.96 f_1}$$

$$\Rightarrow Q_2 = 100.04$$



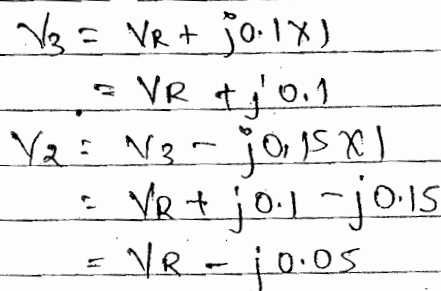
$$0.2 = \frac{\lambda_n \cdot (100)^2}{(11)^2}$$

$$X_L = 0.242 \Omega$$

$$Q = \frac{|V_C| |V_R|}{X_L} \cos \delta - \frac{|V_R|^2}{X_L} = \frac{11 \times 11}{0.242} \cos(11.53^\circ) - \frac{11^2}{0.242}$$

$$= -100 \text{ MVAR.}$$

$$(45) \quad X_{Lm} = \frac{B}{(1-A)} = \frac{200 \angle 90^\circ}{1-0.9} = 2000 \angle 90^\circ$$



$$= 1/R - j0.05 + j0.1$$

$$= 1/R + j0.05$$

V_3 is
maximum

$$(51) \quad Z = 8 + j6, \quad V = 400 \text{ V} \quad \cos \phi_1 = 0.9 \text{ lagg.}$$

$$Q_c = P_1 (\tan \phi_1 - \tan \phi_2)$$

$$= \frac{3 V_1^2}{Z} (\tan \phi_1 - \tan \phi_2)$$

$$= \frac{3 \times 400^2}{\sqrt{8^2 + 6^2}} \left(\tan \phi_1 - \tan \left(\frac{6}{8} \right) \leftarrow \tan \cos^{-1} 0.9 \right)$$

$$= 10.2 \text{ KVAR}$$

Best of DPF

$$(53) \quad C_{ph} = \frac{P_1 (\tan \phi_1 - \tan \phi_2)}{3 (2\pi f V_{ph}^2)} = \frac{200 \times 10^3 [\tan \cos^{-1} 0.8 - \tan \cos^{-1} 1]}{3 \times (2\pi \times 50 \times (11 \times 10^3)^2)}$$

cap. Bank) Δ

$$= 1.316 \mu\text{F}$$

$$(54) \quad (a) \quad P_s = \frac{V_s V_R}{X_L} \sin \delta = \frac{100^2}{5} \sin 30 = 1000 \text{ W}$$

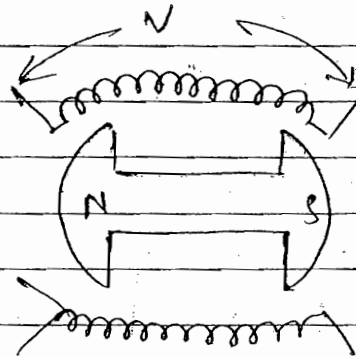
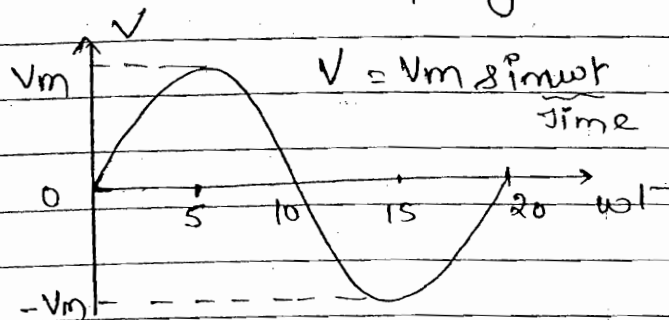
$$Q_s = \frac{V_s V_R}{X_L} \cos \delta - \frac{V_R^2}{X_L} \Rightarrow 268 \text{ VAR}^c$$

12/7/2014

Travelling Waves OR Transient In Tr-line:-

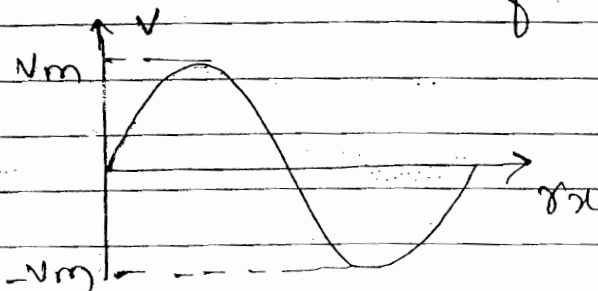
Power sys N/w experiences abnormalities like shortckt, open circuit and lightning surges so that power flow within the line is disturb produces transient in the sys. These transients causes over voltages, over currents so that damaging of electrical appliances and equipments like Transformer, Tr-line, generators, bus, etc. These equipment must be protected from this transient abnormalities. For designing and location of protecting equipment lightning arrestors, surge diverters, earth conductors, ground rods, counter poise, arcing horns

has to be properly located.



$$T = 20 \text{ ms}$$

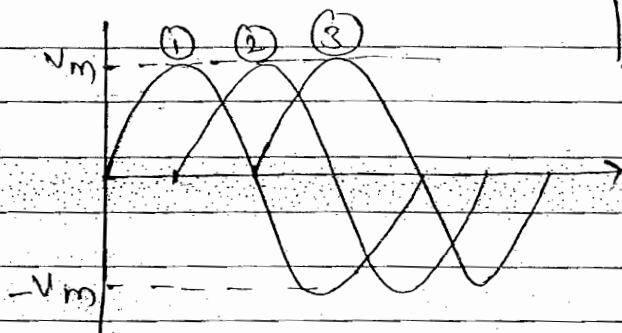
$$f = 50 \text{ Hz} \quad T = \frac{1}{f} = 20 \text{ ms} = 1 \text{ cycle.}$$



$$V = V_m \sin(rx)$$

space / distance.

$$V = V_m \sin(\omega t - rx)$$



$$V = V_m \sin(\omega t - rx)$$

Travelling wave equation

	rx	V
①	0	$V_m \sin \omega t$
②	90°	$-V_m \cos \omega t$
③	180°	$-V_m \sin \omega t$

$$V = V_m \sin(\omega t \pm rx)$$

$$\left| \frac{dV}{dx} \right| = \pm V_m \cos(\omega t \pm rx)$$

$$\left| \frac{d^2V}{dx^2} \right| = \gamma^2 V_m \sin(\omega t \pm rx)$$

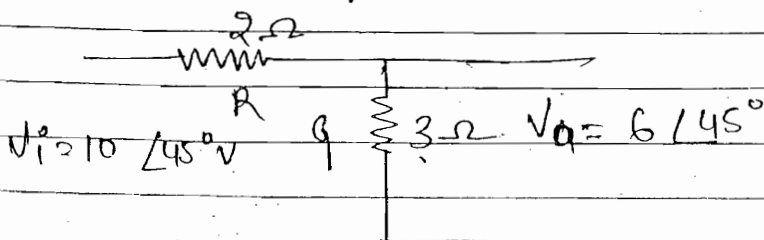
$$\therefore V_m \sin(\omega t \pm rx) = V$$

$$\boxed{\frac{d^2V}{dx^2} = \gamma^2 V}$$

eqn ③ in long Tr-line.

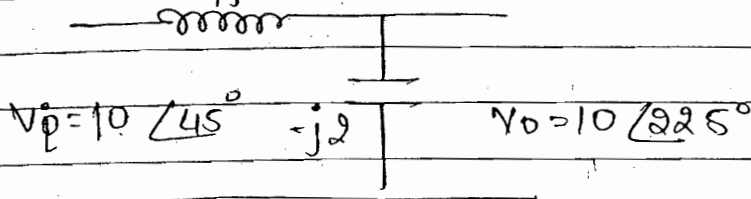
- $V = V_m \sin(\omega t \pm \gamma x)$ represents Travelling wave equation, $\pm \gamma$ indicates wave is travelling on $\pm ve$ x axis, $-\gamma$ indicates wave is travelling on $+ve$ x axis
- During travelling or propagating voltage or current signal through the Tr-line due to R and G parameters attenuation of signal occurs. This is measure in dB represented as α
- Due to LC components phase shift of the signals occurs it is measured in degrees or radians represented as β
- This attenuation and phase shift occurs if the voltage and current signals are travelling through the Tr-line. This also called propagation. represented as γ which is a constant.
- The relation between voltage and currents are depending on the values of R, G, L, C which are depends on type of configuration used so that characteristic behaviours of current and voltages are depends on characteristic impedance of line which are represented by Z_c measured in ohms

• Attenuation Network (α):-

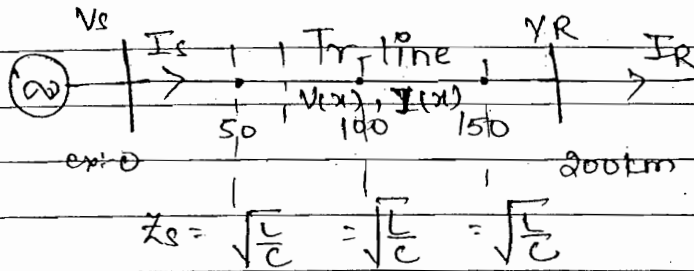


→ magnitude → change
phase → same

- Phase shifting N/w:- (B)

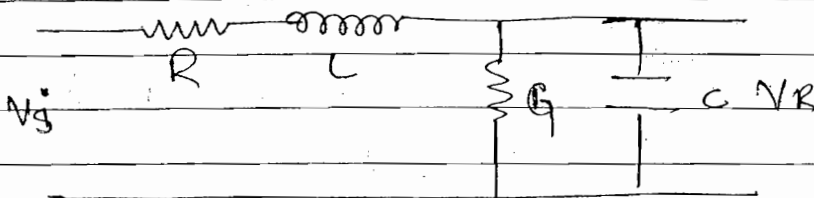


magnitude $\rightarrow$ same
phase $\rightarrow$ change.



at any point In
Tr-line Z_c remain
same. Independent to
length of Tr-line

- Combining both the N/w:-



losses occur
mainly due to
 R, G .

$$\gamma = \alpha + j\beta = \sqrt{ZY} = \sqrt{(R + j\omega L)(G + j\omega C)}$$

$$Z_c = \frac{V(x)}{I(x)} = \sqrt{\frac{Z}{Y}} = \sqrt{\frac{(R + j\omega L)}{(G + j\omega C)}}$$

- Lossless / loss free line:- $G = R = 0 \Rightarrow$ lossless line

- α, β, γ for lossless line:-

$$\gamma = \alpha + j\beta = \sqrt{(0 + j\omega L)(0 + j\omega C)}$$

$$\gamma = \alpha + j\beta = j\omega \sqrt{LC}$$

$$\boxed{\alpha = 0}$$

$$\boxed{\beta = \omega \sqrt{LC}}$$

$$\gamma = j\beta \therefore \alpha = 0$$

$$j\omega \sqrt{LC} = j\beta$$

$$\beta = \omega \sqrt{LC}$$

$$v = \text{velocity}_{\text{light}} = 3 \times 10^8$$

$$\beta = 2\pi f \sqrt{LC} \quad \text{radian}$$

$$\beta = \frac{2\pi fl}{v} \quad \text{radian}$$

$$\beta = \frac{360 fl}{v} \quad \text{degrees}$$

• A, D for lossless line:

$$A = D = 1 + \frac{YZ}{2}$$

For lossless line $Z = j\omega L$, $Y = j\omega C$

$$A = D = 1 + \frac{(j\omega L)(j\omega C)}{2} = 1 - \frac{\omega^2 LC}{2}$$

$$A = D = 1 - \frac{\beta^2}{2}$$

$\beta \Rightarrow \text{radian}$

$$\beta = \omega \sqrt{LC}$$

Surge / lossless / loss free / Transmission line / Flat line / Infinite line / Resonant Impedance (Z_s)
[$R = G = 0$]

$$Z_c = Z_s = \sqrt{\frac{L}{C}} = \sqrt{\frac{L_1 l}{C_1 l}} = \sqrt{\frac{L_1}{C_1}}$$

$$L = L_1 l$$

$$C = C_1 l$$

- ① Overhead line: $Z_s = 300 - 500 \Omega$
- ② Cable: $Z_s = 40 - 50 \Omega$
- Surge impedance is independent to length of the Tr-line
- Distortionless line: line independent to frequency is called distortionless line. It is practically used in communication line.

$$Z_c = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$$

$\hookrightarrow C, f$ freq. depend neglect them.

$$Z_D = \sqrt{\frac{R}{G}}$$

$Z_D \rightarrow$ distortionless impedance

Q 600 km long Tr. line operating at 50 Hz Calculate phase shift of signal at 300 km.

Solution. $f = 50 \text{ Hz}$. $\beta = \frac{2\pi fl}{v} = \frac{360fl}{v}$

$$\beta = \frac{360 \times 50 \times 300 \times 10^3}{3 \times 10^8} = 18^\circ$$

$$= 18 \times \frac{\pi}{180} \text{ rad} = 0.314 \text{ rad}$$

Q A lossless Tr. line has $\beta = 200^\circ$ $V_s = 400 \text{ kV}$
 $l = 800 \text{ km}$ Find the voltage at 500 km and at 800 km
 at 800 km. Calculate shunt reactor required for compensating ferranti effect

Solution. $V_s = 400 \text{ kV}$ $B = 200^\circ$
 $C_n = \frac{\beta}{2\pi fl} = \frac{200^\circ}{2 \times 3.14 \times 50 \times 500}$

① $l = 500 \text{ km}$ $\beta = \frac{2\pi fl}{v} = \frac{2 \times 3.14 \times 50 \times 500 \times 10^3}{3 \times 10^8} = 0.523 \text{ rad}$

② $l = 800 \text{ km}$ $\beta = \frac{2 \times 3.14 \times 50 \times 800 \times 10^3}{3 \times 10^8} = 0.837 \text{ rad}$

$l = 500 \text{ km}$ $A = \frac{1 - \beta^2}{2} = \frac{1 - (0.523)^2}{2} = 0.863$

$V_{sh} = \frac{B}{(1-A)} = \frac{200^\circ}{1 - 0.863} = 1459.85^\circ$

$V_R = \frac{V_s}{A} = \frac{400}{0.863} = 463.49$

$l = 800 \text{ km}$ $A = \frac{1 - \beta^2}{2} = \frac{1 - (0.837)^2}{2} = 0.649$

$V_R = \frac{V_s}{A} = \frac{400}{0.649} = 616.33$

$V_{sh} = \frac{B}{1-A} = \frac{200^\circ}{1 - 0.649} = 569.19^\circ$

Q A 400 km long Tr-line has a surge impedance of 4 p.u. If the length of line is reduce to 300 km then its surge impedance is 400 km.

$$\beta = \frac{2\pi fl}{v} \Rightarrow \frac{2\pi fl}{\lambda f}$$

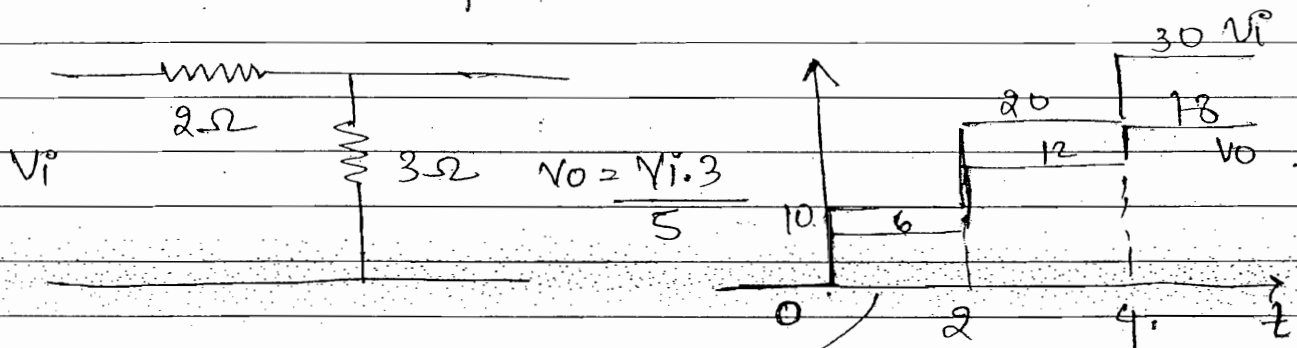
$$\beta = \frac{2\pi l}{\lambda}$$

$$\begin{cases} v = \lambda f \\ \lambda = \text{wave length} \end{cases}$$

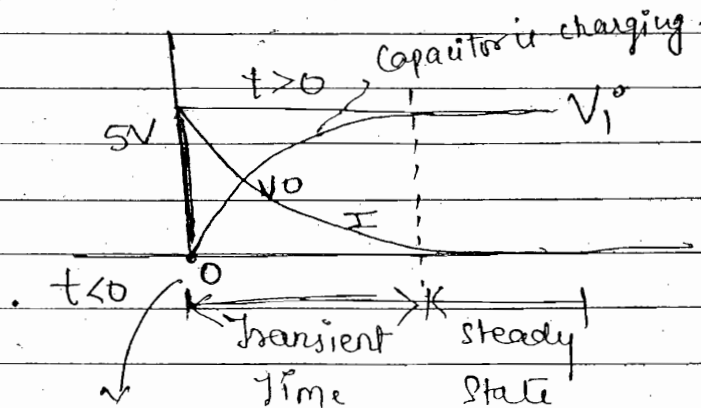
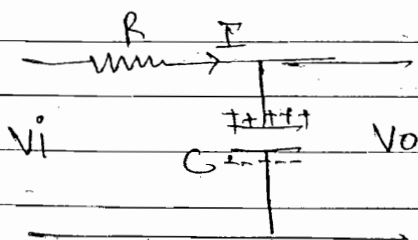
• Transient → when I/p change (sudden) O/p will not change sudden, it will cause delay in O/p w.r.t I/p called Transient.

→ R, G → do not response to Transient.

→ L, C → response to Transient.



No Transient "Zero ORDER"



$$T=0$$

$$f = \frac{1}{T} = \frac{1}{0} = \infty$$

when $f = \infty$ $C \rightarrow \text{short}$ $V_o = 0$

- Energy storing device responsible for transient. Energy dissipating device don't responsible for transient.

$$X_C = \frac{1}{2\pi fC}$$

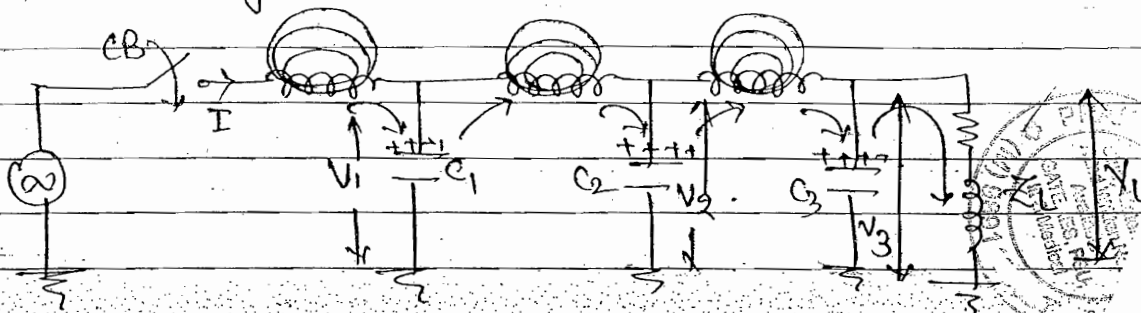
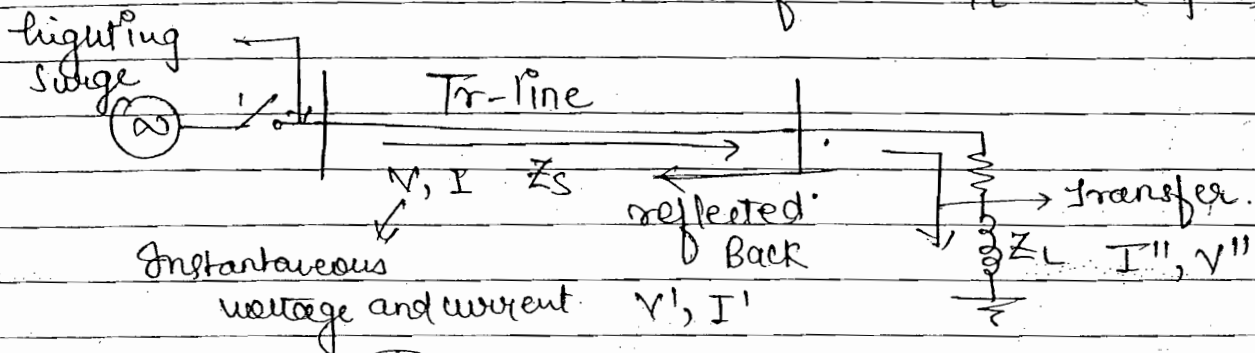
$$DC \Rightarrow f=0 \Rightarrow X_C = \infty \text{ (Open)}$$

$$AC \Rightarrow f=\infty \Rightarrow X_C = 0 \text{ (short)}$$

$$X_L = 2\pi fL$$

$$DC \Rightarrow f=0 \Rightarrow X_L = 0 \text{ (short)}$$

$$AC \Rightarrow f=\infty \Rightarrow X_L = \infty \text{ (open)}$$



$t=0$, CB-closed

$t>0$

$$\frac{1}{2} LI^2 = \frac{1}{2} CV^2$$

- when CB closed at $t=0$

$$L = \text{Open} \quad C = \infty$$

$$V_1 = V_2 = V_3 = 0 \quad V_L = 0$$

$$Z_C = \frac{V}{I} = \sqrt{\frac{L}{C}}$$

- When $t>0$ L short, $C = \text{Open}$, inductor store energy and charged the capacitor, current will start falling, charged capacitor gives it energy to next inductor, this inductor gives it energy to next capacitor and so on... and finally reach to load. This way waves are travelling.

$$V = V' + V''$$

$$I = I' + I''$$

Transmission coefficient of current Date _____

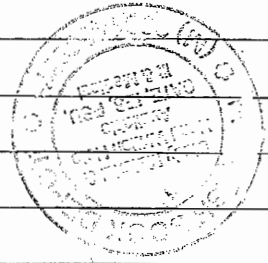
$$T_V = \frac{V''}{V}, \quad T_I = \frac{I''}{I}$$

Transmission coefficient of voltage

$$R_V = \frac{V'}{V}, \quad R_I = \frac{I'}{I}$$

Reflected coeff. of voltage

Reflected coeff. of current.



Z_L

① $Z_L \neq Z_s$	④ $Z_L = \infty$	⑦ $Z_L = \text{parallel lines}$
② $Z_L = Z_s$	⑤ $Z_L = L/S$	
③ $Z_L = 0$	⑥ $Z_L = \frac{1}{S}$	

- Incident Wave:- The voltage and current signal travelling from source to the load through the Tr-line is called incident wave

$$I = \frac{V}{Z_s}$$

- Reflected Wave:- Voltage and current signals travelling from load to source are called reflected wave.

$$I' = -\frac{V'}{Z_s}$$

where $Z_s = \text{Surge Impedance}$

$$Z_{Tr-line} = \sqrt{\frac{L}{C}}$$

- The voltage and current signals which are transmitting into the load are called transmitted or reflected wave

$$I'' = \frac{V''}{Z_L}$$

where $Z_L = \text{load impedance}$

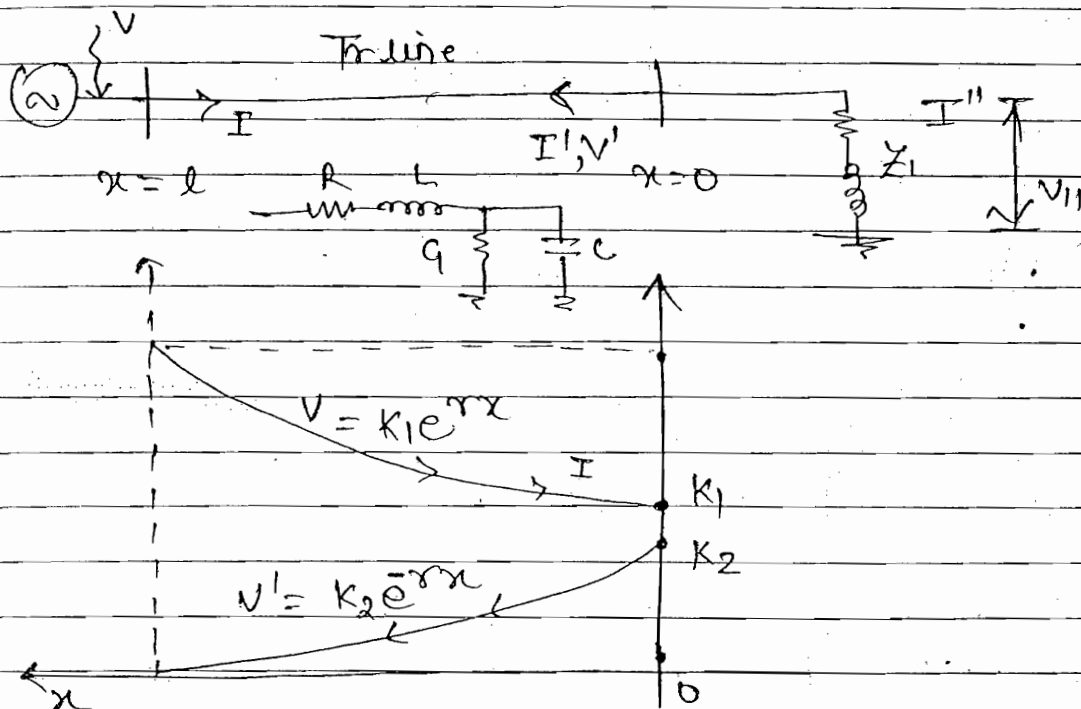
from long line eqn (10) & (13).

$$V(x) = \left(\frac{V_R + I_R Z_C}{2} \right) e^{\gamma x} + \left(\frac{V_R - I_R Z_C}{2} \right) e^{-\gamma x}$$

$$= k_1 e^{\gamma x} + k_2 e^{-\gamma x}$$

$$I(x) = \frac{1}{Z_c} \left(\frac{V_R + I_R Z_c}{2} \right) e^{\gamma x} - \frac{1}{Z_c} \left(\frac{V_R + I_R Z_c}{2} \right) e^{-\gamma x}$$

$$= \frac{1}{Z_c} k_1 e^{\gamma x} - \frac{1}{Z_c} k_2 e^{-\gamma x}$$



① $I = \frac{V}{Z_c}$, $R, G \neq 0$

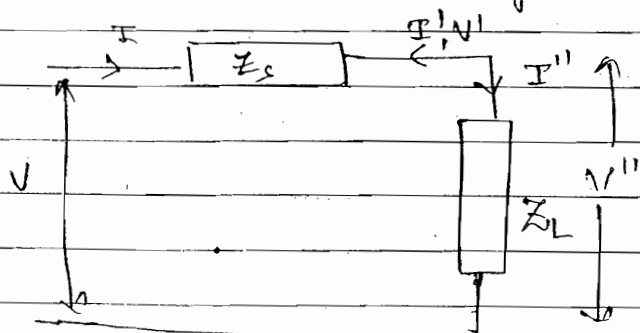
$= \frac{V}{Z_s}$, $R = G = 0$

we get constant
straight line

② $I' = -\frac{V'}{Z_c}$, $R \neq 0, G \neq 0$

$= -\frac{V'}{Z_s}$ if $G = R = 0$
straight line

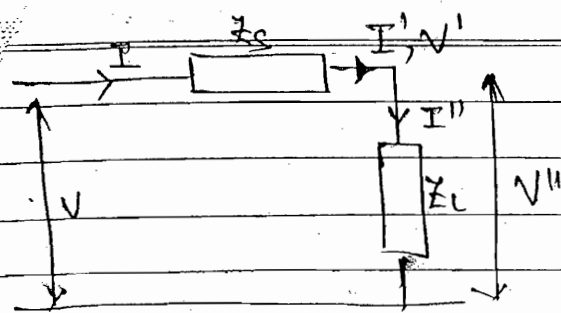
③ $I'' = \frac{V''}{Z_L}$



$V = V' + V''$
 $I = I' + I''$

$Z_s \neq Z_L$ so reflectⁿ.

In Infinite lines $\rightarrow$ No Reflectⁿ.



but of opposite direction
Sign convention

$$V = -V' + V''$$

$$I = -I' + I''$$

$Z_L \neq Z_s$

$$V'' = V + V'$$

$$I'' = I + I'$$

Coefficients:-

Reflection coefficient of voltage $= R_V = \frac{V'}{V}$

Reflection coefficient of current $= R_I = \frac{I'}{I}$

Transmitted / Refracted coefficient of voltage $= T_V = \frac{V''}{V}$

Transmitted / Refracted coefficient of current $= T_I = \frac{I''}{I}$

Relation Between Coefficient:-

(1) $V'' = V + V' \Rightarrow \frac{V''}{V} = 1 + \frac{V'}{V}$

$T_V = 1 + R_V$

(2) $I'' = I + I' \Rightarrow \frac{I''}{I} = 1 + \frac{I'}{I}$

$T_I = 1 + R_I$

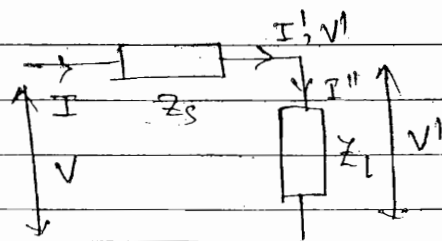
(3) $R_V = \frac{V'}{V} = -\frac{I' Z_s}{I Z_L}$ $R_V = -R_I$

(4) $T_I = \frac{I''}{I} = \frac{V''/Z_L}{V/Z_s}$ $T_I = T_V \cdot \frac{Z_L}{Z_s}$

Case (1): $Z_L \neq Z_s$

$$V'' = V + V'$$

$$V' = V'' - V$$



(1)

$$I'' = I + I' \quad , \quad \frac{V''}{Z_L} = \frac{V}{Z_S} - \frac{V'}{Z_S} \quad \text{--- (2)}$$

Substitute (1) in eqn (2)

$$\frac{V''}{Z_L} = \frac{V}{Z_S} - \frac{(V'' - V)}{Z_S}$$

$$\left[\frac{1}{Z_L} + \frac{1}{Z_S} \right] V'' = \frac{2V}{Z_S}$$

$$T_V = \frac{V''}{V} = \frac{2Z_L}{Z_L + Z_S}$$

• By Using Relation: $R_V = T_V - 1$

$$R_V = \frac{Z_L - Z_S}{Z_L + Z_S} = \frac{V'}{V}$$

$$R_I = \frac{I'}{I} = -R_V$$

$$T_I = 1 + R_I = 1 - R_V$$

$$T_I = \frac{I''}{I} = \frac{2Z_S}{Z_L + Z_S}$$

• Conclusion ($Z_L \neq Z_S$)

$$T_V = \frac{V''}{V} = \frac{2Z_L}{Z_L + Z_S}$$

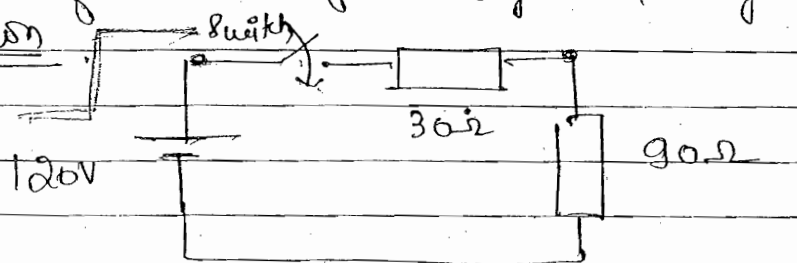
$$T_I = \frac{I''}{I} = \frac{2Z_S}{Z_L + Z_S}$$

$$R_V = \frac{V'}{V} = \frac{Z_L - Z_S}{Z_L + Z_S}$$

$$R_I = \frac{I'}{I} = -R_V$$

Q A dc voltage of 120V magnitude is applied to the N/w shown in fig. Calculate the voltage reflecting from the load end at the end of 5T where T = Time of travel of the signal through the line.

Solution



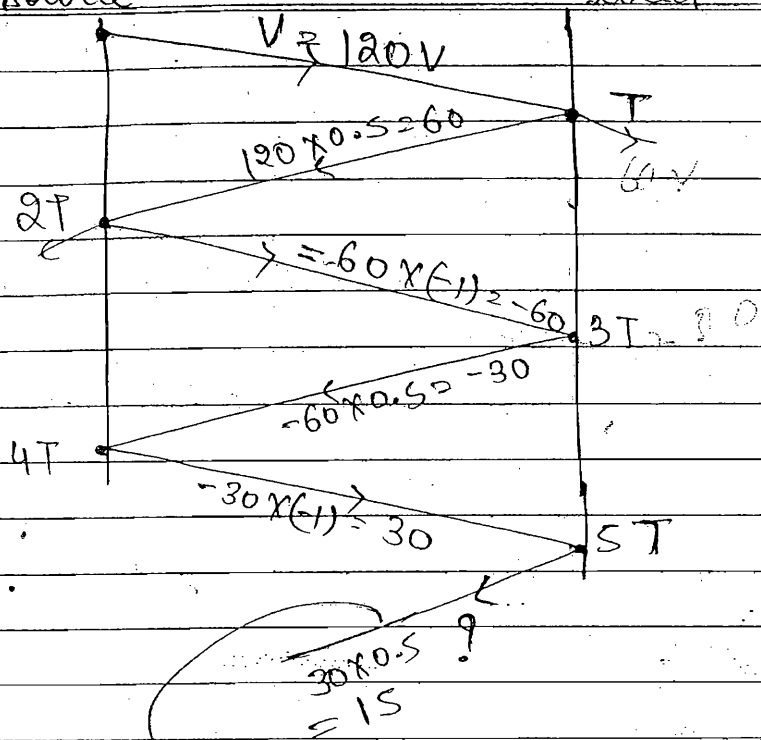
$$RV_s = -1$$

$$RV_R = 0.5$$

Source

Load

Date _____



$$RV_R = \frac{Z_L - Z_s}{Z_L + Z_s} = \frac{90 - 30}{90 + 30} = \frac{60}{120} = 0.5$$

$$RV_s = \frac{Z_L - Z_s}{Z_L + Z_s} = \frac{0 - 30}{0 + 30} = -1$$

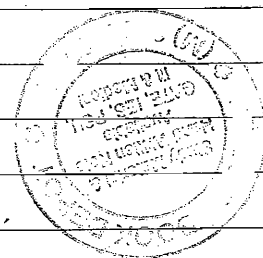
$$V' = RV_R \cdot V \quad \text{load side}$$

$$V' = RV_s \cdot V \quad \text{source side}$$

$$\sum V = 120 + (60) + (-60) + (-30) + 30 + 15 = 135 \text{ V Avg.}$$

Q A Tr. line has a surge impedance of 400Ω is terminated with a cable having surge impedance of 50Ω . If a lightning surge of 100 kV magnitude is travelling from the Tr. line towards the cable. Calculate

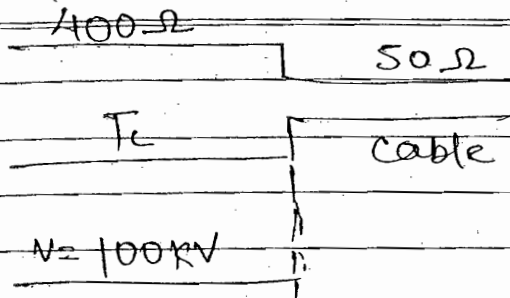
- (1) all the coefficients
- (2) Incident voltage and current
- (3) Reflected voltage and current
- (4) Transmitted voltage and current.



Soln^m (1) $Z_s = 400 \Omega$ $Z_L = 50 \Omega$

$$RV = \frac{Z_L - Z_s}{Z_L + Z_s} = \frac{50 - 400}{50 + 400} = \frac{-350}{450} = -0.77$$

$$R_I = -RV = 0.77$$



$$T_V = \frac{2Z_L}{Z_L + Z_S} = \frac{2 \times 50}{50 + 400} = 0.222$$

$$T_I = \frac{2Z_S}{Z_L + Z_S} = \frac{2 \times 400}{50 + 400} = 1.777$$

$$T_I = T_V \cdot \frac{Z_L}{Z_S} = 0.22 \times \frac{50}{400} = 0.0275$$

(2) $V = 100 \text{ kV}$

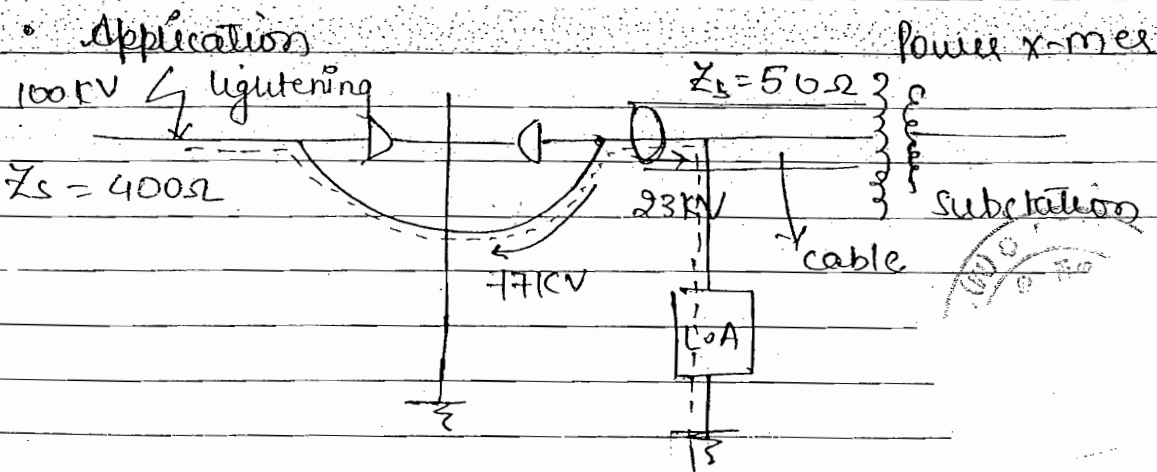
$$I = \frac{100 \times 10^3}{400} = 250 \text{ A}$$

(3) $V' = R_V \cdot V$
 $= (-0.777) \times 100$
 $= -77.7 \text{ kV}$

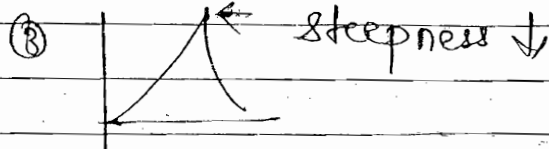
$$I' = -\frac{V'}{Z_S} = \frac{-77.7 \times 10^3}{400} = 194.25$$

(4) $V'' = T_V \cdot V$
 $= 0.22 \times 100 \times 10^3$
 $= 22 \text{ kV}$

$$I'' = \frac{V''}{Z_L} = \frac{22 \times 10^3}{50} = 440$$

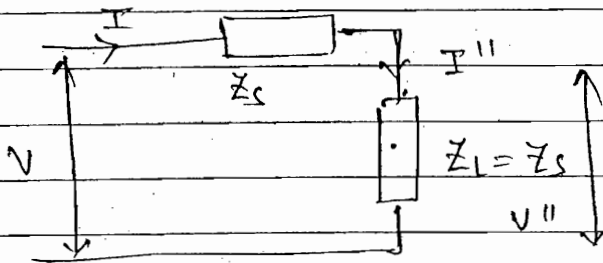


Advantages :- (1) $|V_{\text{surge}}| \downarrow$ (2) velocity $\downarrow$



↳ In fully areas where lightning occurs mostly, cables are used for reducing the magnitude of surge voltage so that rating of L.O.A. can be reduced, ex: 23KV through 1.4 and 77KV is reflected.

Case 2 : $Z_L = Z_S$



$$T_V = \frac{V''}{V} = \frac{2Z_L}{Z_L + Z_S}$$

$$T_V = \frac{V''}{V} = \frac{2Z_S}{Z_L + Z_S} = 1$$

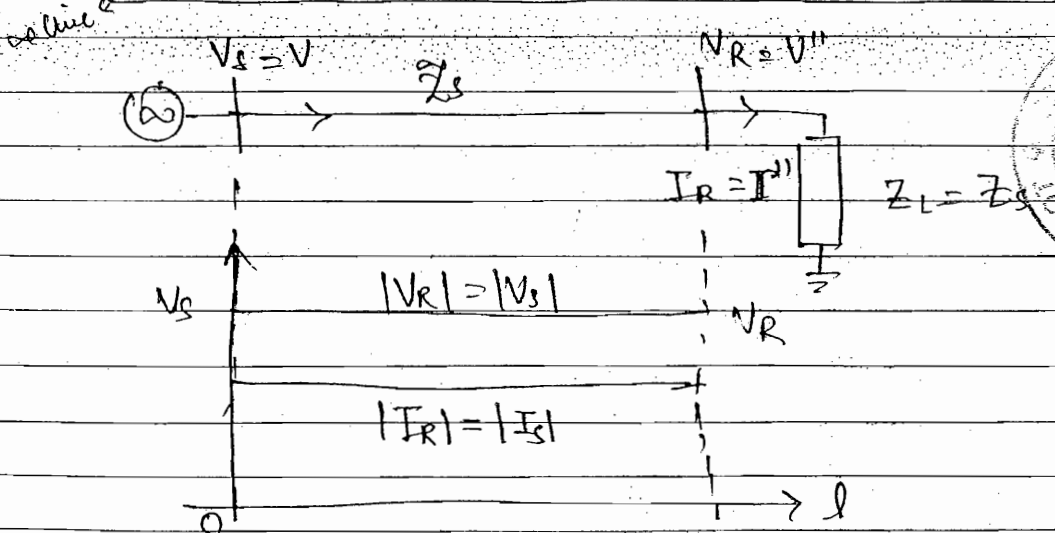
$$R_V = T_V - 1 = 1 - 1 = 0$$

$$R_I = -R_V = 0$$

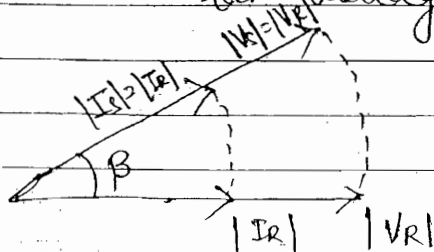
$$T_I = 1 + R_I = 1$$

Conclusion ($Z_L = Z_S$):

$T_V = 1 \Rightarrow V'' = V$	$T_I = 1 \Rightarrow I'' = I$
$R_V = 0 \Rightarrow V' = 0$	$R_I = 0 \Rightarrow I' = 0$



Flat voltage & current profile



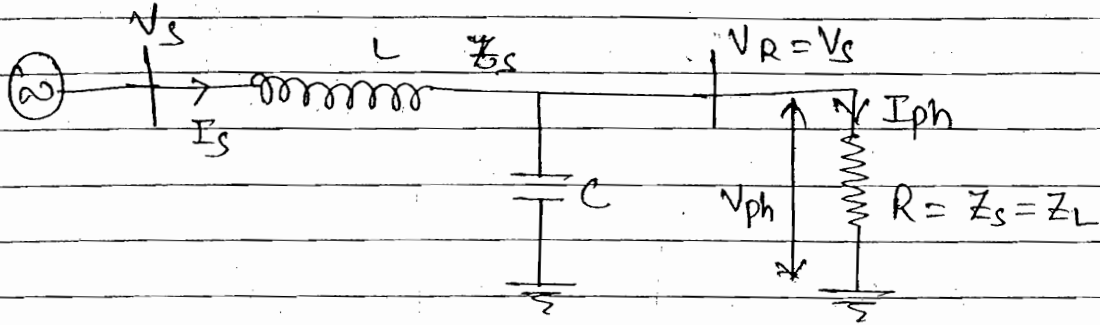
$$\beta = \omega \sqrt{LC}$$

I_S, V_S lead I_R, V_R by β But mag. remain same

Ideal case
convert into active power, ($\phi = 0$) -

Date _____

• Surge Impedance Loading (SIL):-



3 ϕ active power supplied to
pure R load [$\cos \phi = 1$] } = $3 V_{ph} I_{ph}$.

$$I_{ph} = \frac{V_{ph}}{R} = \frac{V_{ph}}{Z_s} = \frac{V_L}{\sqrt{3} Z_s};$$

$$|SIL| = P_{3\phi} = 3 \cdot \frac{V_L}{\sqrt{3}} \cdot \frac{V_L}{\sqrt{3} Z_s} = \frac{V_L^2}{Z_s} = \frac{V_s^2}{Z_s}$$

$$SIL = \frac{V_s^2}{Z_s}$$

where $Z_s = \sqrt{\frac{L}{C}}$, $L, C \Rightarrow$ phase values.

$V_s = V_L =$ line voltage

$$SIL = \frac{V_s^2}{Z_s} = V_s^2 \sqrt{\frac{C}{L}}$$

(1) $SIL \propto V_s^2$
(2) $SIL \propto \sqrt{C}$

(3) $SIL \propto \frac{1}{\sqrt{L}}$

- ① If $Z_L = Z_s$:- (1) Transmission coefficient $T_v = T_I = 1$
(2) Reflection coefficient $R_v = R_I = 0$

Hence line is called Infinite line

(3) $V_R = V_S =$, $I_R = I_S$ is maintain so that Tr-line produce flat voltage and current profile.

(4) V_S lead V_R By β , I_S lead I_R By β

(5) V_S and I_S and V_R and I_R are in phase produces unity works as unity p.f. load.

(6) Inductance of line required reactive power is supplied by capacitance of the line. There is No need of reactive power from the source.

(7) Maximum three phase active power is transmitting through the transmission line which is called

$$SIL = \frac{V_S^2}{Z_S}$$

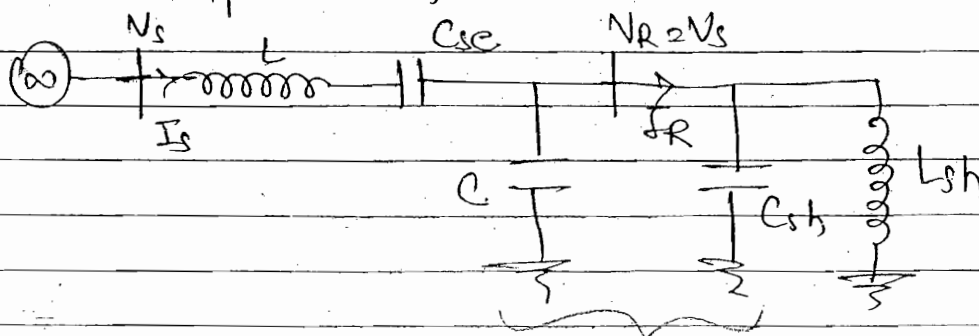
(8) Because of $V_S = V_R$ uniform voltage i.e. uniform insulation level for all the equipment like x-mere PT and CT can be maintain at both ends of line.

• Effect of Compensation on SIL:-

(1) Without Compensation:-

$$Z_{S1} = \sqrt{\frac{L}{C}} \quad (SIL)_1 = V_S^2 \sqrt{\frac{C}{L}}$$

(2) With Compensation



$$C_T = C + C_{sh} \\ = C \left[1 + \left(\frac{C_{sh}}{C} \right) \right] \text{ } \%$$

$$K_{se} = \frac{1}{\omega^2 L C_{se}} = \% \text{ or Degree of } C_{se}.$$

$$K_{csh} = \frac{C_{sh}}{C} = \% \text{ or Degree of } C_{sh}$$

$$K_{Lsh} = \frac{1}{\omega^2 L_{sh} C} = \% \text{ or Degree of } L_{sh}$$

$(SIL)_c$ = SIL with compensation
 Z_{sc} = Surge impedance with Compensation.

$$Z_{sc} = Z_{s1} \sqrt{\frac{(1-K_{se})}{(1+K_{csh})(1-K_{Lsh})}}$$

$$(SIL)_c = \frac{V_s^2}{Z_{sc}} = (SIL)_1 \sqrt{\frac{(1+K_{csh})(1-K_{Lsh})}{(1-K_{se})}}$$

Q A 3 ϕ Tr-line surge impedance = 400 Ω applied at 400 kV Find

① Surge Imp. loading without compensation

② If the line is compensated with 30% of shunt capacitor. Calculate Z_s and SIL with compensation

Q③ If the generator is connected at source end delivering 200 MW through these lines Calculate load angle δ .

① without compensation ② with compensation.

Solution (1)

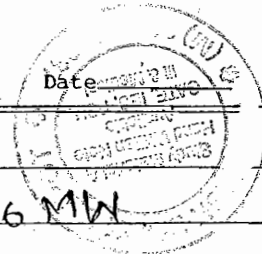
Without compensation: $V_s = 400 \text{ kV}$ $Z_{s1} = 400 \Omega$

$$SIL = \frac{V_s^2}{Z_{s1}} = \frac{400^2}{400} = 400 \text{ MW}$$

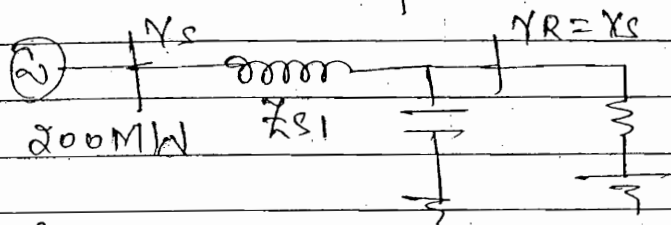
(2) With C_{sh} : $K_{csh} = 30\% = 0.3$

$$Z_{sc} = \frac{Z_{s1}}{\sqrt{1+K_{csh}}} = \frac{400}{\sqrt{1+0.3}} = 350.8 \Omega$$

$$(SIL)_c = (SIL)_1 \cdot \sqrt{1 + K_{sch}} \\ = 400 \cdot \sqrt{1 + 0.3} = 456 \text{ MW}$$



(3) (a) Without Compensation



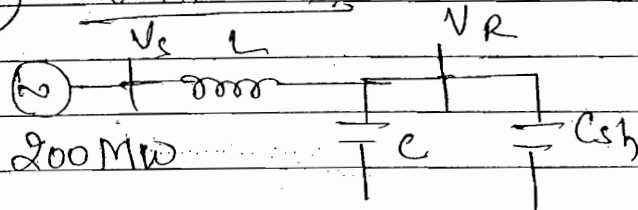
$$P_s = \left| \frac{V_s^2}{Z_{s1}} \right| \sin \delta_1$$

$$P_s = (SIL)_1 \sin \delta_1$$

$$200 = 400 \sin \delta_1$$

$$\boxed{\delta_1 = 30^\circ}$$

(b) with Csh:-

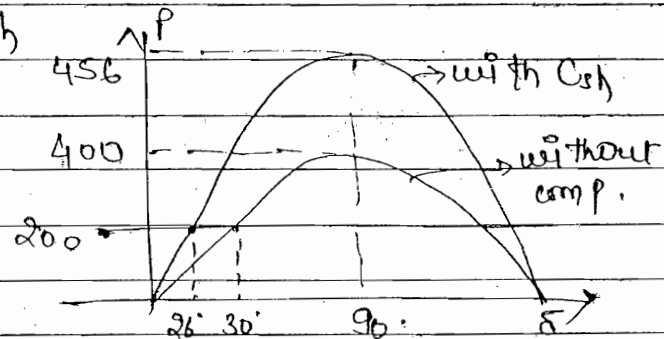


$$P_s = (SIL)_c \sin \delta_2$$

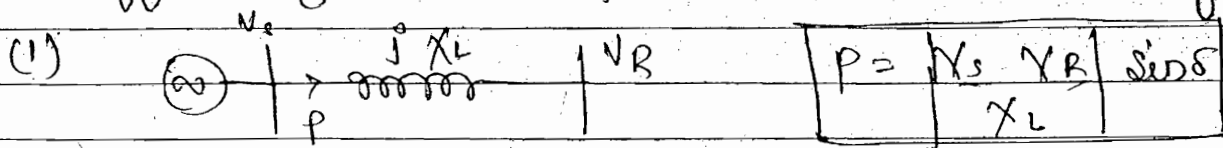
$$200 = 456 \sin \delta_2$$

$$\boxed{\delta_2 = 26^\circ} < \delta_1$$

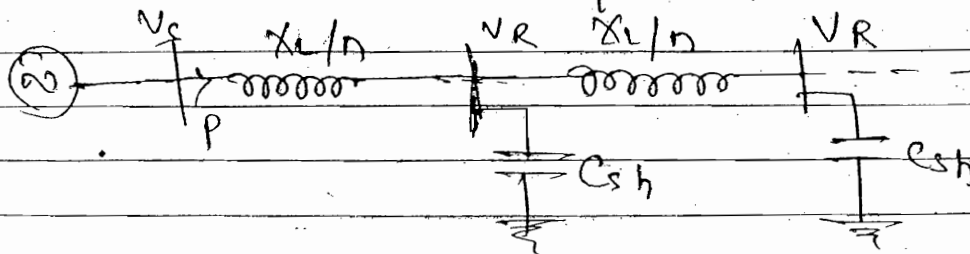
stability ↑



• Effect of Csh Compensation in n-Section of line



(2) line divided in n-Equal sections



$$P = \left| \frac{V_s V_R}{\left(\frac{X_L}{n} \right)} \right| \sin \left(\frac{\delta}{n} \right) = \left| \frac{n V_s V_R}{X_L} \right| \sin \left(\frac{\delta}{n} \right)$$

$$\text{If } V_s = V_R \Rightarrow P = \left| \frac{\eta V_s^2}{X_L} \sin \frac{\delta}{n} \right|$$

Max (or) Ideal or steady state power:-

$$P_{\max} = \left| \frac{\eta \cdot V_s V_R}{X_L} \right|$$

$$\text{If } V_R = V_s \quad P_{\max} = \left| \frac{\eta V_s^2}{X_L} \right|$$

Pg No. 54.

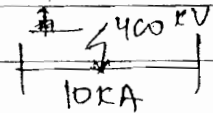
Q. 50 $X_L = 0.4 \quad V_{\text{width}} = 0.96$

$$P = \frac{2 V_s^2 \sin^2 \frac{\delta}{2}}{X_L} = \frac{2 \times 0.96^2}{0.4 \times 0.2} \quad P_{\max} = 4.8 \text{ p.u.}$$

Q. 47 $(SIL)_c = \frac{(SIL)_i}{\sqrt{1 - K_{sc}}} = \frac{2280}{\sqrt{1 - 0.3}} = 2725 \text{ MW}$

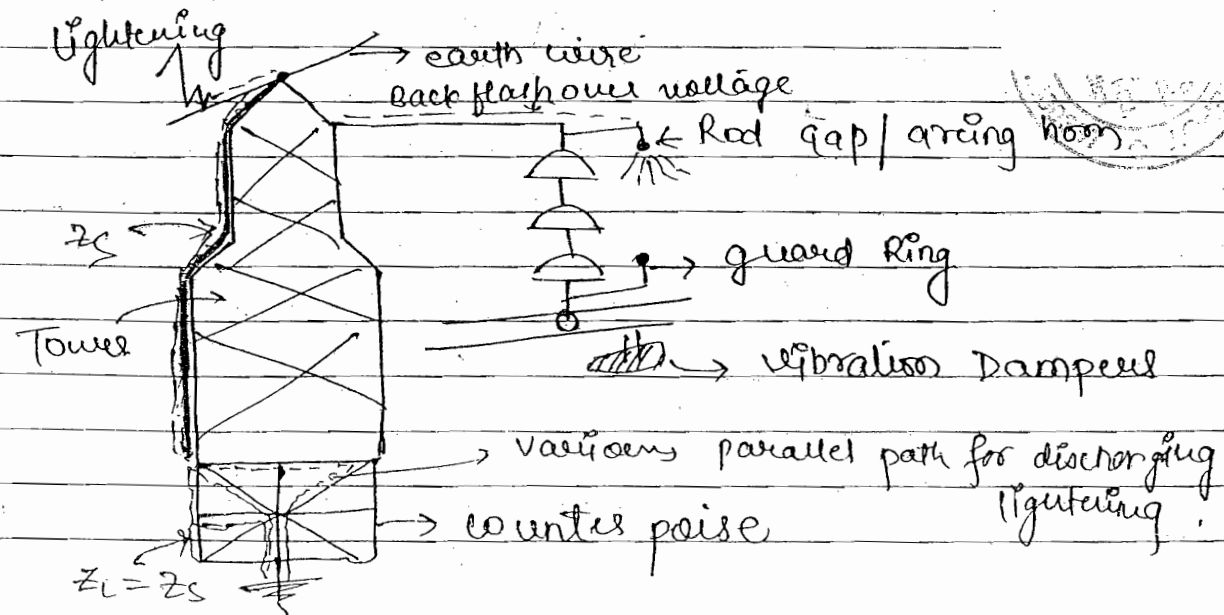
Q. 48 $SIL = \frac{V_s^2}{Z_L} \cdot \sqrt{\frac{C}{L}} = 800^2 \times \sqrt{\frac{11.68 \times 10^{-9}}{1.1 \times 10^{-3}}} = 2085 \text{ MW}$

Pg. No. 41, (33) $Z_L = 250 \Omega \quad V_s = 400 \text{ kV}$
 $V = 10 \times 250 = 2500 \text{ kV - Av.}$

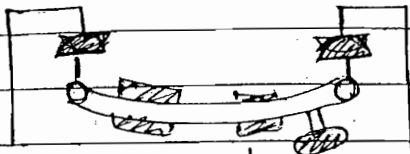
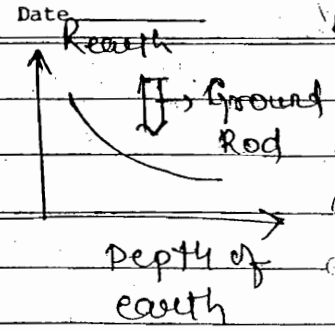


(36) (d) 1, 2 and 3

Pg. No. 95 $v = \frac{2\pi f l}{\sqrt{B \cdot X_L}} = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{0.201 \times 10^{-6} \times 196.2 \times 10^{-12}}} = 159.24 \text{ m/s.}$



- As the depth $\uparrow$ $Z \downarrow$ so use earth Rod
- guard Ring $\rightarrow$ for improving η , uniform voltage can maintain

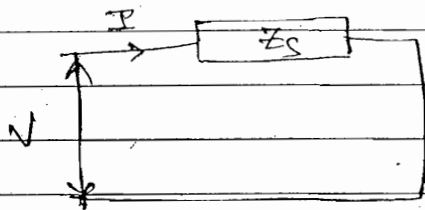


When snow will accumulated over the conductor

V or stock bridge which causes vibration because of non-uniform accumulation of snow. So we use vibration clamps for reducing the vibratⁿ.

- For protecting insulating disc from flash over voltage arcing horn are used which discharge the arc in air. And not pass to next one.

Case 3:- $Z_L = 0$



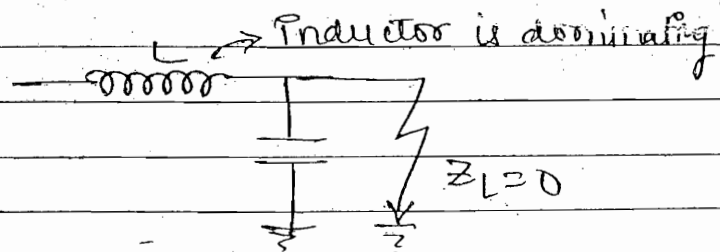
$$T_V = \frac{2Z_L}{Z_L + Z_s} = \frac{2(0)}{0 + Z_s} = 0$$

$$R_V = T_V - 1 = 0 - 1 = -1$$

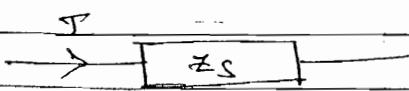
$$R_I = -R_V = +1$$

$$T_I = 1 + R_I = 1 + 1 = 2$$

$T_V = 0 \Rightarrow V'' = 0$
$T_I = 2 \Rightarrow I'' = 2I$
$R_V = -1 \Rightarrow V' = -V$
$R_I = 1 \Rightarrow I' = I$



Case 4:- $Z_L = \infty$



$$T_V = \frac{2Z_L}{Z_L \left[1 + \frac{Z_s}{Z_L} \right]} = \frac{2}{1 + \frac{Z_s}{\infty}} = \frac{2}{1 + 0} = 2$$

$$= \frac{2}{1 + 0} = 2$$

$$= 2$$

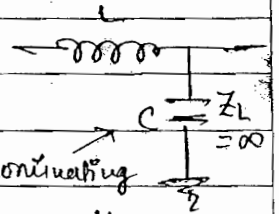
$$R_V = T_V - 1 = 2 - 1 = 1$$

$$T_I = 1 + R_I = 1 - 1$$

$$R_I = -R_V = -1$$

$$= 0$$

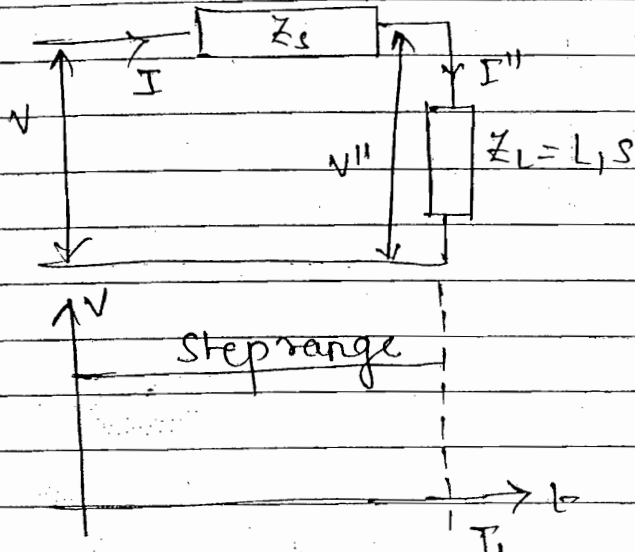
$$\boxed{\begin{array}{l} T_V = 2 \Rightarrow V'' = 2V, \quad T_I = 0 \Rightarrow I'' = 0 \\ R_V = 1 \Rightarrow V' = V, \quad R_I = -1 \Rightarrow I' = -I \end{array}}$$



- Counter poise is used at the bottom of the tower for discharging of lightning surge. It is containing parallel paths for effective discharging of lightning surges.
- In place of counter poise Ground rods can also be used which has thinner in diameter and higher length and used because earth resistance reduces as the depth of the earth increases.
- ~~Earths~~ Aring horn are used for protecting the insulating disc from the Back flash over voltage produce due to lightning surge.
- Guard Ring is used for maintaining uniform voltage in the disc so that string η is $\uparrow$
- Vibration dampers are used for protecting the reducing the vibrations only conductors which are produce due to non uniform ice loading.
- When $Z_L = 0$ Tr-line behaves as highly lagging N/W demanding for the lagging VAR's.
- When $Z_L = \infty$ Tr-line behaves as highly leading N/W demand. causes the receiving voltage to $\uparrow$

- If $Z_L = Z_S$ Tr-line has unity power factor.

Case 5 $Z_L = L_1 S$:-



Assume a step range

$$V(s) = V_S$$

$$V''(s) = \frac{2 Z_L \cdot V(s)}{Z_L + Z_S}$$

$$= \frac{2 L_1 S}{(L_1 S + Z_S)} \cdot V$$

$$V''(s) = \frac{2 V K_1}{K_1 \left[s + \frac{Z_S}{L_1} \right]}$$

$$V''(t) = L^{-1} [V''(s)]$$

$$= L^{-1} \left[\frac{2V}{s + \frac{Z_S}{L_1}} \right]$$

Time constant = $T = \frac{L_1}{Z_S}$

$Z_S = \text{Surge Imp. of line} = \sqrt{\frac{L}{C}}$

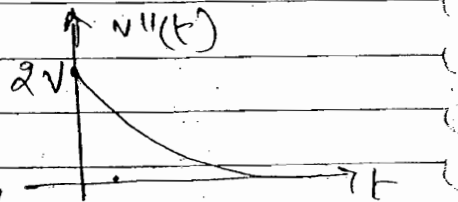
$L_1 = \text{load inductance}$

- (1) At $t = T_1 = 0 \Rightarrow$ instant at which step range surge touching $Z_L = L_1 S$

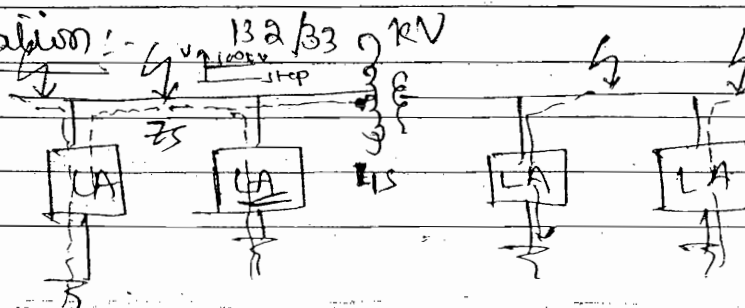
$$V''(t) = 2V e^{-0} = 2V$$

- (2) At $t = \infty$

$$V''(t) = 2V \cdot e^{-\infty} = 0$$



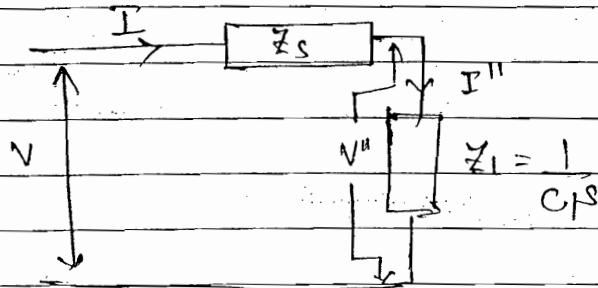
Application:-



- When L.A is not present and lightning of 100kV surge is occur, it will hit the x-mel wdg. X-mel has inductive behaves as load of L/S . (Voltage will rise up) X-mel has insulatⁿ protectⁿ upto $132 \text{ kV} + 10\%$, and the surge is of $2 \times 100 \text{ kV} = 200 \text{ kV}$, ^{than exp. d} damage x-mel. so we kept LA on both side of x-mel.

Case 6:- $Z_L = \frac{1}{C_1 S}$

Assume step surge
 $V(s) = V/s$



$$V''(s) = \frac{2Z_L}{(Z_L + Z_s)} \cdot V(s)$$

$$= \frac{2 \cdot \frac{1}{C_1 S}}{\left(\frac{1}{C_1 S} + Z_s\right)} \cdot \frac{V}{s}$$

step surge

$$V''(s) = \frac{2V}{s(1 + sC_1 Z_s)}$$

$$V''(t) = \mathcal{L}^{-1}[V''(s)]$$

$$= \mathcal{L}^{-1}\left[\frac{2V}{s(1 + sC_1 Z_s)}\right]$$

Time constant $T = C_1 Z_s$

$Z_s = \text{Surge Imp. of line} = \sqrt{\frac{L}{C}}$

$C_1 = \text{load capacitance}$

$$V''(t) = 2V \left[1 - e^{-t/C_1 Z_s}\right]$$

- ① At $t = T_1 = 0 \Rightarrow$ instant at which step surge reaching
 $Z_L = 1/C_1 S$

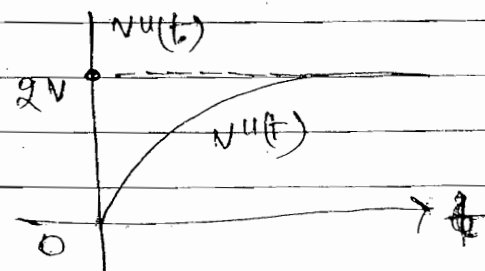
$$V''(t) = 2V(1 - e^{-0}) = 0$$

- ② At $t = \infty$

$$V''(t) = 2V(1 - e^{-\infty}) = 2V$$

- No protecting device used.

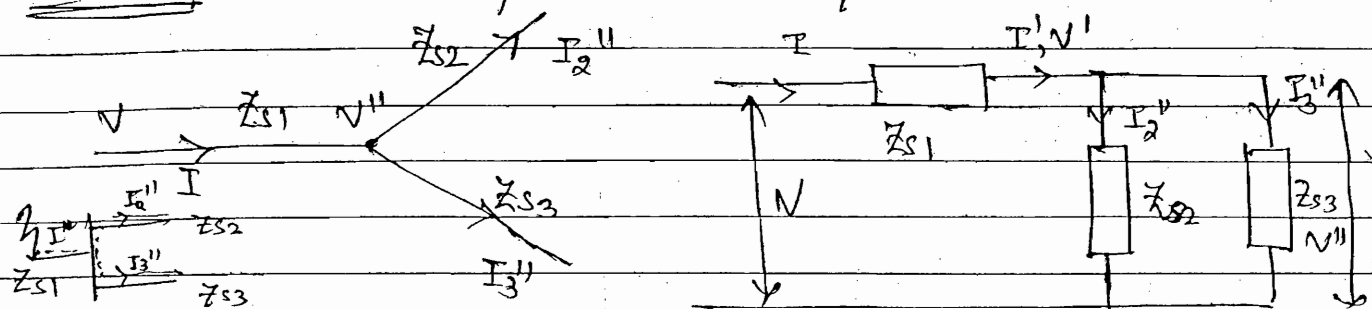
because $V > 0$ at $t = 0$



for
Conventional
Imp

Date _____

Case 7:- Z_1 = parallel lines / T Junction :-



For parallel voltage is equal.

$$V'' = V + V'$$

$$V' = V'' - V \quad \text{--- (1)}$$

$$I'' = I_2'' + I_3'' = I + I'$$

$$\frac{V''}{Z_{s2}} + \frac{V''}{Z_{s3}} = \frac{V}{Z_{s1}} - \frac{V'}{Z_{s1}} \quad \text{--- (2)}$$

Substitute (1) in (2).

$$V'' \left[\frac{1}{Z_{s2}} + \frac{1}{Z_{s3}} \right] = \frac{V}{Z_{s1}} - \frac{V'' - V}{Z_{s1}}$$

$$V'' \left[\frac{1}{Z_{s1}} + \frac{1}{Z_{s2}} + \frac{1}{Z_{s3}} \right] = \frac{2V}{Z_{s1}}$$

$$T_V = \frac{V''}{V} = \frac{2/Z_{s1}}{\left(\frac{1}{Z_{s1}} + \frac{1}{Z_{s2}} + \frac{1}{Z_{s3}} \right)}$$

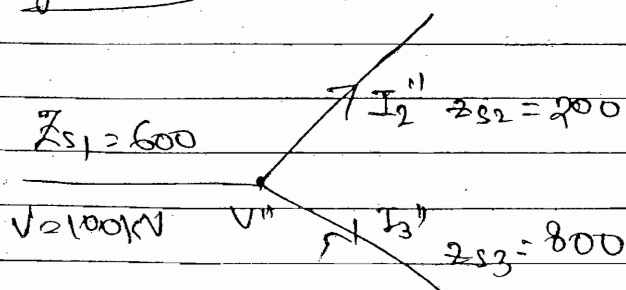
$$R_V = \frac{V'}{V} = T_V - 1, \quad R_I = \frac{I'}{I} = -R_V$$

$$T_{I_2} = \frac{I_2''}{I} = \frac{V''/Z_{s2}}{V/Z_{s1}}, \quad T_{I_3} = \frac{I_3''}{I} = \frac{V''/Z_{s3}}{V/Z_{s1}}$$

$$= T_V \frac{Z_{s1}}{Z_{s2}}$$

$$= T_V \frac{Z_{s1}}{Z_{s3}}$$

Page No. 45 Q.9



$$T_V = \frac{V''}{V} = \frac{2/Z_{s1}}{\left(\frac{1}{Z_{s1}} + \frac{1}{Z_{s2}} + \frac{1}{Z_{s3}} \right)}$$

$$V'' = 42.1 \text{ kV}$$

$$I_2'' = \frac{V''}{Z_{s2}} = \frac{42.1 \times 10^3}{200}$$

$$= 0.210 \text{ kA}$$

$$I_2'' = \frac{V''}{Z_{S3}} = \frac{42.11 \text{ kV}}{800} = 52.5 \text{ A}$$

Page No 41 (34) $V = 20 \text{ kV}$ $L =$

$$L_1 = 0.4 \times 10^{-3}$$

$$C_1 = 0.5 \times 10^{-6}$$

cable

$$Z_{S1} = \sqrt{\frac{L_1}{C_1}}$$

$$= 28.28$$

$$V'' = 2 \times 20$$

$$= 33.93 \text{ kV}$$

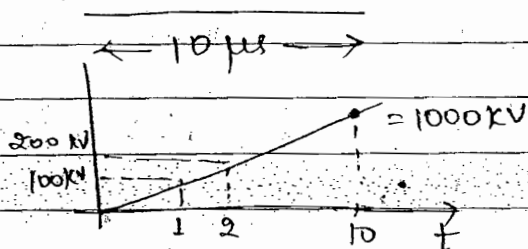
$$28.28 \sqrt{\frac{1}{28.28} + \frac{1}{316.2} + \frac{1}{316.2}}$$

(32)

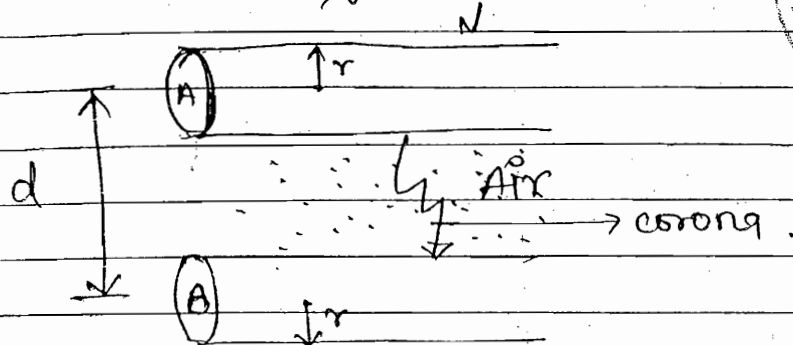
$$Z_L = \infty$$

$$V' = V = 1000$$

$$(c) 1000 \text{ kV} / \mu\text{s}$$



CORONA:-



$$g = 21 \text{ KV/cm (RMS)}$$

Peek Empirical
Name of Scientist.

- Corona is self electrical discharge of atmospheric air.
- If the operating voltage is b/w the conductor is more than dielectric strength of atmospheric air. The air molecules get ionised and initiate corona.
- The corona is form ozone gas is released.
- Critical Disruptive voltage: V_c :- The voltage at which corona is just initiated is called V_c . The sound can be heard at this voltage.

$$V_c = m g r \delta \ln \left(\frac{d}{r} \right) \text{ KV/phase (RMS)}$$

m = Surface factor

= 0.8 - 0.9 for ACSR / Rough Conductor

= 0.9 - 1 for Hollow / smooth Conductor

g = Dielectric strength of air = 21 KV/cm (RMS)

r = Radius of conductor in cm.

d = Distance between conductors in cm.

δ = Air density factor

$$= \frac{3.92 b}{(273 + T)}$$

b = barometric pressure of air in cm of Hg

T = Atm. Temp. °C.

- Critical Visual Voltage: - V_v :- The voltage at which corona is visible with violet or blue colour is called V_v .

$$V_v = mg \gamma \delta \left(1 + \frac{0.3}{\sqrt{r \delta}} \right) \ln \frac{d}{r} \quad \text{KV/phase (RMS)}$$

- Power loss Due to Corona: If Corona is form power loss will occur which is given by Peck empirical formula.

$$P_L = 241 \times 10^{-5} \left(\frac{f + 25}{\delta} \right) \sqrt{\frac{r}{d}} (V_{ph} - V_c)^2$$

$$P \propto (f + 25) \quad \dots \text{KW/km/phase}$$

V_{ph} = Tr-line voltage / phase

V_c = Critical Disruptive Voltage

NOTE: - (i) If $V_{ph} > V_c$ CORONA OCCURS

$$P_L \neq 0$$

(ii) If $V_{ph} \leq V_c$ NO CORONA

$$P_L = 0$$

Q 1- ϕ Tr-line with conductor $A = 0.5 \text{ cm}$ distance b/w conductor is 40 cm operating at voltage of 30 kV
Calculate (1) V_c Assume $m = \delta = 1$

(2) Power loss at 50 Hz

Solution

$$A = \pi r^2$$

$$0.5 = \pi r^2$$

$$r^2 = \frac{0.5}{\pi}$$

$$r = 0.39$$

$$V_c = 1 \times 21 \times 0.5 \times 1 \times \ln \frac{40}{0.5}$$

$$= 46.011 \text{ KV/phase}$$

② $V_{pm} = 30KV < V_c \Rightarrow$ No corona loss
 $\therefore P_L \neq 0$

Factors affecting Corona and Methods of Reducing

- (1) Higher value of V_c preferred so that corona does not occur and $P_L = 0$
- (2) $V_c \propto m$, m is higher for hollow and smooth conductor so that corona is less compare to ACSR or rough conductor
- (3) $V_c \propto r$, Bundle conductor radius $\uparrow$, $V_c \uparrow$.
By using Bundle conductor effective radius of conductor is $\uparrow$ so that corona is minimised.
- (4) At higher V_c , $P_L = 0$ and hence do not consider $P_L \propto \sqrt{r}$
- (5) $V_c \propto \delta \propto b$. In hill areas b is smaller so that corona is more frequent compare to plain areas.
 $b \rightarrow$ pressure
 $b \uparrow$ in hilly areas
- (6) As the operating voltage $\uparrow$, distance b/w conductor are $\uparrow$ (d), for maintaining higher V_c because $V_c \propto \ln d$
- (7) By $\uparrow$ height of tower corona is reduced. (capac $\uparrow$ if height is less, $X_L \uparrow$ Over voltage cause, and greater than V_c , corona starts.)
- (8) By using transposition corona is reduce
- (9) $P_L \propto (f+25)$, Corona power less is more in HVAC compare to HVDC.

Disadvantages:-

- (1) Power loss occurs
- (2) Produces interference to other lines
- (3) ~~the~~ charging current $\uparrow$

Advantage :-

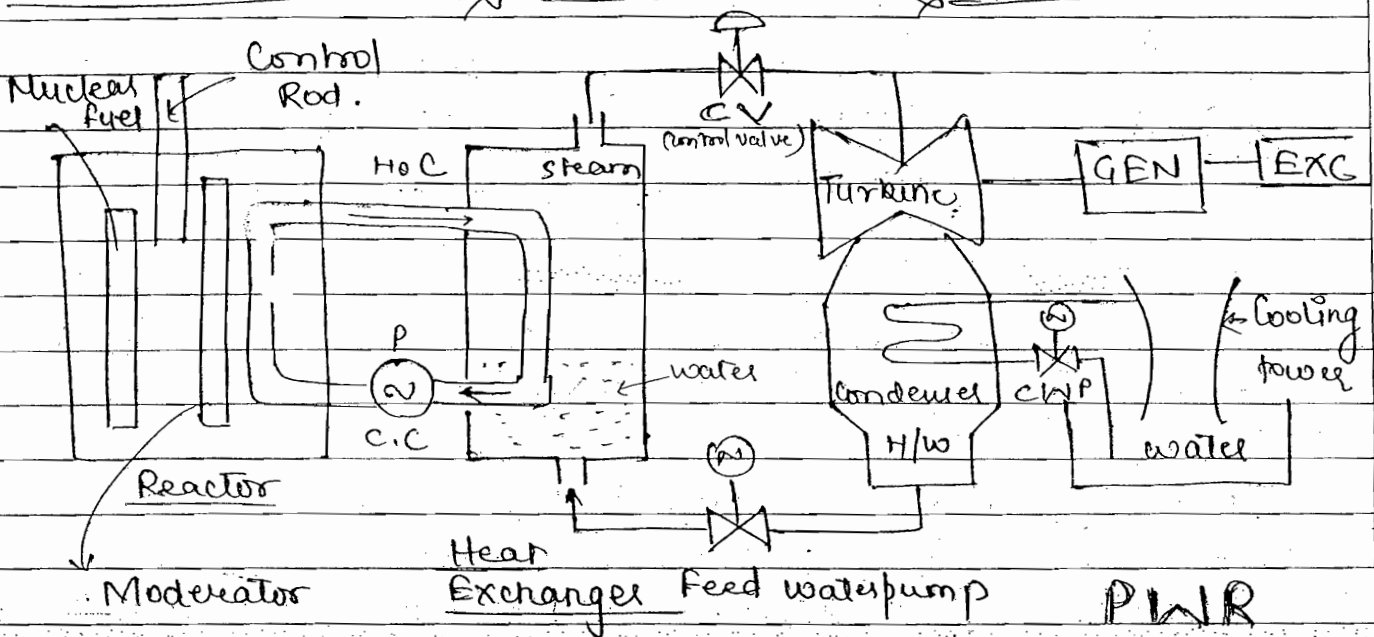
- (1) Intensity or peak voltage of lightning surge is reduce if lightning surge initial corona.
(lightening $u > V_c$, start corona, & change into corona)
so peak value of lightning of surge is ↓).

Hydro Power Plant

- **Surge Tank**: - It is used in the medium and high head hydro power stations. It is mainly used for protection of penstock from the water hammering effect.
→ It is used to supply water to the turbine in case of emergency load demands.
- **Spill way**: - It is used as a safety valve for the hydro station for protection of hydro plant from the excess water due to heavy rain. This water is diverted using spillway.
- **Trash Rack**: - It is used for collecting waste materials from the water so that turbine blades are protected.
- **Hydro graph**: - It is a graph b/w discharge of a water (land) tank. By using this hydro graph the power generated by the plant can be predicted so that scheduling of the maintenance for the hydro & thermal & nuclear are programmed.
- **Pumped Storage plant**: - It is one of the type of hydro plant containing two tanks i.e. down stream and upstream tanks during peak load demand water flows from upstream to downstream through the turbine for supplying peak load demand.
→ During off peak load time water will reserise from downstream to upstream. during this time turbine is working as pump and gen. working as Motor. Taking the power from other parallel generator.

Advantages of Pumped Storage:-

- (1) Most economical as a peak load supply plant
- (2) Used as load frequency control unit.
- (3) If it is combine with thermal plants, plant load factor is increased.
- (4) Pollution free
- (5) Easily adaptable for remote control operation.



Nuclear Power Plant (Layout)

CC → Cold Coolant HC → Hot Coolant P = pump

	BWR	PWR	CANDU	Liquid Na	FBK
Fuel	Enriched	Enriched	Natural	Enriched	Enriched
Coolant	Water	Water	Heavy water	liquid Na	liquid Na
Moderator	Water	Water	Heavy water	Graphite	—
Control Rod	Cadmium	Cadmium	—	Boron	Water

enriched → fuel → 99% USA

natural → fuel → 0.07% India

BWR = Boiling water Reactor	Enriched:
PWR = Pressurised water Reactor	U_{92}^{238}
CANDU = Canadian Deuterium Uranium	Natural:
FR = Fast Breeder Reactor	U_{92}^{235}



• Principle: - Nuclear Fission.

- Mostly use CANDU, PWR.
- Liquid Na, FR → laboratory purpose.
- Pressure is less than thermal p.p. But flow rate is high.
- Moderator → Ordinary water → to moderate control the speed of neutron.

BWR: - In BWR ⇒ we don't use the Heat exchanger. Water is directly goes to Reactor where it will change into steam. This steam will send to turbine.

PWR.

Working: - When fuel get hot, (after fission), its hotness is collected by the cold coolant, which is circulated through pump. Cold coolant get converted into hot coolant, Heat exchanger having the water, the heat of hot coolant transfer to water. Water will convert into steam. This steam will sent to turbine.

Remaining steam will condense and convert into water again. This water is again used in heat exchanger for converting into steam.

disadvantage

- If feed water pump get damage: - (for BWR), water level will goes down, its Moderator and control Rod also not working, then neutron produce heat extreme high, which Burst the Reactor.

ex: - Happened in Japan 4 out of 6 → Burst.

Reproduction and Multiplication Factor:- (K)

$$K = \frac{\text{NO. of Neutrons released in present cycle}}{\text{NO. of Neutrons released in previous cycle}}$$

$K = 1 \Rightarrow$ Constant power O/p

$K > 1 \Rightarrow$ Increased power O/p.

$K < 1 \Rightarrow$ Decreased power O/p

practical value of K is just higher than 1

ex:- 09:00 - 100 MW - 100 Neutron -

10:00 - 100 MW - 100 Neutron - $K = \frac{100}{100} = 1$

11:00 - 120 MW - 120 Neutron - $K = \frac{120}{100} = 1.2 > 1$

18:00 - 80 MW - 80 Neutron - $K = \frac{80}{120} = \frac{80}{120} < 1$

- In nuclear reactor heat is produced due to nuclear fission chain reaction.
- This heat is absorbed by coolant which is used to convert water into steam in heat exchanger. This steam admitting into turbine for producing power generation.
- The amount of heat released is depending on velocity of neutron and NO. of Neutrons released.
- Moderator is used for moderating the speed of the neutron. The molecular weight of the moderator is to be minimum.
- Ordinary water is used as moderator in the enriched uranium plants.
- Control Rod: It is used for absorbing excess neutrons released during Nuclear fission chain reaction.

Load Frequency Control

Date _____

Rated value of freq. = 50 Hz.

Range: Ideal: $50 \pm 1\%$ (49.5 - 50.5 Hz)

: Practical: $50 \pm 2\%$ (48.5 - 51.5 Hz)

Disadvantages of frequency variation:-

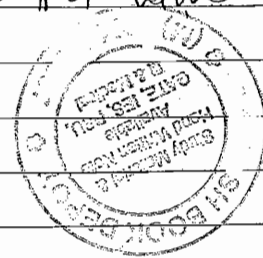
- (1) For maintaining constant voltage, at low freq. the ϕ to the x-mei core has to be increased. This will increase the causes saturation of the x-mei core.
- (2) All the electrical Motor speeds are, freq. dependent. By changing the frequency, the performance of electrical motor are effected.
- (3) Due to core saturation of C.T. at low frequency, relays produces trip signals without any fault.
- (4) PA, FD and ID fans are runned by induction Motor. If the freq. changes the performance will be effected. so that thermal efficiency is effected.
- (5) The turbine blades are damaged at higher frequency & speed. [at low speed blades will compress and at high speed blades will come out due to centrifugal force]

• Method of Frequency Control:-

- (1) Primary control:- Speed governing control valve
- (2) Secondary control:-
 - (A) Pumped storage plant
 - (B) Load regulation.

≡ Speed Governing Control Valve:-

Diagram in Next page.

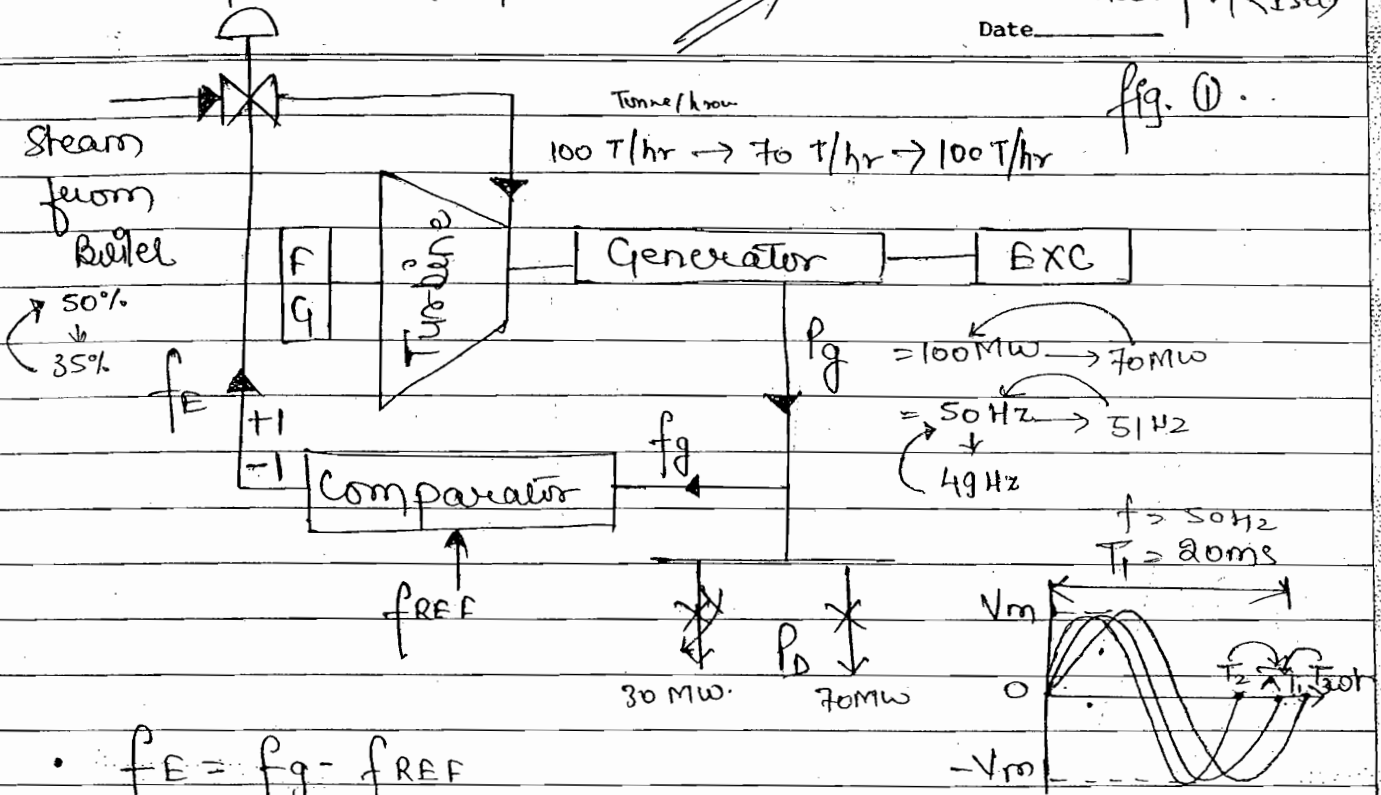


Govn. Valve (HP/IPCV)

this process take some time delay. ($< 1 \text{ sec}$)

Date _____

fig. ①.



$$f_E = f_g - f_{REF}$$

- ① If $f_g = f_{REF} \Rightarrow f_E = 0 \Rightarrow$ Constant opening position of Govn. Val
- ② If $f_g > f_{REF} \Rightarrow f_E > 0 \Rightarrow$ close valve until $E = 0$
- ③ If $f_g < f_{REF} \Rightarrow f_E < 0 \Rightarrow$ open valve until $E = 0$

Internal Structure of Govn. Valve

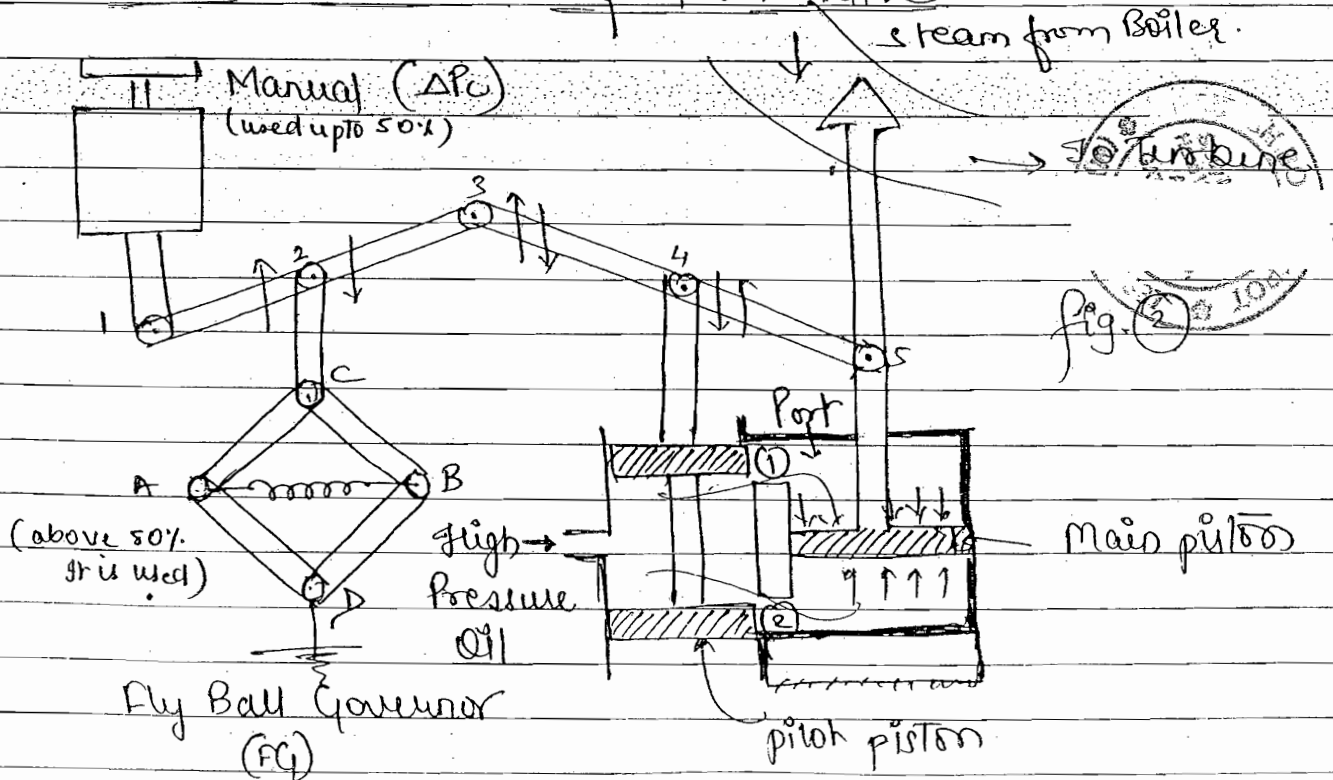
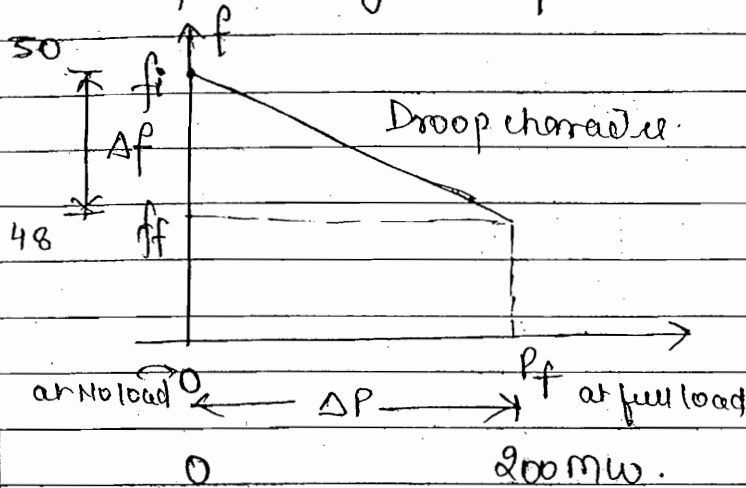


fig. ②

practically freq. at No. load $\Rightarrow > 50 \text{ Hz}$.

Date _____

Speed Regulation Parameter



$$R = - \frac{\Delta f}{\Delta P} \quad \text{Hz/MW}$$

$$\text{Ex: } R = - \frac{(50 - 48)}{(200 - 0)} = -1 \text{ Hz/mw}$$

$$= -0.01 \text{ Hz/mw}$$

$$\frac{\Delta f_2}{\Delta P_2} = \frac{\Delta f_1}{\Delta P_1}$$

Speed Regulation Constant:

$$\Delta f \rightarrow \%$$

$$f_i - f_f \Rightarrow \Delta f$$

$$\frac{f_i - f_f}{f_i} \Rightarrow \frac{\Delta f}{f_i} \%$$

Ex: 4% of Speed Regulation
or (0.04 pu)

$$\frac{\Delta f}{50} = 4\% \Rightarrow \Delta f = 2 \text{ Hz}$$

Ques. that like for 2MW How much freq. will added...

Q A 200 MVA turbo gen. have speed regy. of 8%. How much of turbine slip has to be ↑ for steady state operating for freq. drop of 0.05 Hz.

Solve

$$R = 8\% = 0.08$$

$$\frac{f_2}{P_2} = \frac{f_1}{P_1} \Rightarrow 0.085$$

$$|R| = + \frac{\Delta f}{\Delta P} = \frac{8\% \text{ of } 50}{200} = \frac{4}{200} \text{ Hz/mw}$$

$$\frac{\Delta f_2}{\Delta P_2} = \frac{\Delta f_1}{\Delta P_1}$$

$$\frac{0.05}{\Delta P_2} = \frac{4}{200}$$

$$\Delta P_2 = \frac{200 \times 5}{100 \times 4} = 2.5 \text{ mw}$$

fig. ① Explanation:- Suppose the generated power $P_g = 100 \text{ MW}$ and demand is also 100 MW , for this 100 Tonne/hour coal is required for which 50% valve is opened (freq. 50 Hz time period of 1 cycle is $T_1 = 20 \text{ ms}$).

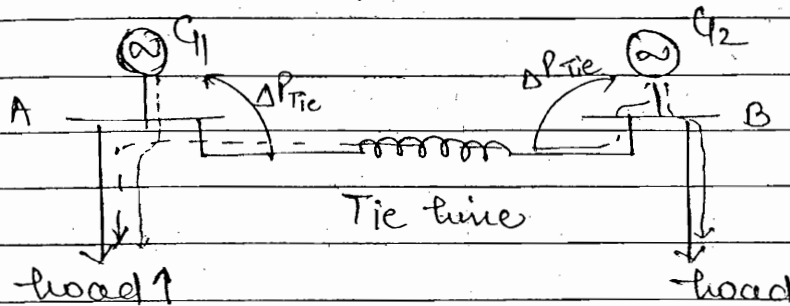
- Suppose CB of 30 MW get opened due to fault. $P_D > P_g$ and $P_g = 100 \text{ MW}$, rotor speed get high $K.E. \propto \omega^2$ because of which freq get $\uparrow$ 51 Hz . Comparator will generate of an error of $+1$, which send to govn. valve. It will close the valve upto 35% , Now coal requirement will be 70 T/hr . [51 Hz set to again 50 Hz]
- Suppose CB. of 30 MW get closed, Now $P_D = 100 \text{ MW}$ But $P_g = 70 \text{ MW}$, Rotor speed get $\downarrow$ due to which freq. will $\downarrow$ and become 49 Hz , $T_3 = \frac{1}{f} = \text{more than}$

$T_1 = 20 \text{ ms}$. Comparator will generate error of -1 and send signal to govn. valve. It will open the valve, Now coal requirement $\uparrow$, $70 \text{ T/hr} \rightarrow 100 \text{ T/hr}$ freq. will again set to $49 \text{ Hz} \rightarrow 50 \text{ Hz}$. So maintain the freq.

fig ② Explanation:-

- for $\downarrow$ in demand, FG will expand. pull c down, 2 $\downarrow$, 3 $\uparrow$, 4 $\downarrow$, high pressure oil will enter through ② gate and close the valve.
- for $\uparrow$ in demand, FG will compressed push c upward, 2 $\uparrow$, 3 $\downarrow$, 4 $\uparrow$, oil will enter through ① gate and open the valve.

• Area frequency Control :-



- (1) Flat frequency control
- (2) Flat Tie line / Tie Bias Control
- (3) Parallel frequency control.

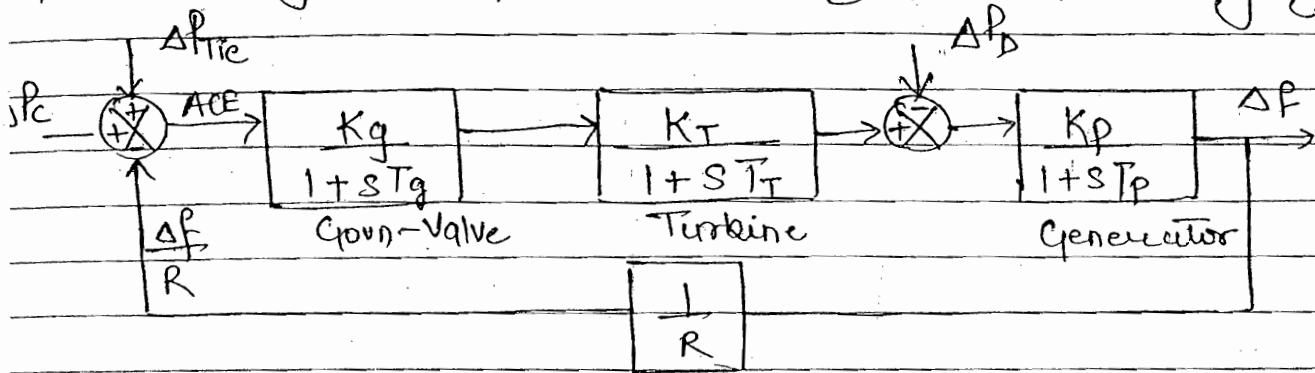
• Area freq. control is used to maintain constant frequency for an inter connected grid sys. containing more generators connected in parallel.

(1) Flat frequency control: - load changes of Bus Bas A is supplied by the generator G_2 for maintaining constant frequency. In this method the Tie line may be over loaded.

(2) Flat Tie line / Tie Bias Control: - load changes of Bus Bas A or B supplied by G_1 and G_2 without over loading of the tie-line so that the control signal is proportional to changes in the Tie line power and frequency.

(3) Parallel freq. Control: - load changes of Bus Bas A or B is supplied simultaneously by both the generators without overloading for maintaining constant freq. this method is most practically used in Area freq. control.

Block Diagram Representation of Speed Governing System



ACE = Area Control Error

$$= \Delta P_c + \Delta P_{tie} - \Delta f/R$$

For auto control $\Delta P_c = \text{constant}$

Bias Coefficient $= b = -\frac{1}{R}$

$$ACE = \Delta P_{tie} + b \cdot \Delta f$$

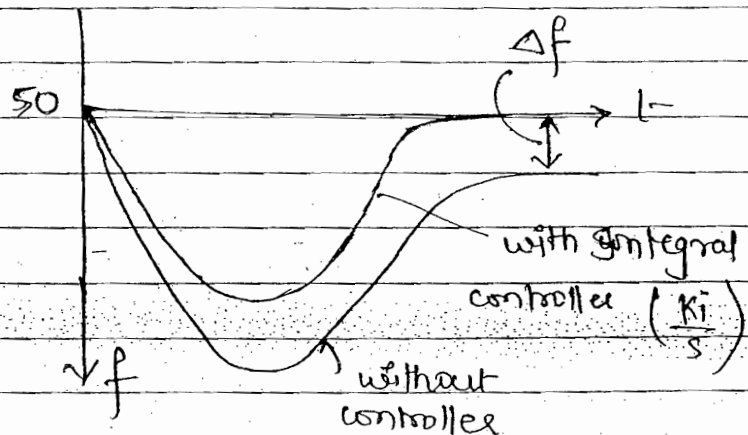
Time Constants: T_p, T_g, T_T
Gain Constants: K_p, K_g, K_T

$$T_p = 0.1 - 0.2 \text{ sec}$$

$$T_T = 0.1 - 0.3 \text{ sec}$$

$$T_g = 0.1 - 0.2 \text{ sec}$$

Δf = steady state freq. deviation / drop



- Integral controller eliminates steady state freq. drop

Steady state freq. Drop (Δf): -

$$\Delta f = (f_N - f_i)$$

① Isolated Generator

(a) Sudden load Demand: - (ΔP_D)

$$f_N = f_i \left[\frac{H \cdot s - (\Delta P_D) T_d}{H \cdot s} \right]^{1/2}$$

(b) Sudden load loss (ΔP_D) (Trip of load)

$$f_N = f_i \left[\frac{H \cdot s + (\Delta P_D) \cdot T_d}{H \cdot s} \right]^{1/2}$$

H = Inertia constant of Gen. MW Sec/MVA.

s = Rating of Generator in MVA.

ΔP_D = Load / Power Demand in MW.

T_d = Time Delay in Govn. Sys. in Sec.

f_N = New frequency

f_i = Initial frequency.

(2) Area Control: -

$$\Delta f = - \frac{\Delta P_D}{(\beta + 1/R)}$$

β = $\frac{\text{Rated value} \times \% \text{ change in power}}{\text{Rated freq} \times \% \text{ change in frequency}}$

R = Speed Reg. parameter in Hz/MW

ΔP_D = -ve for load loss

= +ve for load Demand.

Q An interconnected pow sys. N/W. At the pow of 1500 MW at 50 Hz. The freq. is changing 2.5% for a load change of 1.5%. Calculate the steady state freq. drop of a 200 MW of industrial load is trip. Assumed $R = 0.005$ Hz/MW

Solution:
$$\Delta f_D = - \frac{-200}{\frac{1500 \times 1.5}{50 \times \frac{2.5}{100}} + \frac{1}{0.005}} = \frac{200}{\frac{225}{10} + \frac{1000}{5}}$$

$$\Delta f = 0.917 \text{ Hz.}$$

$$f_N - f_i = 0.917$$

$$f_N - 50 = 0.917$$

$$f_N = 50.917 \text{ Hz}$$

Q 200 MVA 50 Hz Turbo gen. is operating at No load if a load of 70 MW is applied at the terminals of generator. Calculate

(1) Steady state freq. drop

(2) New freq. due To time delay of gov. sys. of 0.5 sec. Assume. Inertia Const. of the generator is 4 MW Sec / MVA

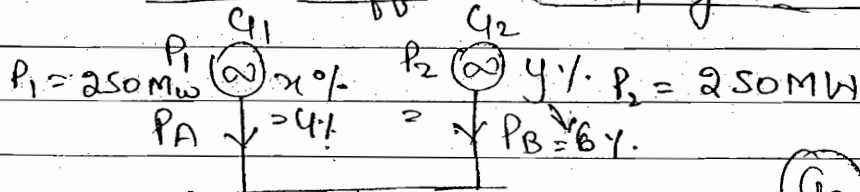
Solution: $f_N = \left[\frac{4 \times 200 + 70 \times 0.5}{4 \times 200} \right]^{1/2} \times 50$

$$= 48.89 \text{ Hz}$$

$$\Delta f = 50 - 48.89 = 1.11 \text{ Hz}$$

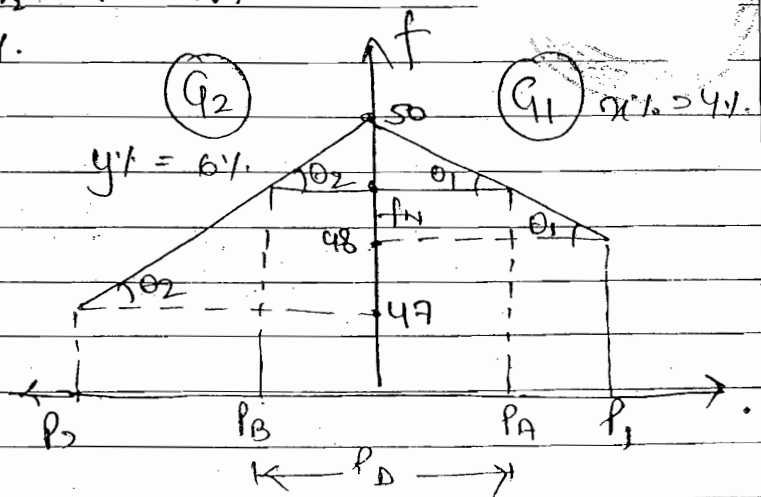
• Load Sharing of Parallel Generator

(1) With different Drooping Characteristic:



$$P_A + P_B = P_D = 400$$

$$P_D = 400$$



G₁

$$\tan \theta_1 = \frac{50 - f_N}{P_A} = \frac{50 - 48}{250} = \frac{1}{125}$$

— (1)

$$\Rightarrow P_A + P_B = 400 \text{ given}$$

$$P_B = 400 - P_A$$

Put in eqn (2).

G₂

$$\tan \theta_2 = \frac{50 - f_N}{P_B} = \frac{50 - 48}{250} = \frac{2}{250}$$

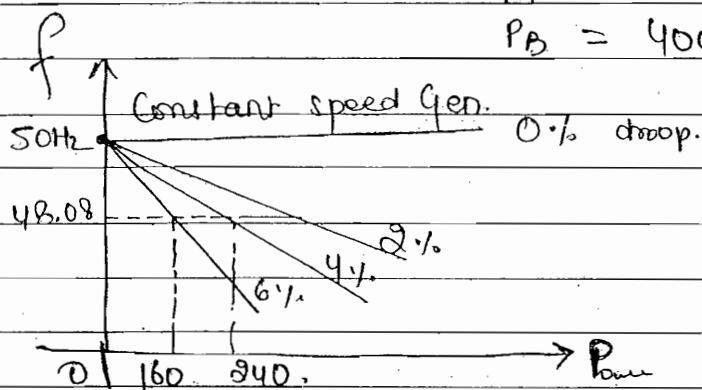
— (2)

$$\frac{50 - f_N}{400 - P_A} = \frac{2}{250} \quad (3)$$

Solve (1) & (3) $f_N = 48.08 \text{ Hz}$

$$P_A = 240 \text{ MW}$$

$$P_B = 400 - P_A = 400 - 240 = 160 \text{ MW}$$



- In parallel operation generators, the generator with lowest % of droop character. will share Maximum load
- If a 0% or Constant Speed Gen. is connected in parallel to the other generators with 2, 4, 6% droop character then 0% generator can supply entire load changes with loading other generator. This is an ideal generator.

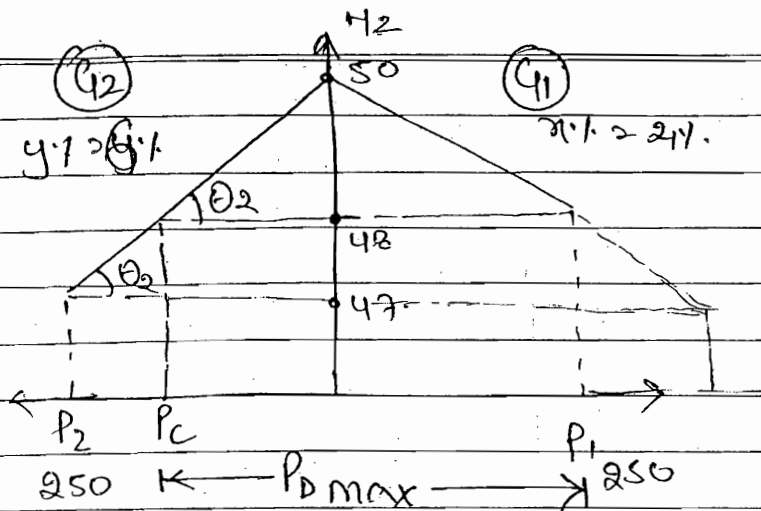
Case

Maximum load supply by gen. without overloading

$$G_1 \quad 2\% > 4\% \quad P_1 = 250 \text{ MW}$$

$$G_2 \quad 9\% > 6\% \quad P_2 = 250 \text{ MW}$$

$$P_{\max} = P_A + P_B = ?$$



$$\tan \theta_2 = \frac{50 - 48}{P_c} = \frac{50 - 47}{250}$$

$$P_c = 166.66 \text{ MW}$$

$$P_{Dmax} = P_1 + P_c = 250 + 166.6$$

$$P_{Dmax} = 416.66 \text{ MW}$$

$$f_N = 48 \text{ Hz}$$

∴ If operate at 47 Hz freq. P_1 delivers more than 250
 ∴ we can't take this condition.

∵ Because of different drooping characteristic. Generators
 are not able of loaded to the maximum full
 load capacity.

∵ The lowest drooping character is loaded to full load
 capacity.

② Both Generator has same droop characteristic.

$$P_1 = 250 \text{ MW} \quad G_1 \quad 4\% \text{ droop}$$

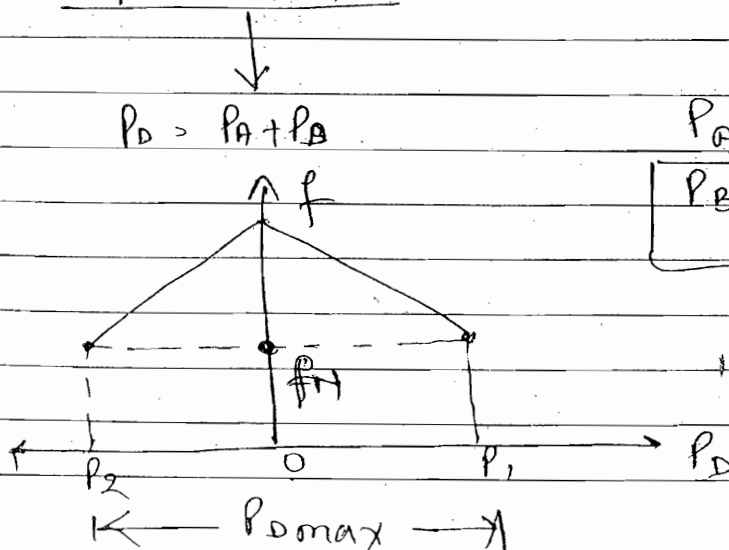
$$P_2 = 250 \text{ MW} \quad G_2 \quad 4\% \text{ droop}$$

$$P_A = \frac{P_1 \times P_D}{P_1 + P_2}$$

$$= \frac{250 \times 500}{250 + 250}$$

$$P_A = 200 \text{ MW}$$

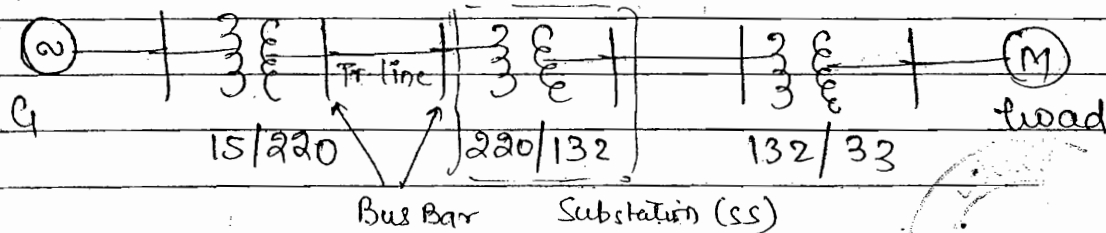
$$P_B = \frac{P_2 \times P_D}{P_1 + P_2} = 200 \text{ MW}$$



- If both generator have equal droop character can supply the load demand as per their capacity. proportionately.
- Maximum demand = Sum of their individual full load capacity.

30/10/14

Protection And Switchgear



→ shown only for R phase (Next page fig).

→ We have to protect $\Rightarrow$ low X-mes 220/132 KV, 220 KV Bus Bar, 132 KV Bus Bar.

→ (1) Identification of fault (2) Isolation of fault from healthy part.

→ Tr-line $\rightarrow$ SF6, Distributⁿ $\rightarrow$ Vacuum CB.

• Lock out condition :- CB do not operate, even fault is present. Bcoz pressure (sufficient) is not present, if open CB get Blast.

→ ex - R₂ (operate for fault occur across R₁)

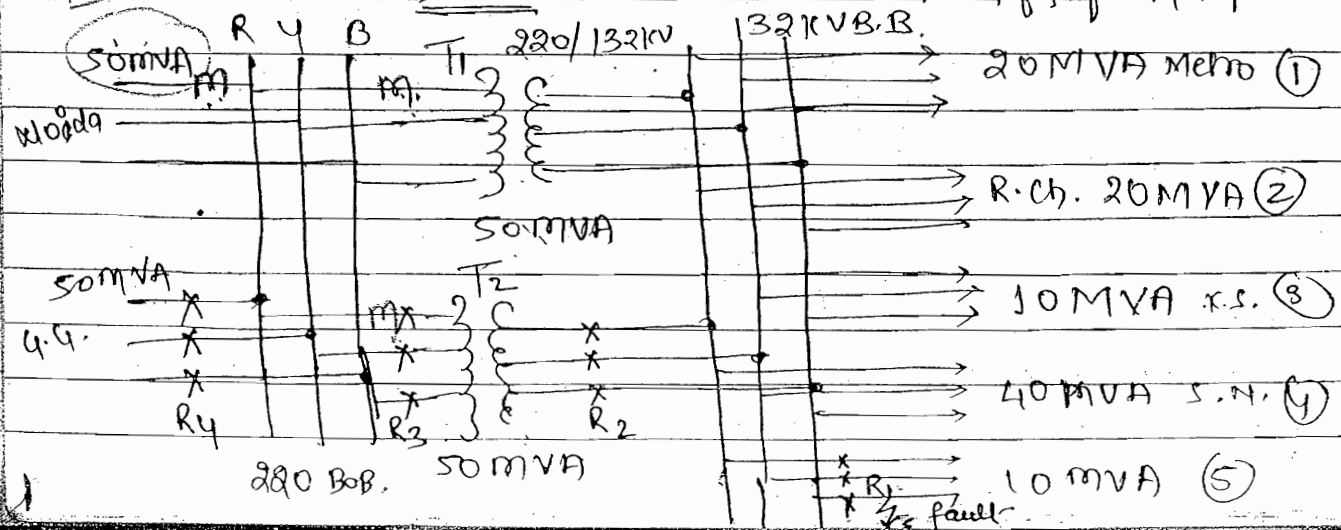
• Non-unit Protection: Identify the fault not only its own unit (area) But also outside. (also called Backup protection)

• Unit Protection: - ex: Buchholz Relay. which operate only in specified area.

• 100

Delhi

If R₁ get failed R₂ will operate, if R₂ $\rightarrow$ fail, R₃ operate, if R₃ $\rightarrow$ fail R₄ $\rightarrow$ operate.



• Suppose (G.G.) generator fail, then gen. is 50 MVA and demand is 100 MVA, then area (3) and (4) are disconnected, [G₂ is fail due to fail of Relay R₁]

Date _____

• Power Sys N/W consisting of generators, x-mei, Bus Bars, x-line and electrical Motors etc. These equipments are to be protected from the abnormal condition like short circuit, open circuit, faults and lightning surges.

• Non-Unit Protection: - The protecting equip. like Relays, CB etc are operating for the faults within in own zone and also in the other zone equipment and faults is known as N.U.P. ex: - overcurrent and distances relays.

• Unit Protection: - The protecting equipments are operating within for the fault within some physical space with in or equipments is called U.P.
ex: - Differential Relay or Buchholz Relay.

• LA: The first and last protecting device of the substation is LA used for diverting the lightning surges occur outside the substation.

⇒ Two more LA are kept on both side of pow-x-mei for discharging the surges occur within the substation.

⇒ LA are made of metal oxides like - Zinc oxide, silicon carbide (SiC) which offer low resistance for the lightning surges and high resistance for Normal voltage.

⇒ LA have impulse ratio of unity

Impulse Ratio = $\frac{\text{Mag. of lightning surge with high freq.}}{\text{Mag. of lightning surge with low freq.}}$

→ P.O.T → only in Bus Bar

→ CVT → each feeder.

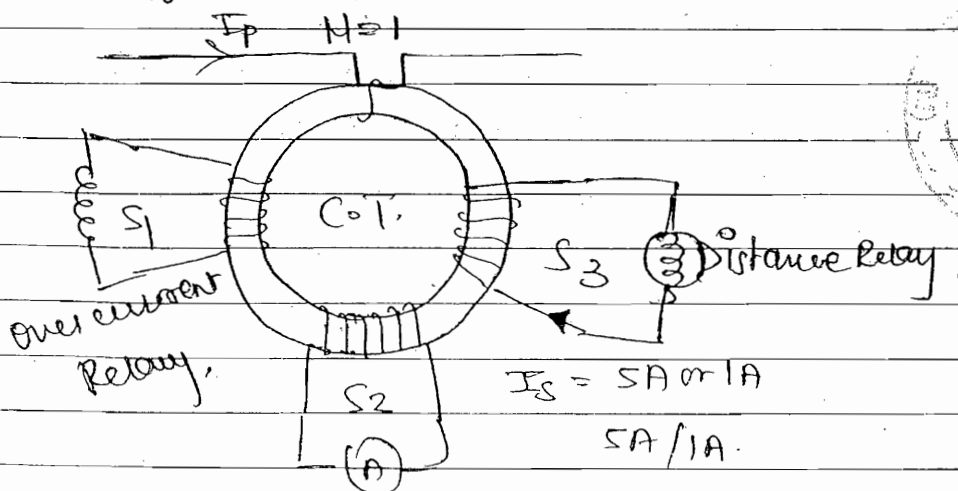
- CVT: It is working on principle of capacitance using for Reducing the high voltage of 220 kV/132 kV etc. to a low voltage the standard low voltage is of 110V. It provides voltage signal for

- (i) Voltmeter
- (ii) Wattmeter and energy meter
- (iii) Distance and directional Relay.

Each phase has one CVT. The cost of CVT is less than compare to PT.

- P.T. $\Rightarrow$ It is working on principle of μ -max, used to measure high voltage. The standard secondary voltage of the P.T. is 110V. It provides voltage signal for voltmeter, energy wattmeter and Relays like directional and distance. It can used as a Backup for CVT's

- CT: It consist of single turn primary and multiple secondary turns with different ratio used for measuring high currents. The standard sec. current is of 1A or 5A. It provide signals for ammeter, wattmeter and energy meters, and relays like overcurrent differential, distance etc.



• Power X-mel. $\rightarrow 220/132 \text{ kV}$ capacity of X-mel = 100 MVA

$$I_1 = \frac{100 \times 10^6}{\sqrt{3} V_1} = \frac{100 \times 10^6}{\sqrt{3} \times 220 \times 10^3} = 262.43 \quad I_2 = \frac{100 \times 10^6}{\sqrt{3} \times 132 \times 10^3} = 437.38$$

Then Current value of C.T. $\Rightarrow 300/1 \text{ A}$ in primary (CT_1)
 $\Rightarrow 500/1 \text{ A}$ in secondary (CT_2)

• Let $132/33 \text{ kV}$ having capacity of X-mel = 20 MVA .

$$I_1 = \frac{20 \times 10^6}{\sqrt{3} \times 132 \times 10^3} = 87.4 \quad \text{So value of C.T. Ratio} \\ = 100/1 \text{ A } (CT_3)$$

• Suppose another power-X-mel of 165 MVA capacity $440/220 \text{ kV}$

$$I_2 = \frac{165 \times 10^6}{\sqrt{3} \times 220 \times 10^3} = 445.6 \text{ A}$$

So C.T. ratio will become (CT_2) = $500/1 \text{ A}$.

• As C.T. ratio are not same, $CT_2 = 500/1 \text{ A}$, $CT_1 = 300/1 \text{ A}$, to make equal we add 65 MVA capacity X-mel at bus bar of 220 kV .

• C.B $\Rightarrow$ C.B are filled with arc quenching medium like SF_6 , oil, vacuum air etc so that this can be open or closed at NO load or full load.

✓ This can be operated by relay or manual

• Isolator - It must be opened or closed at No load only because it does not contain any arc quenching medium.

• Earth Switch - It is used to discharge residual energy present in the electrical equipment.

✓ It has to be open position under normal condition.

✓ Sequence used Before attending the maintenance of the equipment:

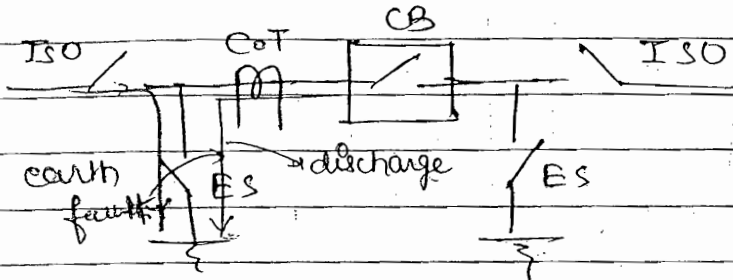
(1) Open C.B under No load or full load

(2) open Isolator under No load.

(3) Close Earth Switch

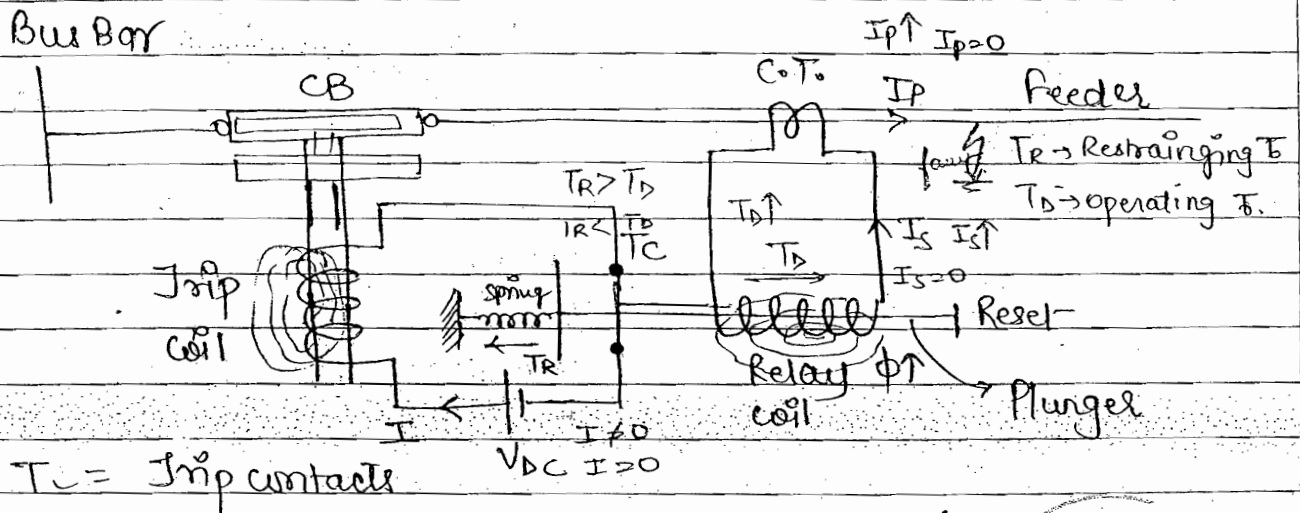
⇒ Sequence Used before charging of the equipment:

- (1) open Earth switch
- (2) Close Isolator
- (3) Close CB.



After maintenance, if ES is not open and ISO → closed, intentionally created earth fault.

• Relation B/w CB and Relays:-



(1) Block (Healthy Condition)

$T_c \rightarrow \text{open (Normal open - N.O)}$

$CB \rightarrow \text{close}$

(2) Trip (Faulty Condition)

$T_c \rightarrow \text{close (Normal close - N.C)}$

$CB \rightarrow \text{open}$

• After fault is removed, Manually Reset is pressed to open the T_c

- How to identify which Relay get operate after the fault.
In Normal condition, CB are closed, when a particular CB is get operated, it will pull down and can see the identification, by which we get know which CB get operate.

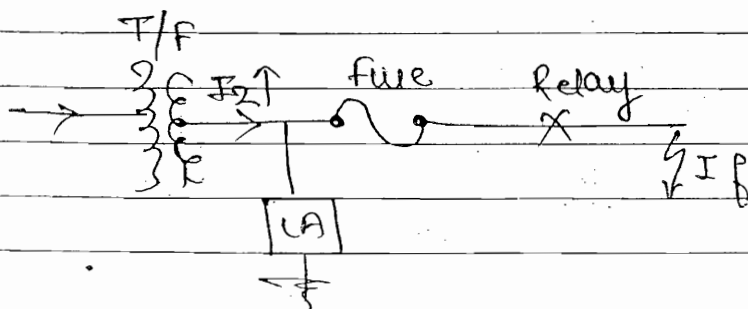
• Types of Relay:-

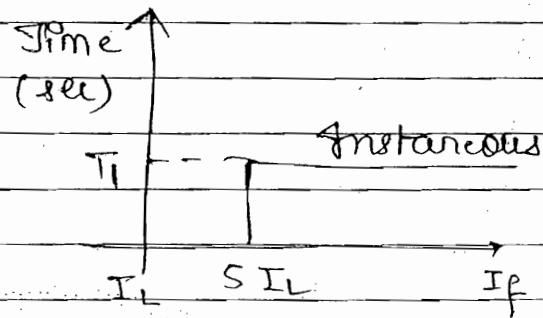
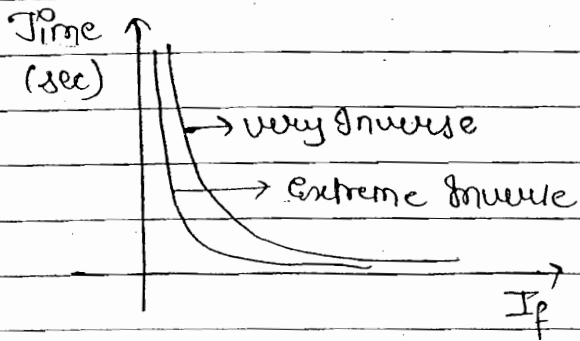
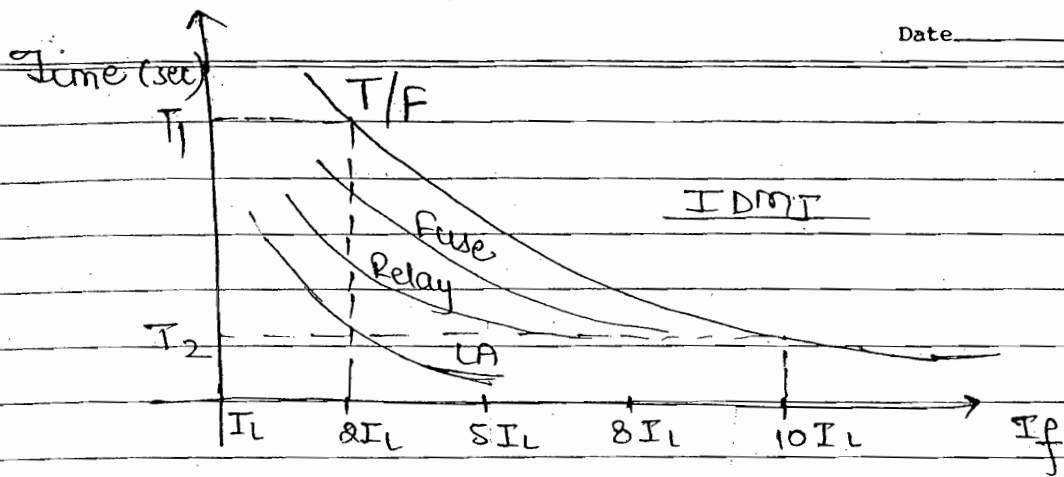
Depends on: PRINCIPLE	Equipment Protected	Sensing Element	Time (IDMT)
(1) Electromagnetic	Generator	Over current	Inverse Definite
(2) Thermal	X-mel	Over Voltage	Minimum Time
(3) Static	Tr-line	over flux	Very Inverse
	Bus-Bar	Over speed	Exponential Inverse
	Motor	Earth fault	Instantaneous
		Distance	
		Directional	
		Differential	

• Total fault clearing time =

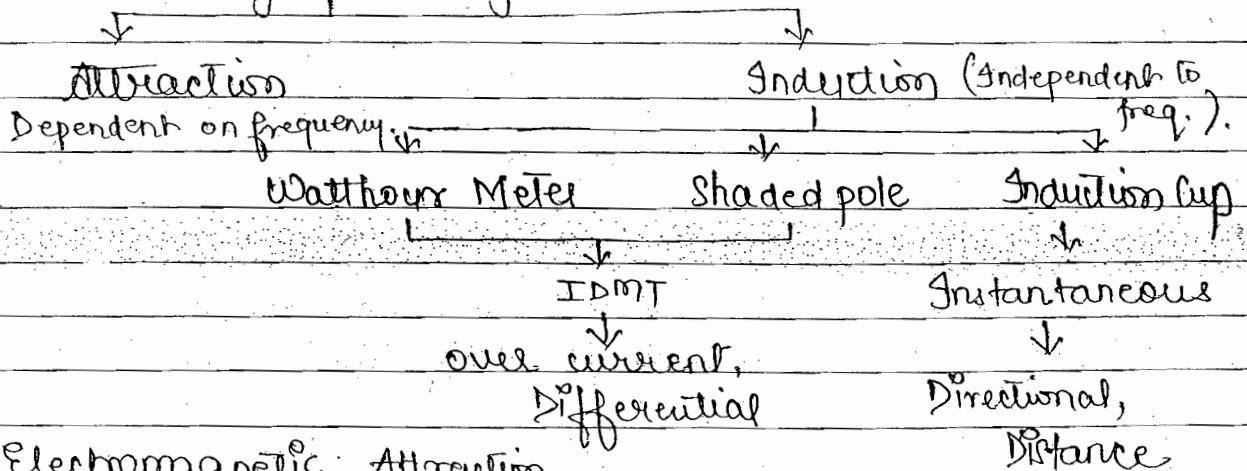
$$\text{Relay Time} + \text{Circuit Breaker Mechanical operating time} + \text{Arc quenching time}$$

- The minimum fault clearing time required 5 to 6 cycles.
(100 - 120 milliseconds)

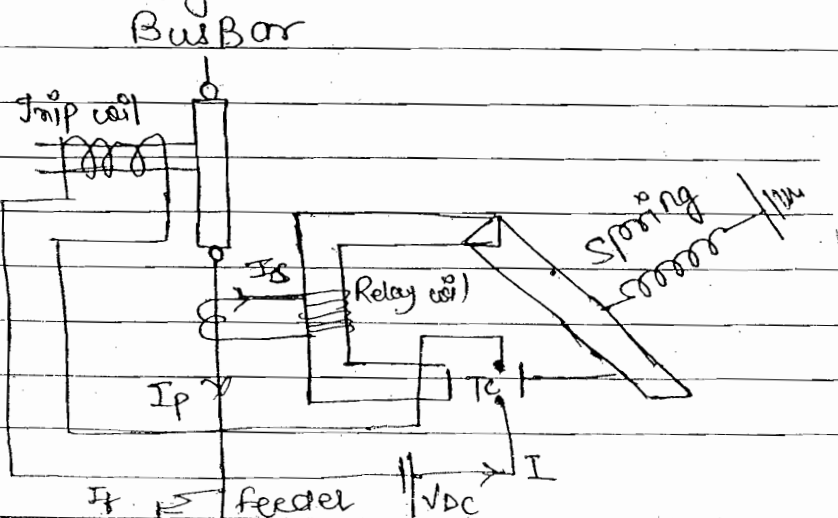




① Electromagnetic Relay:-



Electromagnetic Attraction



$$\phi \propto I_s \propto I_p \propto I_f$$

$$I_f = I_m \sin \omega t$$

$$T_D \propto I_f^2$$

$$\propto I_m^2 \sin^2 \omega t$$

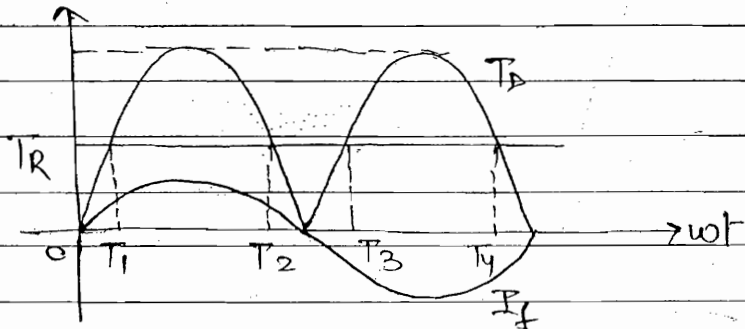
$$T_D = \frac{K I_m^2}{2} (1 - \cos 2\omega t)$$

T_D = Operating / Deflecting Torque

T_R = Restraining / Control Torque.

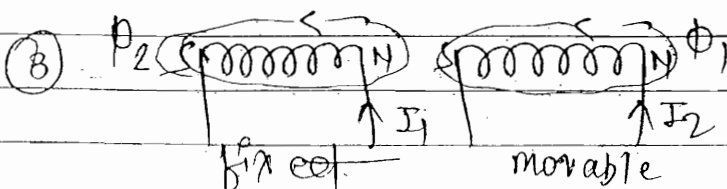
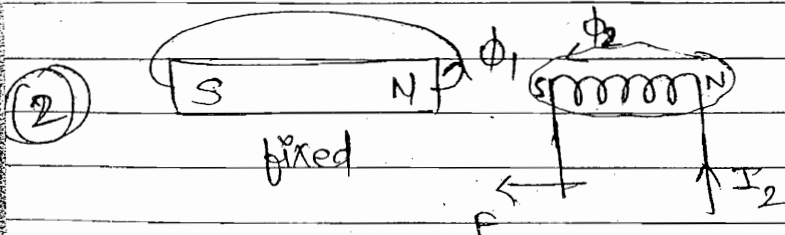
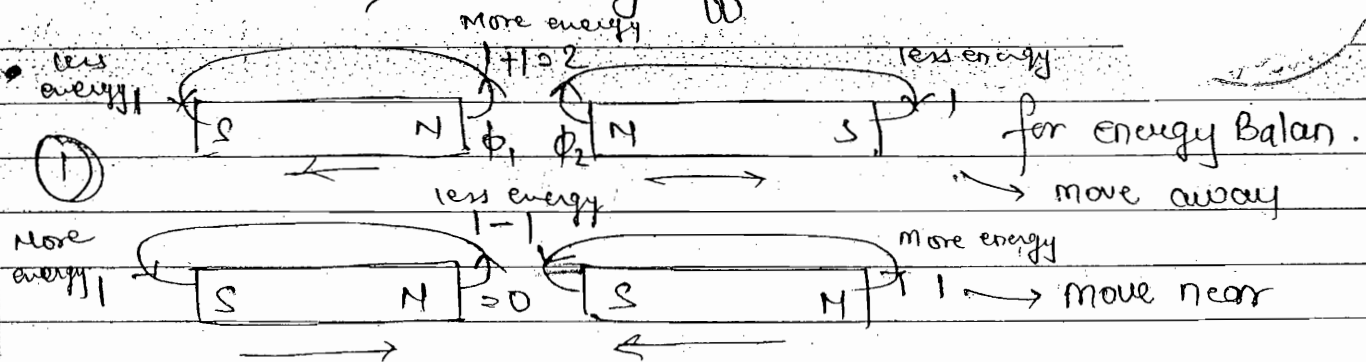
Trip: $T_D > T_R$

Block: $T_D \leq T_R$



• Attraction Type → Not in use now.

Problem ⇒ Doubling effect.

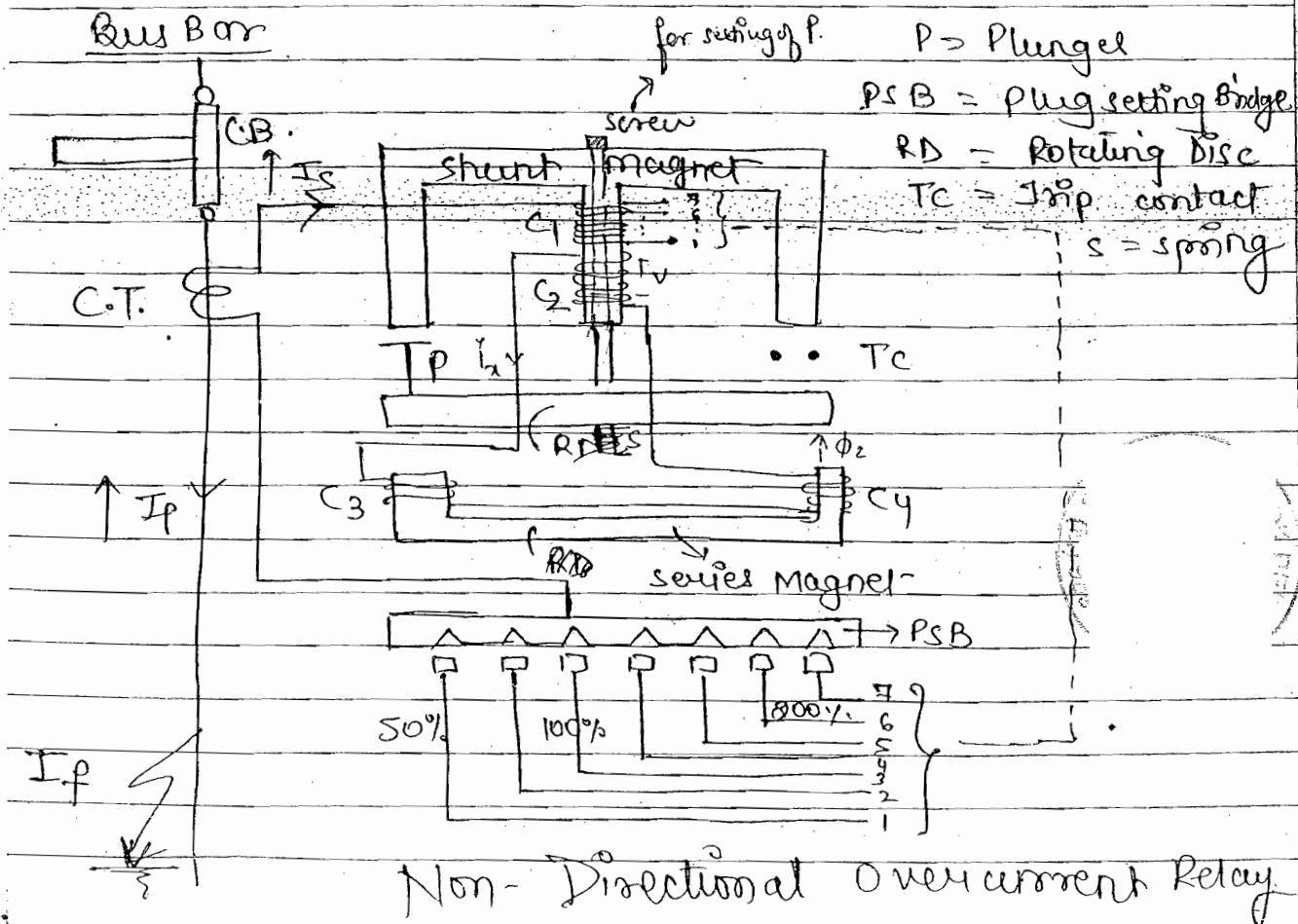


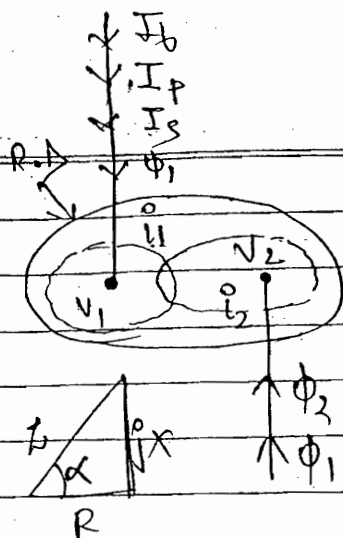
Doubling effect - In electromagnetic attraction relay $T_d \propto (1 - \cos \omega t)$ i.e. in one cycle of fault current, trip contacts and close twice, so that arcing is produced b/w the trip contacts and the plunger. This will cause overheating and damages the relay trip contacts. This effect is called doubling effect. Due to this effect electromagnetic relays are practically not used.

B/w T_2 to $T_3 \rightarrow$ contact open $\rightarrow$ produce arc, after T_4 again open.

• Electromagnetic Induction Relay:

✓ Watt-hour Meter Relay:- Problem of doubling effect can be eliminated in the electromagnetic relays. Hence, these are used most practically in the substation.





$$I_f = I_m \sin \omega t$$

$$\Phi_1 \propto I_s \propto I_p \propto I_f$$

$$\Phi_1 = \Phi_m \sin \omega t$$

$$V_1 = - \frac{d\Phi_1}{dt} = \Phi_m \omega \sin(\omega t - 90^\circ)$$

$$i_1 \propto V_1 \propto \Phi_m \sin(\omega t - 90^\circ - \alpha)$$

$$\Phi_2 = \Phi_m \sin(\omega t - \theta)$$

$$V_2 = - \frac{d\Phi_2}{dt} = \Phi_m \omega \sin(\omega t - \theta - 90^\circ)$$

$$i_2 \propto V_2 \propto \Phi_m \sin(\omega t - \theta - 90^\circ - \alpha)$$

$$T_D \propto (\Phi_1 i_2 - \Phi_2 i_1) \propto \Phi_m \Phi_m [\sin \omega t \cos(\omega t - \theta) - \cos \omega t \sin(\omega t - \theta)]$$

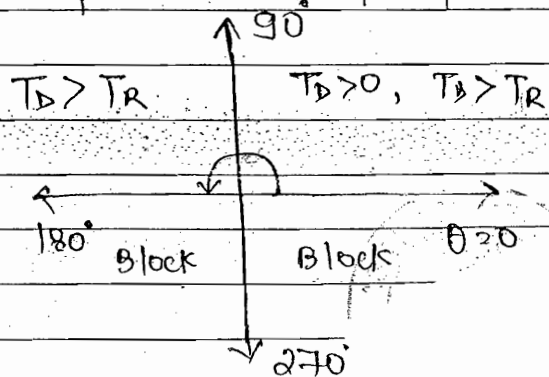
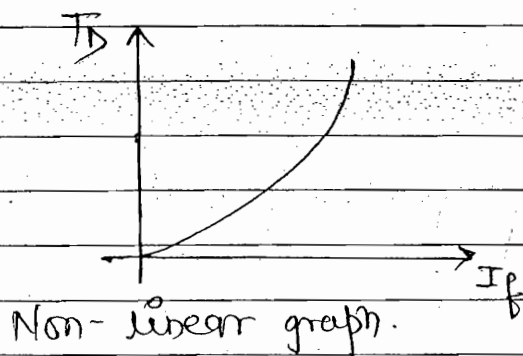
$$T_D \propto \Phi_m \Phi_m \sin \theta$$

$$\Phi_m \propto I_{f1} \text{ and } \Phi_m \propto I_f$$

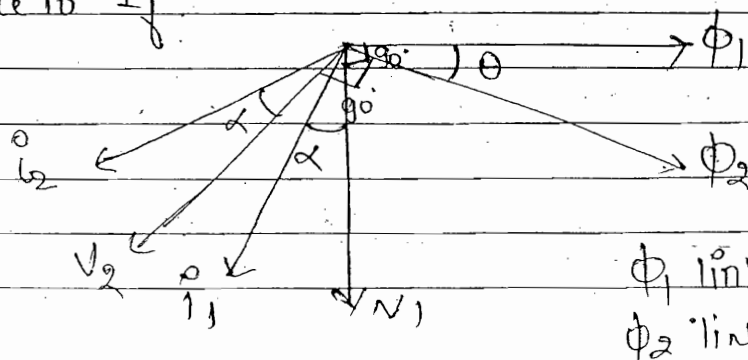
$\theta \rightarrow$ Impedance Angle
due to C_2, C_3, C_4

$$T_D \propto I_f^2 \sin \theta$$

Independent to frequency.

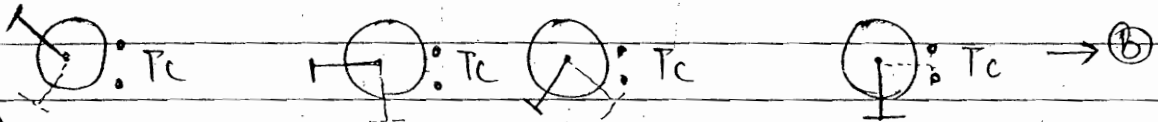
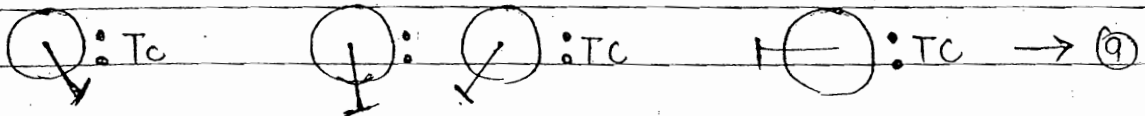
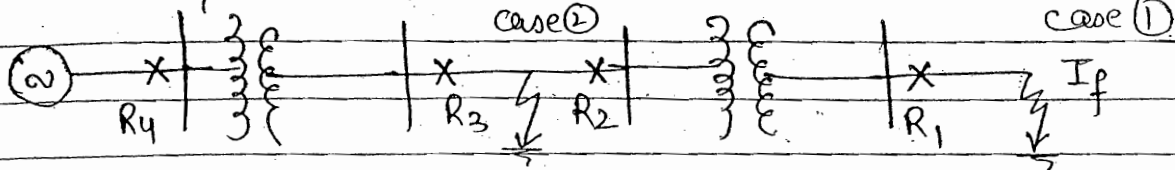


- Φ_2 due to i_1 , i_1 due to V_1 , V_1 due to Φ_1 , Φ_1 due to I_s , I_s due to I_p
 I_p due to I_f



Time Grading

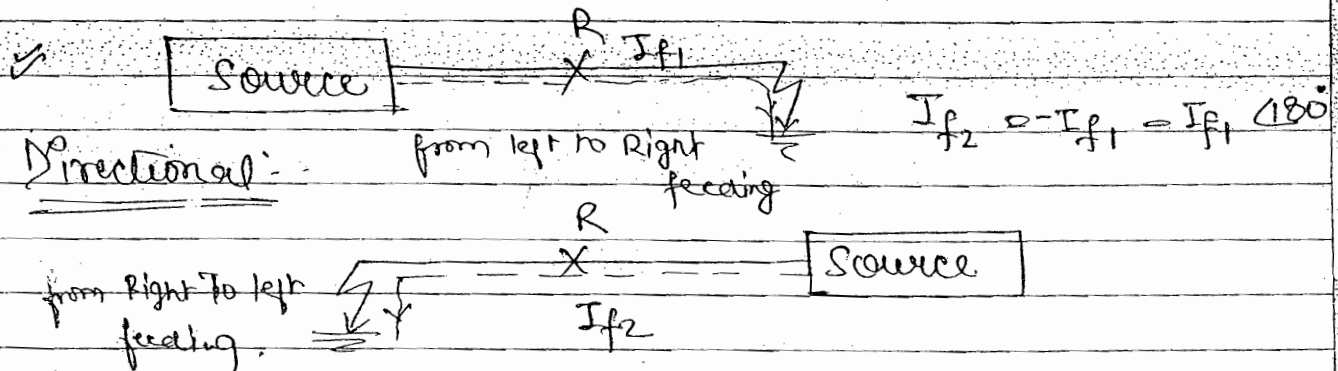
Date _____



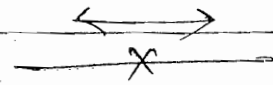
Case 1:-

In (a) condition, plunges are arranged in this manner, fault is away from source, R_4 will operate first, then R_3, R_2, R_1 . Not a good sys. So arrangement is done in (b) condition manner. At fault, Sequence of operating Relay $\rightarrow R_1, R_2, R_3, R_4$. When fault occur, all relay will simultaneously operate, if R_1 get fail, then seq. of operating of Relay $\rightarrow R_2, R_3, R_4$.

Case 2: If fault occur b/w R_3 & R_2 , near the source, as $T_D \propto I_m^2$ fault current value is more, so R_3 will operate quickly in less time. $\Rightarrow$ fault Near the source. If value more, away the source If value is low



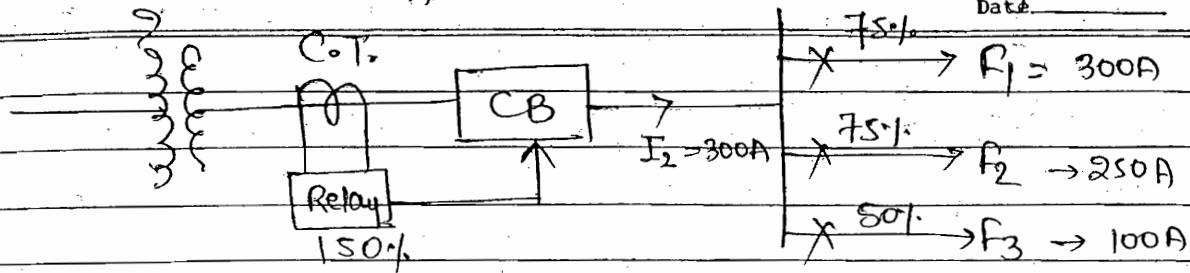
Symbol Non directional Relay



$\Rightarrow$ CB will operate in either direction of fault current.

Current Grading

500/5A



PSB

250	375	500A	625	750	825	1000A
1	2	3	4	5	6	7
50%	75%	100%	125%	150%	175%	200%

for 300A $\rightarrow 100\% = 500$
5A

✓ Now added $F_2 \Rightarrow 300 + 250 = 550$ it will set to

4 Nob. = 625A (125%) $\Rightarrow 125\% \times 5 = 6.25$

✓ Now again added a feeder F_3 of demand 100A.

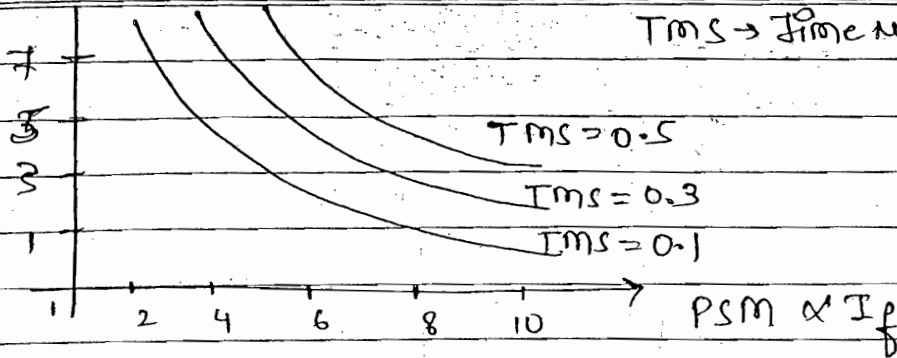
Total = $300 + 250 + 100 = 650$ A, set to 180%.

$180\% \times 5A = 7.5$

Now it will get connected to nob 5.

Time (sec)

Date _____

TMS $\rightarrow$ Time multiplier setting.

IDMT (character of dc Relay)

(1) Pick up current of Relay: -

$$I_{pk} = \% \text{ setting of Relay} \times \text{C.T. Sec Current}$$

(2) Plug setting Multiplier (PSM)

$$PSM = \frac{I_f}{I_{pk} \times \text{C.T. Ratio}}$$

(3) Time of operation of any Relay: -

$$T_o = TMS \times (\text{Time calculated from IDMT graph/Table corresponding to PSM})$$

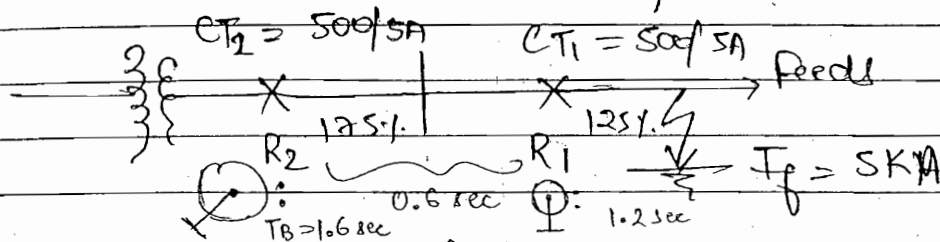
(4) Time of operation of Back up Relay: -

$$T_B = (T_p + T_d)$$

 T_p = Time of operation of primary Relay T_d = Time delay b/w Primary and Back up Relay.

Q Part of pow sys N/w is shown in the fig. The primary relay R_1 has TMS of 0.3. The time delay b/w primary and Back up relay R_1 & R_2 is 0.8 sec. Both Relays having CT Ratio of 500/5A. The IDMT character is given in the Table for the R_1 and R_2 . Calculate

- (i) Time of operation of Primary Relay
 (ii) PSM of Back up Relay.



PSM	10	8	5.7	4.5
Time (sec)	2	4	↓ 5	8

Solution: for Relay 1 $\therefore I_{PK} = \frac{125}{100} \times 5 = 6.25 \text{ A}$

$$PSM = \frac{I_P}{I_{PK} \times CT \text{ Ratio}} = \frac{5000}{6.25 \times 500} = 8$$

$$T_0 = 0.3 \times 4 = 1.2 \text{ sec}$$

for Relay 2 $\therefore I_{PK} = \frac{175}{100} \times 5 = 8.75 \text{ A}$

$$PSM = \frac{5000}{8.75 \times 500} = 5.7$$

$$T_0 = T_B = T_P + T_d = 1.2 + 0.6 = 1.8 \text{ sec}$$

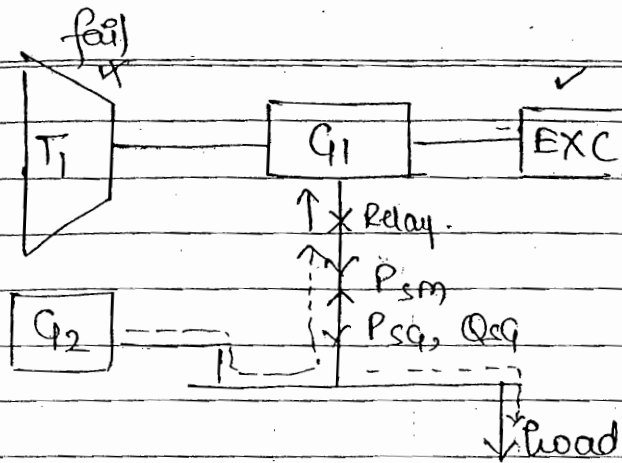
same for
primary or
back up relay.

$$TMS \times 5 = 1.8 \text{ sec}$$

$$TMS = 0.366$$

31/10/14

- Directional OR Reverse Power OR Wattmetric Relay
 When the prime mover get fail or stop delivering the HP to gen G_1 , G_1 will draw the huge amount of active power from G_2 to drive the Turbine bcoz now it will work as motor bcoz it has flux. It will damage the G_1 wdg, so we use Reversal power Relay to watch the flow of power direction.



Relay → Block when power flow from G_1 to load. (syn. Gen.)

Relay → operate when power flow from G_2 to G_1 (syn. Motor)

- Non directional Overcurrent Relay: -

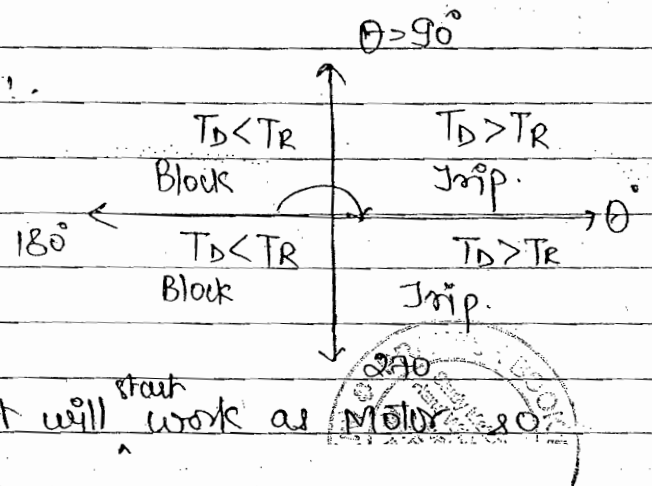
$$T_D \propto \Phi_{m1} \Phi_{m2} \sin \theta$$

Directional / Reverse power Relay: -

$$\Phi_{m1} \propto V, \Phi_{m2} \propto I$$

$$\sin \theta \rightarrow \cos \theta$$

$$\text{Ideal} \rightarrow \begin{cases} T_D \propto VI \cos \theta \\ T_D \propto P \end{cases}$$



- Relay must operate Before it will ^{start} work as Motor. speed must be high.

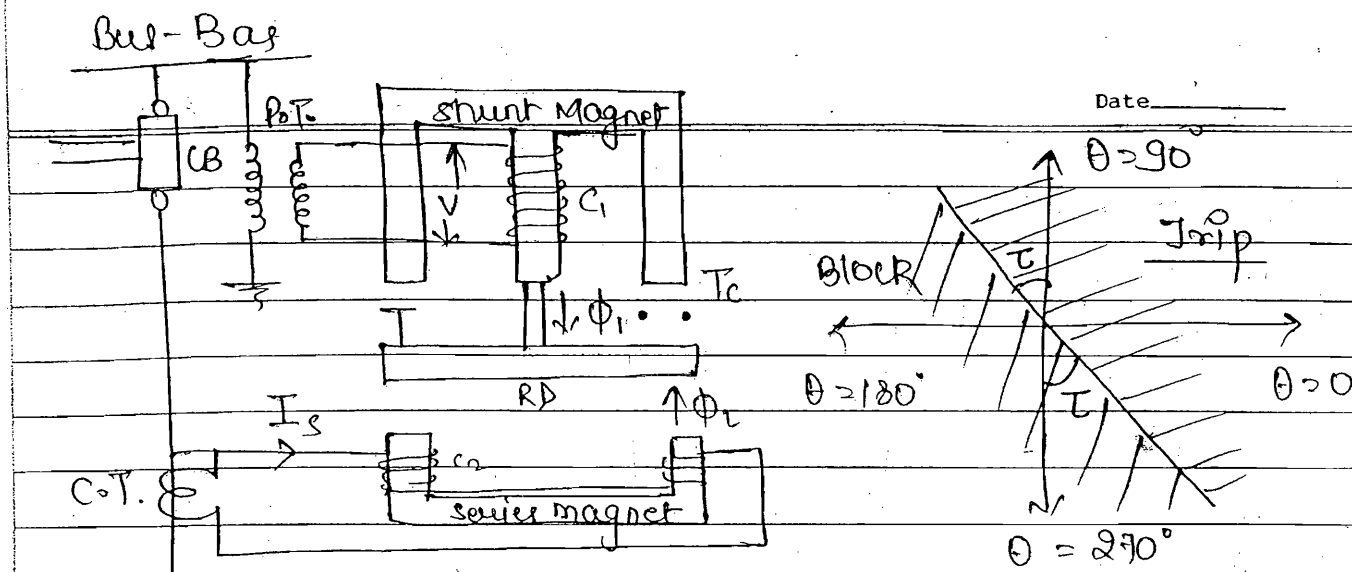
- To get Maximum Torque θ must equal to 0° , for this V and I are in same phase, for this we use Resistive coil, (such RC arrangement).

practically: - $T_D \propto VI \cos (\theta - \tau)$

τ = Max. Torque adjustment angle

$$\text{If } \tau = 0 \Rightarrow T_D \Rightarrow T_{Dmax} = VI$$

- Never use $\tau = 90^\circ$, otherwise $T_D = VI \cos (\theta - 90^\circ) = VI \sin \theta$ which is non directional condition.



$$T_d = VI \cos(\theta - \tau)$$

✓ T value should lie b/w 0 to 90°

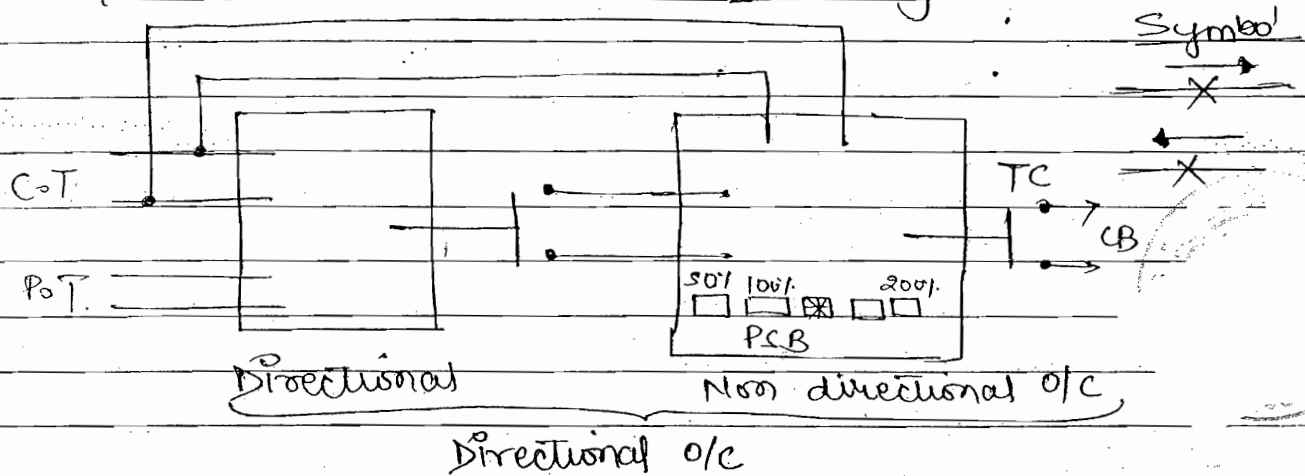
- We make C_1 very highly inductive. So we get now $\theta = 90^\circ$ which make $\sin \theta \Rightarrow \sin(90^\circ) = \cos \theta$. To make VI are in phase θ must $= 0$, (Resistive nature) for this ϕ_1 and ϕ_2 have phase displacement $= 0$, To make phase displacement we use other value τ . T_p max when $\theta = \tau$.

- Directional or reversal power relay is used to produce trip signal if the direction of power is reversed.
- operating T is proportional to the power. so that C.T. and P.T. are applied to the relay.
- Max T is required so that it is normally make up of induction cup structure which is working on the principle of Induction Motor.
- In watt hour Meter Relay an extra τ adjustment angle is provide to get max T .

- Application (1) The Reverse power Relay used to protect generator from the failure of prime Mover (Turbine) (2) In Normal condition if prime mover and excitation is present the syn. generator delivers more

active and reactive power to the load. If the excitⁿ is present and prime mover is failed then the gen. absorbs active power from the other parallel gen. and start working as syn. Motor. The Turbine is working as Mechanical load for this Motor. Bcoz of huge Mass of the turbine the motor draws heavy current which damages the wdg. To protect the gen from this abnormality, Reverse power Relay is used.

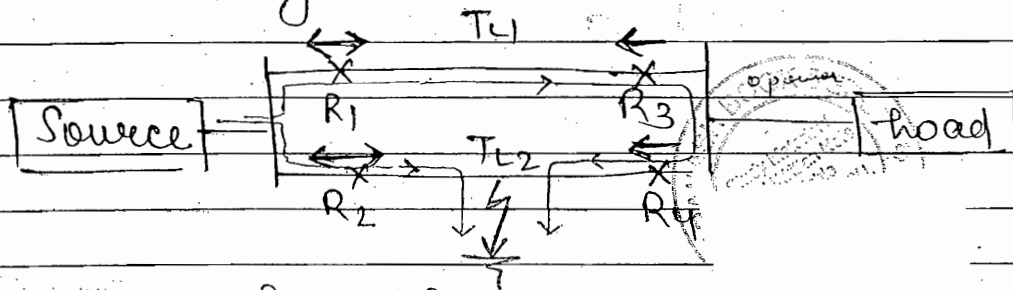
• Directional Over current Relay:-



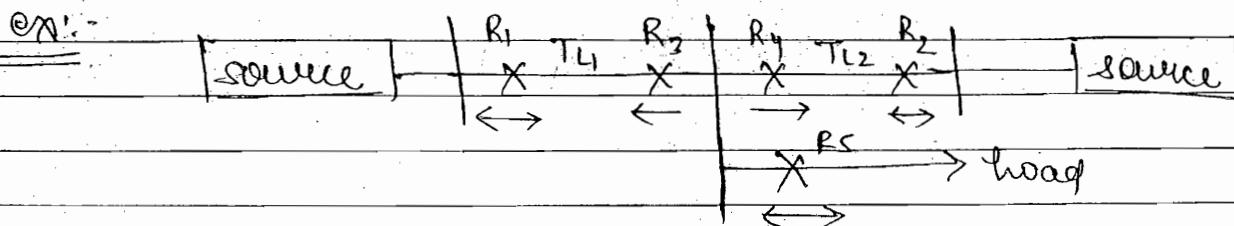
- Directional Over current Relay containing Both reverse power element and non-directional over current Relay. In case of power direction is reversed the direction element operates and closes the trip contacts which initiates non-directional over current relay. This relay checks whether the reverse current is exceeding the P.S.V. and produce trip signal if it is exceeding which open the CB.

- Application of Non-directional o/c & Directional o/c Relays
 - (1) Protection of parallel feeders:- In case of n feeders Source & Relays are Non-directional o/c relay and load and Relays

are directional O/C relays are used. Under Normal condition power flows from source to load through the parallel feeders. If any fault is occur in one of x-line, corresponding relays operate isolating the faulty line. So that 50% of power can be transferred from the healthy line.

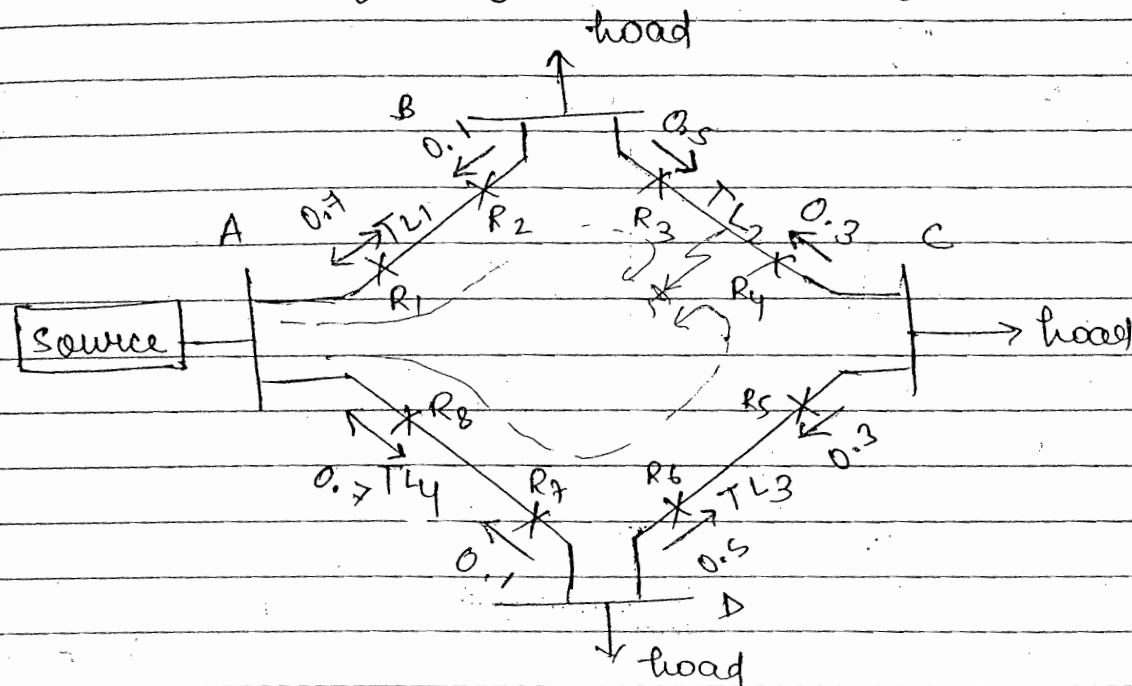


- Relay operate R_2 and R_4 .
- If we use R_3 and R_4 also Non-directⁿ then what happen. If fault occur at T_{L2} , R_3 relay get operate $\rightarrow$ Not Req. If we provide time delay $R_4 \Rightarrow 0.1$, $R_3 = 0.4$, then R_4 will operate, but by this time delay if fault occurs at T_{L1} , then T_{L1} will operate which is not required. So we use directional Relay.



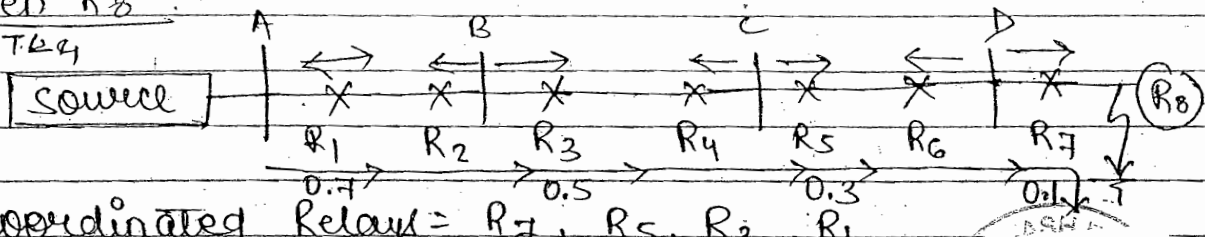
Here R_1 and R_2 are non-directⁿ o/c Relay. and R_3 and R_4 are direction o/c Relay. But in case of R_5 , Bus Bar is source for load. so R_5 is non-directⁿ o/c Relay.

Protection of Ring Distribution Systems:-



• Open R_8 :

fault TL_2

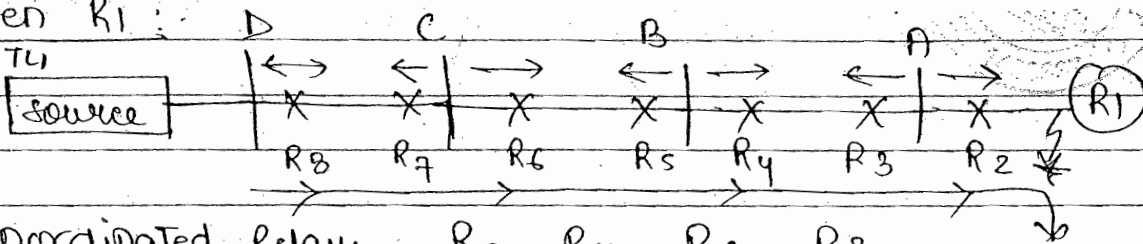


Coordinated Relays = R_7, R_5, R_3, R_1

provide time delays 0.1, 0.3, 0.5, 0.7

• Open R_1 :

fault TL_1



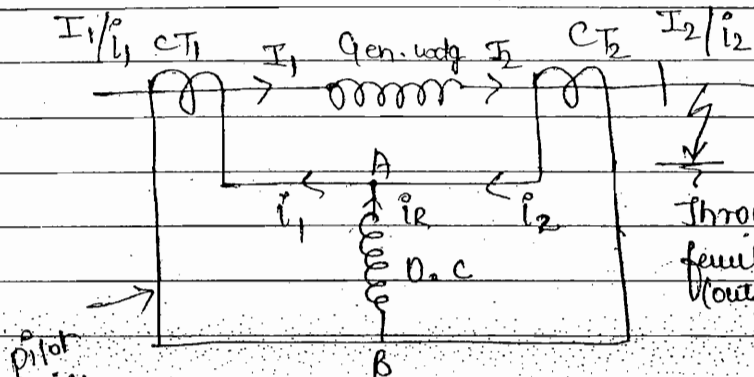
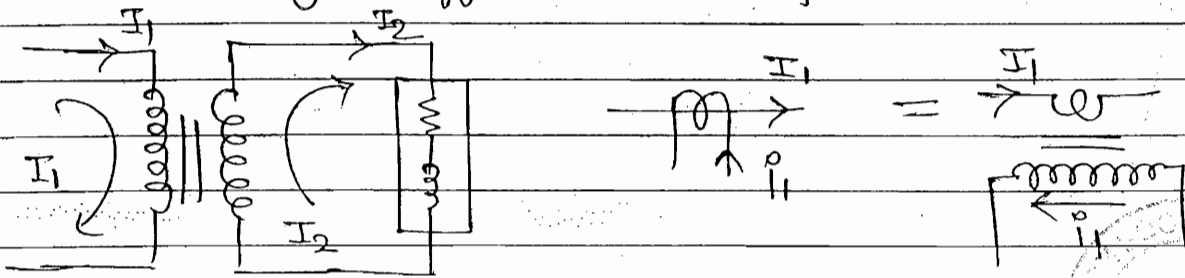
Coordinated Relays: R_2, R_4, R_6, R_8

provide time delay:- 0.1, 0.3, 0.5, 0.7

- If fault at $TL_2 \rightarrow R_4, R_6, R_8$ and R_3, R_7 will operate
time delay $\rightarrow 0.3, 0.5, 0.7$ $0.5, 0.7$

- for protection of Ring System Non-directional relays are kept on source side, and directional relays are kept on load side. Time grading is provided b/w the relays for complete protection of Ring System

• Ordinary Differential Relay :-



At Node A

$$i_R + i_2 = i_1$$

Through fault.

$$i_R = i_1 - i_2$$

$$= |i_1| \angle \theta_1 - |i_2| \angle \theta_2$$

(Outside the protect zone)

$$i_R = \frac{I_1}{CT_1 \text{ Ratio}} - \frac{I_2}{CT_2 \text{ Ratio}}$$

$$\text{If } CT_1 \text{ Ratio} = CT_2 \text{ Ratio} = C \text{ Ratio}$$

$$i_R = \frac{I_1 - I_2}{CT \text{ Ratio}}$$

OC = operating coil of Diff. Relay.

i_R = Relay current.

• ① Trip

$$i_R \neq 0 \text{ (Ideal)}$$

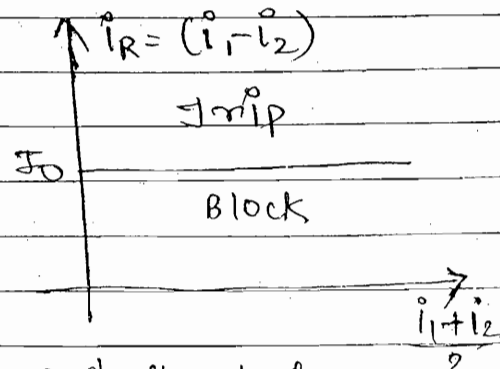
$$i_R > I_0 \text{ (Practical)}$$

② Block :-

$$i_R = 0 \text{ (Ideal)}$$

$$i_R \leq I_0 \text{ (Practical)}$$

I_0 = Min. pick up current of relay
= spring Restraining Torque



graph: Charact. of ordinary Diff. Relay.

- Power X-Mer have diff. CT Ratio Bcoz of voltage step up and step-down.
- Motor and gen. have same voltage so same CT ratio.

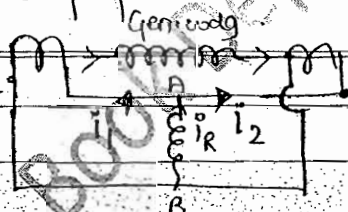
Date _____

- Differential Relay is a unit protectⁿ Relay, used for protection of generator, x-mer, motor loads and Bus Bar protection. Also used to protect x-line. This is called pilot relaying.
- If the phasor difference of two electrical sys. i.e. I & V exceeding the setting value of relay produces trip signal. This principle is used in the diff. relay.
- Through Fault:- If the fault is occurring outside the unit protection zone is called through fault.
- If the any relay is producing trip signal without any operation is called mal operatⁿ of Relay.

mp current

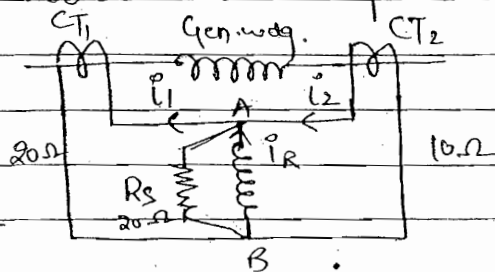
Advantages of Ordinary Diff. Relay:-

- If one of the sides of pilot wire is wrongly connected, Relay produces trip signal without any fault.



$$I_R = (I_1 + I_2) \neq 0 \rightarrow \text{Trip}$$

- Difference in the length or resistance of pilot wire produces potential difference across the relay coil so that $I_R \neq 0$ occur. Which operate the relay without any fault.



To overcome this difficulty a Stabilizing Resistor is connected in parallel to the relay coil

R_S = Stabilizing Resistor

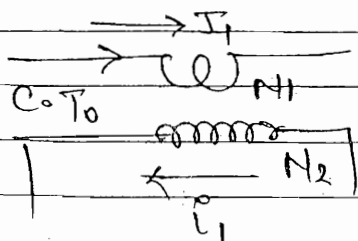
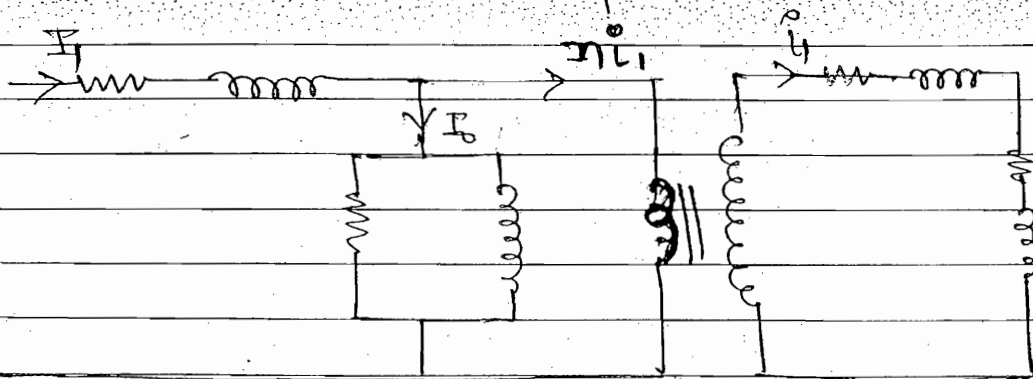
- Use 11 resistor, Not series Becoz we can't cut the cable and place the series Resistor.

(3) If the CT of core of CT is saturated produced trip signal without any fault. But for the outside fault are through fault produce trip.

I_f	CT ₁	CT ₂	$I_R = I_1 - I_2$	
100	100/1	100/1	1-1=0	} Block
200	200/2	200/2	2-2=0	
400	400/4	400/2	4-2=2	} Trip
600	600/6	600/2	6-2=4	

↓ saturation

(4) If CT₁ and CT₂ has different ratio and phase angle error produces trip signal without any fault. Becoz of No-load component of current phase angle and ratio-error are produce.



$$N_1 \cdot N_2$$

$$n = \frac{N_2}{N_1} = \text{Nominal Ratio}$$

$$I_1 = I_0 + n I_2$$

$$\frac{I_1}{I_2} = \text{Actual Ratio}$$

$$\text{Actual Ratio} = \frac{I_1}{I_2} = n + \frac{I_0}{I_1} \leftarrow \text{Ratio Error}$$

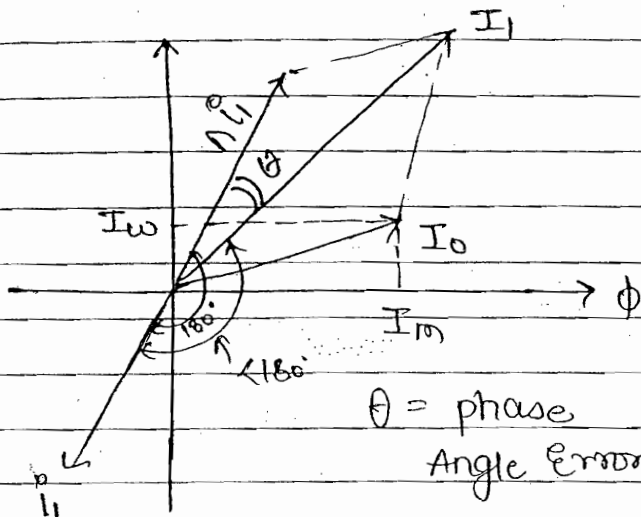
Suppose Ideal case.

$$N_1 = 1, N_2 = 100$$

$$n = \frac{N_2}{N_1} = \frac{100}{1} = 100$$

$$I_1 = 500; I_2 = 5A$$

$$\frac{I_1}{I_2} = \frac{500}{5} = 100$$



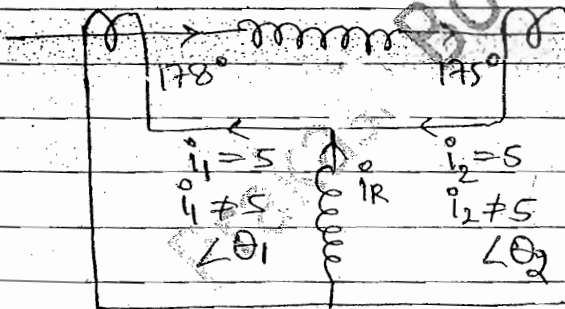
When I_1 transfer to primary it become nI_1 . Diff b/w nI_1 and $I_2 = 180^\circ$ (Ideal case)

But due to error it is $< 180^\circ$, So $I_1 = nI_2 + I_0$

Error called θ

$$CT_1 = \frac{500}{5} = I_1 = 100 \text{ (N.R.)}$$

$$CT_2 = \frac{I_2}{5} = \frac{500}{5} = 100 \text{ (N.R.)}$$



But when the primary current get change. $CT_1 = 101$ and $CT_2 = 99$
 $I_1 \neq 5, I_2 \neq 5$, Trip signal
 Due to Ratio Error.

Suppose the angle is 178° in CT_1 side and 175° in CT_2
 This causes the phase error.

(5)

pt 1) } pilot wire
2) }

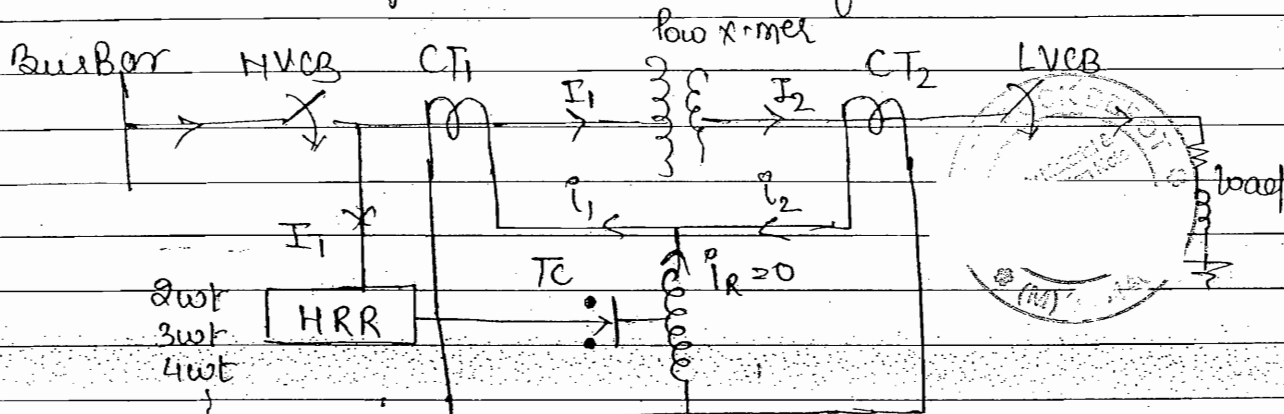
3) } Related to CT
4) }

5) } pow x-mel
6) }

Date _____

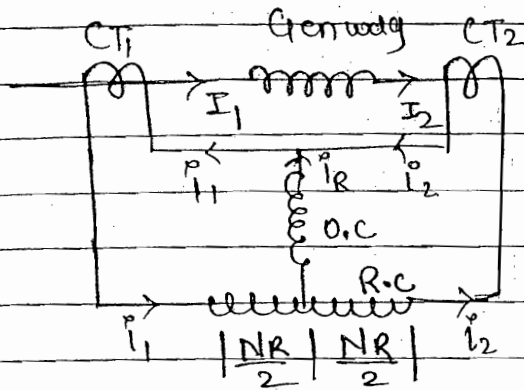
(6) During initial charging time of the power-x-mel magnetic inrush current having high magnitude flows, which will cause unequal current in the primary and secondary CT's so that relay operates without any fault. To overcome this difficulty harmonic restraining relay is used.

The magnetic inrush current consisting of 2, 3, 4 harmonic signals. These signals are filtered by the harmonic restraining relay which will produce additional restraining torque so that relay will not operate during charging time of power x-mel.



- During charging HVCB $\rightarrow$ closed, current I_1 will flow through CT₁ and HRR. HRR produces additional restraining torque, not to operate the relay with HVCB get close. (2wt, 3wt, 4wt) - $I_1 \neq 0$, $i_1 \neq 0$ But $I_2 = 0$, $i_2 = 0$ $i_R \neq 0$, But restraining torque is not allow the ~~set~~ CB to get open, after 10-5 minutes (charging) LVCB also close, so that $I_1 = I_2$, $i_1 = i_2$ and $i_R = 0$

% Differential / pilot wire / Merz price / Biased Scheme Relay



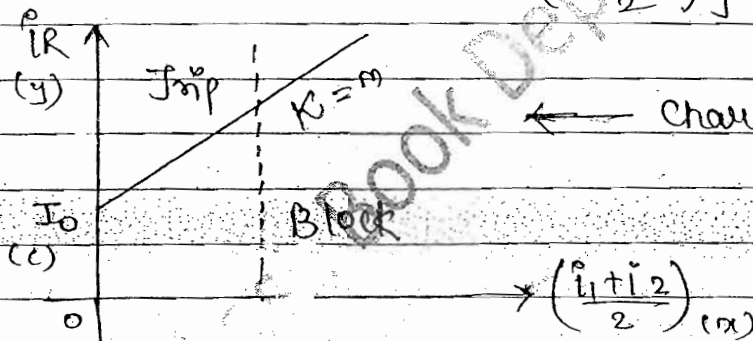
$$\begin{aligned} \text{operating mmf} &= N_o \dot{I}_R \\ \text{Restraining mmf} &= \frac{NR \dot{I}_1}{2} + \frac{NR \dot{I}_2}{2} \\ &= \frac{NR}{2} (\dot{I}_1 + \dot{I}_2) \end{aligned}$$

$$N_o \dot{I}_R = NR \left(\frac{\dot{I}_1 + \dot{I}_2}{2} \right)$$

O.C = operating coil
R.C = Restraining coil.

$$\frac{\dot{I}_R}{\left(\frac{\dot{I}_1 + \dot{I}_2}{2} \right)} = \frac{NR}{N_o} = K = \% \text{ setting}$$

(1) Trip $\dot{I}_R > \left[I_o + K \left(\frac{\dot{I}_1 + \dot{I}_2}{2} \right) \right]$; I_o = spring Torque
 (2) Block : $\dot{I}_R \leq \left[I_o + K \left(\frac{\dot{I}_1 + \dot{I}_2}{2} \right) \right]$; $K \left(\frac{\dot{I}_1 + \dot{I}_2}{2} \right)$ = Restraining coil Torque



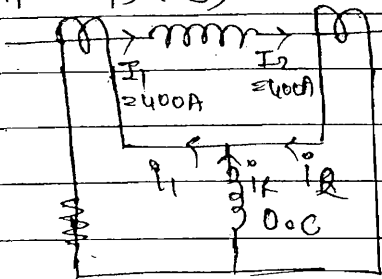
← Characteristic graph of % Diff. Relay.

In the % Diff. Relay, During abnormal conditions when current in R.C flow, spring torque + Restraining T also ↑ with current value. So relay will not operate.

But during fault condition, fault current value is very high $\dot{I}_R$ will operate the relay as operating T is higher than (spring T + restraining T).

Solution (1) (b) Percentage Diff $\hat{I}_1 = \frac{I_1}{CT_1 \text{ Ratio}} = \frac{400}{79} = 5.06 \text{ A}$

$CT_1 = 400/5 (79)$ $CT_2 = 400/5 (81)$ $\hat{I}_2 = \frac{I_2}{CT_2 \text{ Ratio}} = \frac{400}{81} = 4.94 \text{ A}$



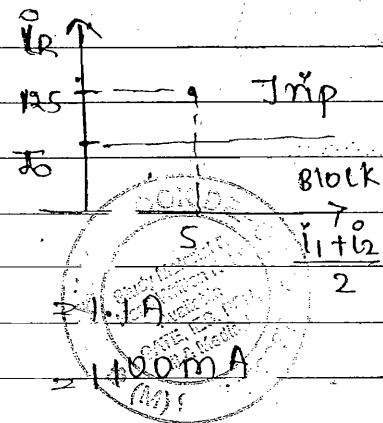
$$\frac{\hat{I}_1 + \hat{I}_2}{2} = \frac{5.06 + 4.94}{2} = 5$$

$$\hat{I}_R = \hat{I}_1 - \hat{I}_2 = 5.06 - 4.94 = 0.125 \text{ A} = 125 \text{ mA}$$

$I_0 = 100 \text{ mA}$ (given)

$I_R = 125$

$I_R > I_0$ (Trip)



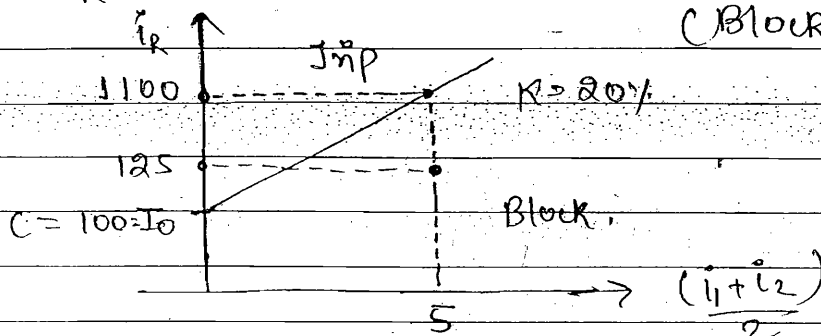
(c) % Diff :-

$$K > 20\% = 0.2$$

$$I_0 + K \left(\frac{\hat{I}_1 + \hat{I}_2}{2} \right) = 100 \times 10^{-3} + 0.2 \times 5 = 1.1 \text{ A}$$

$$\hat{I}_R = 125 \text{ mA} < 1100 \text{ mA}$$

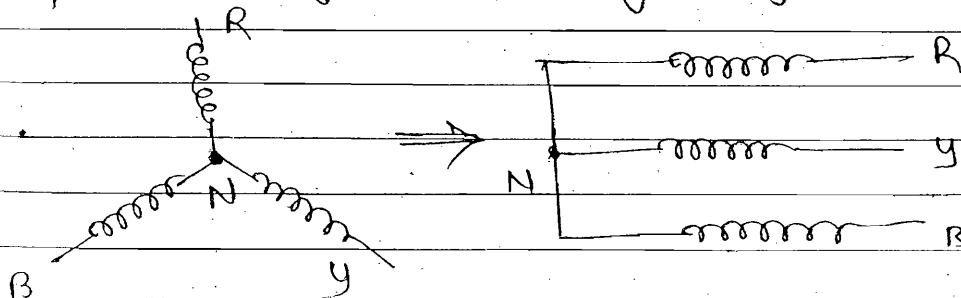
(Block)

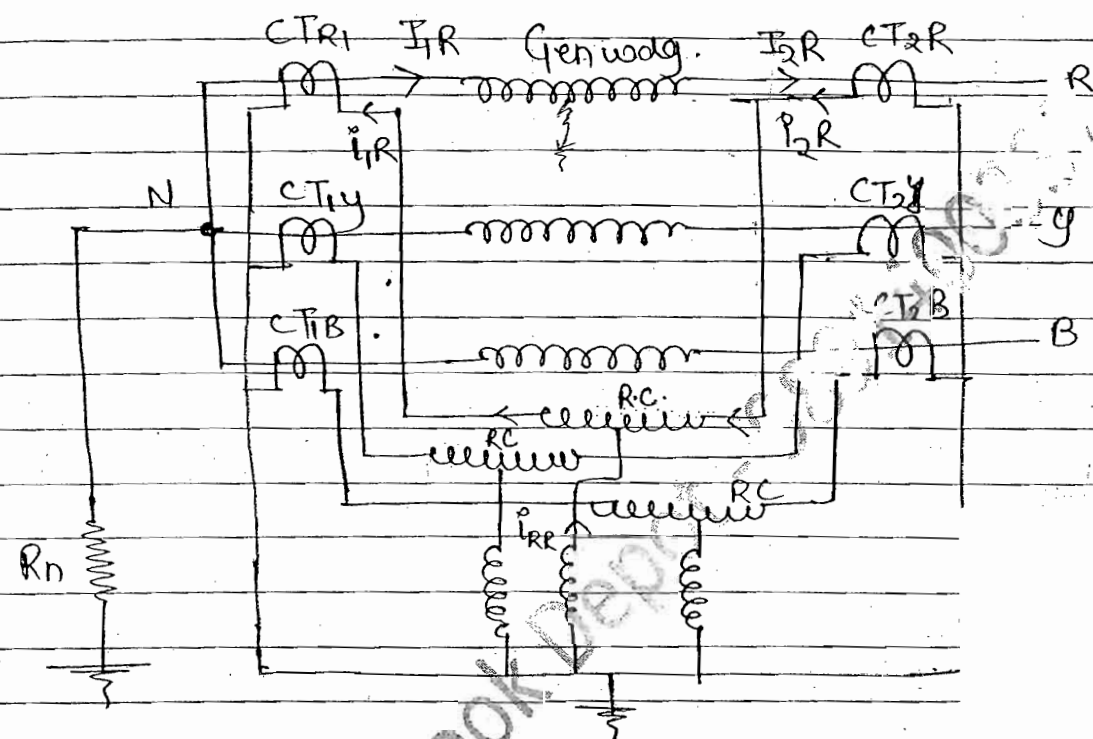
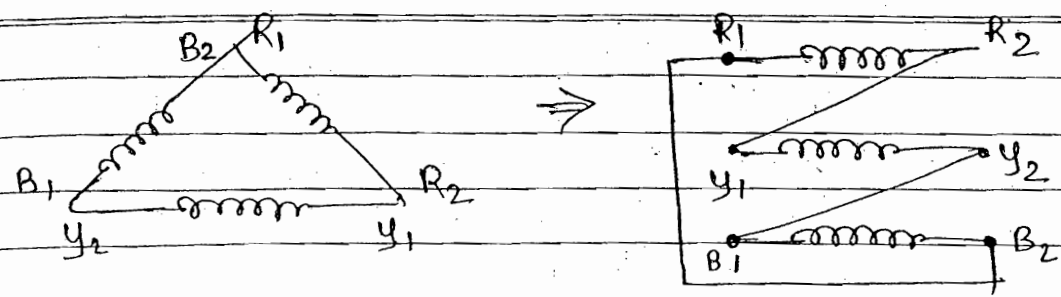


Relay current = 125

corresponding to S
value $\rightarrow$ Block region.

• Protection of 3- ϕ Gen wdg using % Diff. Relay:-

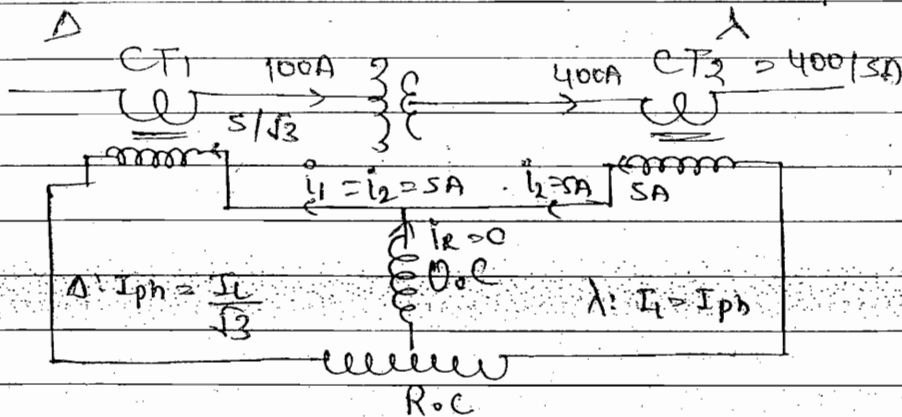
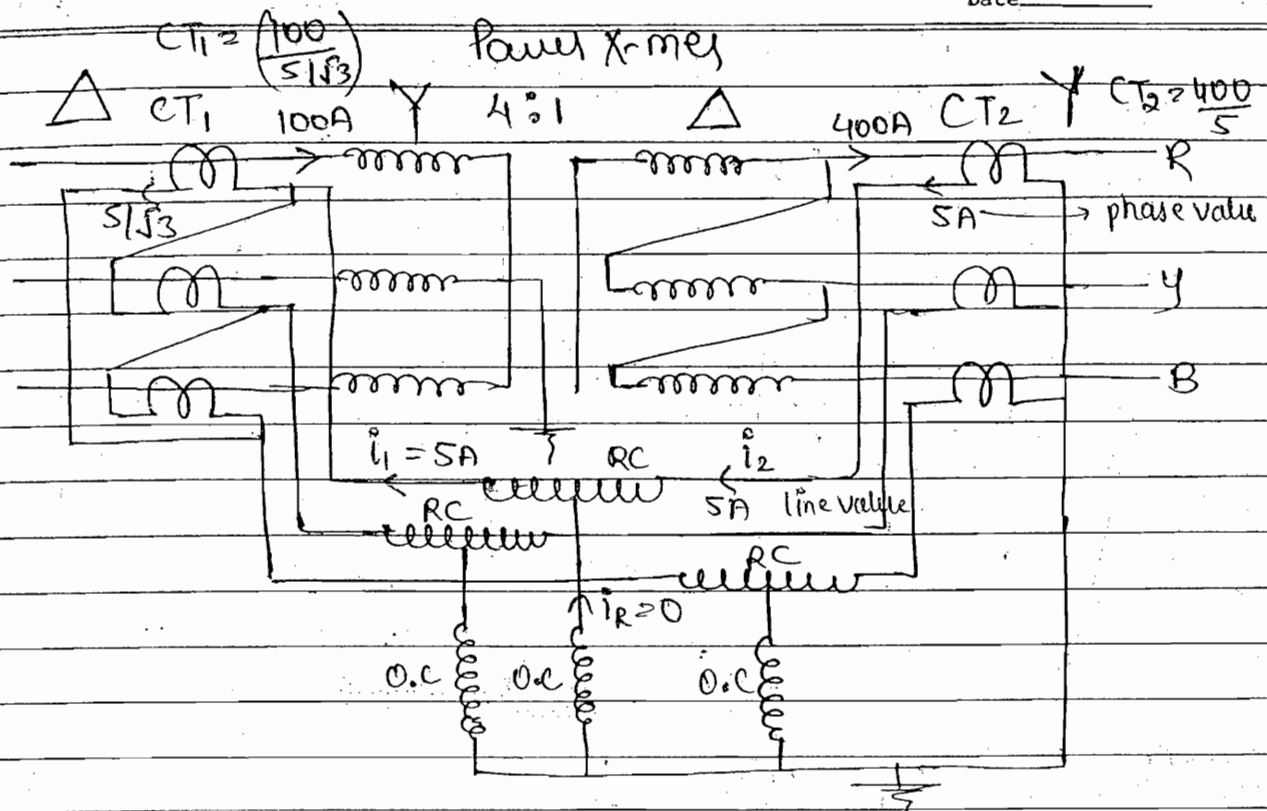




• When fault occur in any phase, for Balance condition all phase CB will get open.

✓ Protection of 3- ϕ X-Mer using % Diff Relay! -

POWER X-MER		CURRENT X-MER	
Primary	Secondary	CT ₁	CT ₂
Δ	Δ	Δ	Δ
Δ	Δ	Δ	Δ
Δ	Δ	Δ	Δ
Δ	Δ	Δ	Δ



Q A 3- ϕ 13.2/33 KV pow X-mel is protected By Merz price protection. The CT ratio on LV side of X-mel is 400/5A. Calculate the CT ratio required on the HV side of pow-xmel If the X-mel is connected

- (1) Δ Δ (2) Δ Δ ($\frac{100}{5\sqrt{3}}$):1

Solution

$$\frac{13.2}{33} = 4:1$$

$$\frac{V_2}{V_1}$$

$$CT_2 = \frac{400}{5} = \text{primary}$$

$$\text{sec}$$

$$\frac{I_2}{I_1} = \frac{V_1}{V_2}$$

$$I_2 = \frac{400}{X4} > 100$$

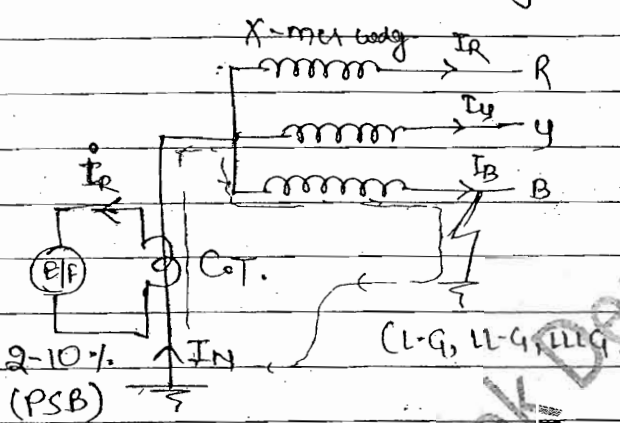
- Inside the CT, per phase values of current
- In RC line value of current used

✓ Secondary current at $CT_2 = 5 \text{ A}$. $\Delta \rightarrow I_{ph} = I_L = 5 \text{ A}$
 we required $I_R = 0$ so $I_{ph} = 5 \text{ A}$.

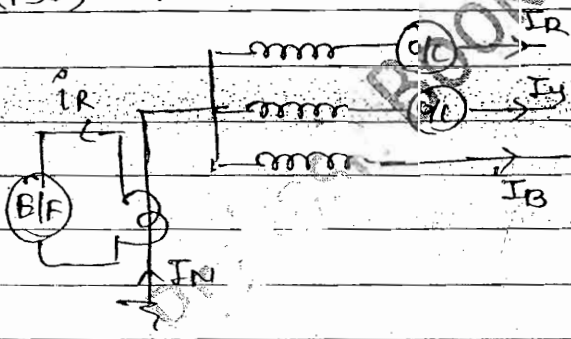
✓ $CT_1 \rightarrow \Delta$ connected so $I_R = \frac{5}{\sqrt{3}}$ $I_{ph} = \frac{I_L}{\sqrt{3}} \because \Delta$.

3/11/2014

• Earth Fault Relay:-



- At No fault $I_N = 0$, $I_R = 0$
- Over-current relay.
- At fault $I_N \neq 0$, $I_R \neq 0 \rightarrow \text{trip}$
- Only operate at Earth fault. for phase fault, O/C relay required.



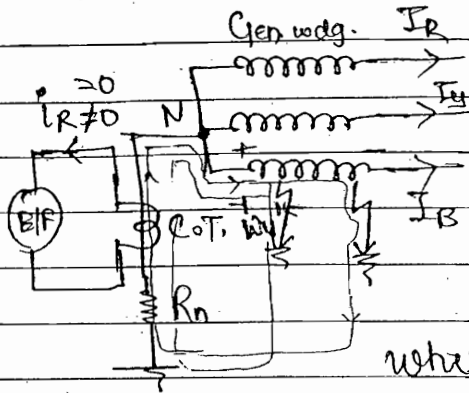
SoC Fault

- LG } → Earth fault
- LLG } → Relay
- LLL } → 2 over current

Total Relay : 3 Relays

- Earth fault relay is Basic over current or directional over current relay with flexing value b/w 2 to 10%.
- It is used to identify ground faults like (LG, LLG, LLLG). For complete protect of 3- ϕ sys. the min. no. of relays required are 3 relays i.e. one earth fault relay and two over current relays.

• Restricted Earth fault Relay: - (Generator)



% protected

% winding unprotected: -

$$= \% W_u = \frac{I_o R_n \times 100}{V_{ph}}$$

where I_o = min pick up current of Relay $\times$ C.T. Ratio

R_n = Neutral Resistance

V_{ph} = Gen. phase voltage = $V_L / \sqrt{3}$

$$\% \text{ Wdg protected} = 100 - \% W_u$$

$$\uparrow I_f = \frac{V_{ph}}{X_{th}}$$

$$\uparrow I_f = \frac{V_{ph}}{X_{th}}$$

- For improving sys. stability, Gen. Neutral is connected to the ground through resistor, i.e. Resistance grounding is used. Because of this resistance, if any ground fault occur, some % of wdg cannot be protected in the generator. For complete protection of gen wdg, % diff. relay is associated with the restricted earth fault relay.

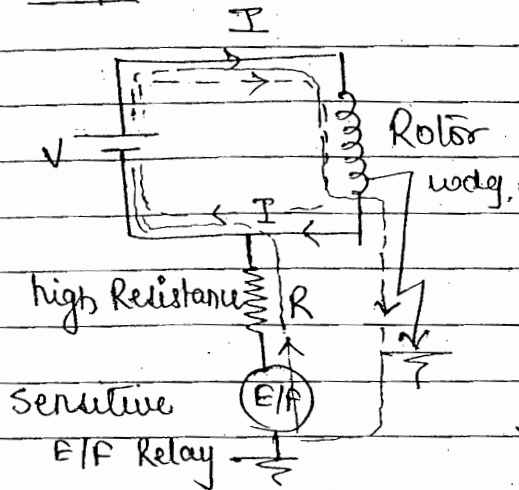
- At less no. of turns, less voltage induce, less I_f value, goes through R_n . But I_{R20} does not operate the relay.

Q.8
Pg no. 66.

$$\% W_u = \frac{0.75 \times 1000 \times 5}{11 \times 10^3 / \sqrt{3}} \times 100 = 11.8\%$$

$$W_p \%. = 100 - 11.8 = 88.2\% \text{ Ans.}$$

• Gen. Rotor E/F Relay:



• Normal condition (Blue colour)

• At fault (Red colour)

• Under Normal condition current do not flow high Relay due to high Resistance. If any fault (ground) occur the fault current flows through sensitive E/F relay and produces trip signal if it is exceeding the setting value of Relay.

• Protection of 3 ϕ - x-mer:

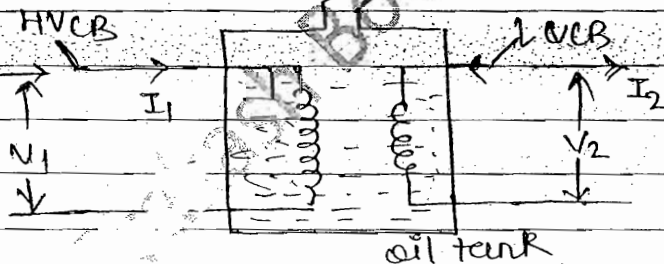
(1) HV O/C

(2) HV directional O/C

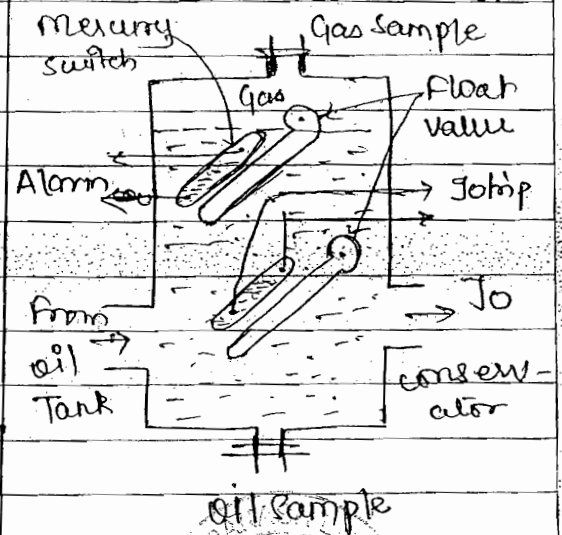
(3) HV O/V

(4) HV E/F

Buchholz
Relay
chamber



• Buchholz Relay



(5) % Diff Relay (6) Buchholz Relay

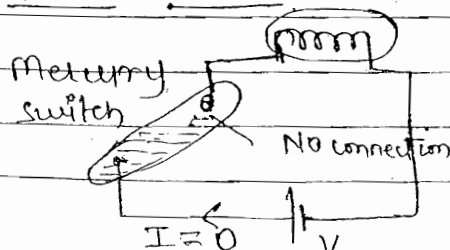
(7) Over flux Relay (8) LV O/C

(9) LV direction O/C

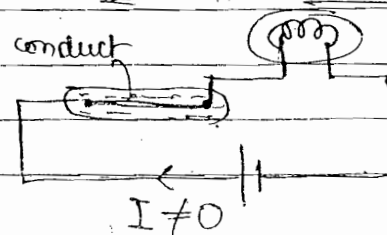
(10) LV O/V

(11) LV E/F

ALARM OFF (Block)



ALARM ON (trip)



Locatⁿ of fault

Construction parts

Winding

OLTC

Core joints

Chemicals

C_2H_2 , H_2

C_2H_2 , CH_4 , H_2

CH_2 , C_2H_6 , H_2 , CO_2

CH_2 , CH_4 , H_2 , CO_2

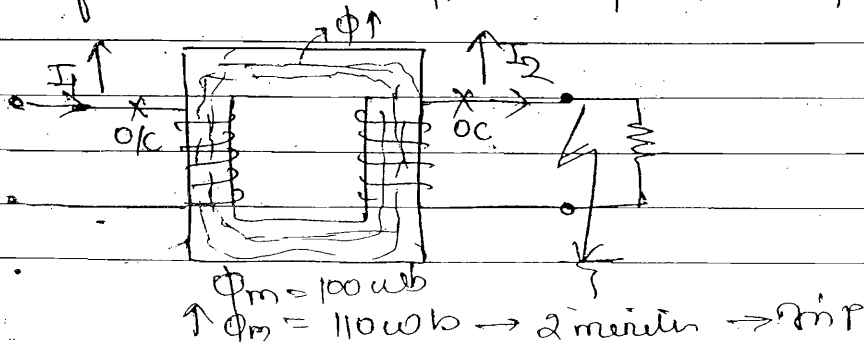
- Buchholz relay is gas actuated relay used for protection of x-mr from the internal or incipient faults
- If the intensity of fault is low value produces alarm signal initially. If the intensity of fault is very high produces trip signal by opening LV and HV C.B.
- It is most efficient for identification of internal fault. But the time of operation is more and hence it is associated with % diff. Relay for complete protection of power x-mr.

• Over flux Relay :- $V = 4.44 f \Phi_m N$ $\Phi_m \propto \left(\frac{V}{f}\right)$

(1) $V/f > 1.1$ for 2 minutes $\Rightarrow$ Trip

(2) $V/f \leq 1.1 \Rightarrow$ Block.

- At the rated voltage and freq. the flux produce in the x-mr is consider as 100%. If due to fault or freq. variatⁿ or internal damage to the x-mr. If the Φ is $\uparrow$ by 10% more than the rated value the timer is set for 2 minutes, so that produces trip signal.



• Protection of Generator:-

STATOR FAULT:-

- 1> Inter-phase fault $\rightarrow$ Split phase Relay
- 2> phase-phase fault $\rightarrow$ ϕ . diff. Relay
- 3> Earth fault $\rightarrow$ Restricted E/F Relay.

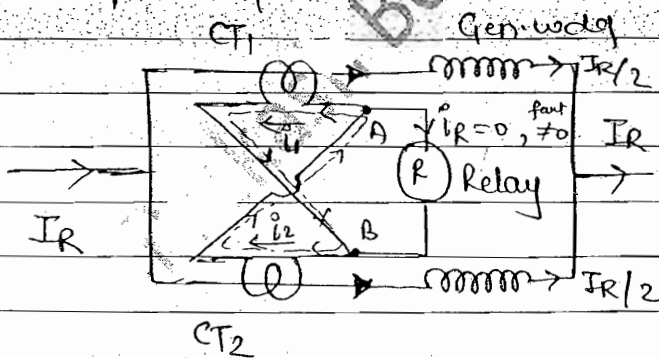
ROTOR FAULT:-

- 4> Rotor Earth fault $\rightarrow$ Sensitive E/F Relay.

EXTERNAL FAULT:-

- 5> Failure of prime voltage $\rightarrow$ Reverse power Relay
- 6> " " Excitation $\rightarrow$ Off set Mho Relay
- 7> " " Cooling Medium $\rightarrow$ Temp. Sensitive Relay
- 8> Over load $\rightarrow$ O/C Relay.
- 9> Over speed $\rightarrow$ Mech. Centrifugal Relay (Flyball Governor)
- 10> Unbalanced loading $\rightarrow$ Negative Sequence Current Relay
- 11> Over voltage $\rightarrow$ O/V Relay.

• Split - phase Relay:

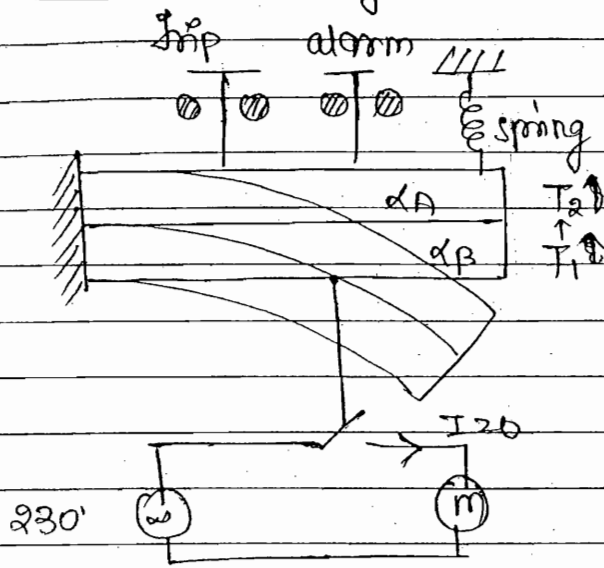


- Split phase relay is used to identify the fault occur within the same phase of the generator.
- Two CT's are connected back to back. Under normal condition the

current through relay is zero so that relay $\rightarrow$ Block

- If any S.C or O.C fault occur at any one of 11 path potential diff. occur across the relay which produce trip signal.

• Thermal Relay :-



→ Thermal relay consisting of Bi-metallic strip made of Ni and Chromium.

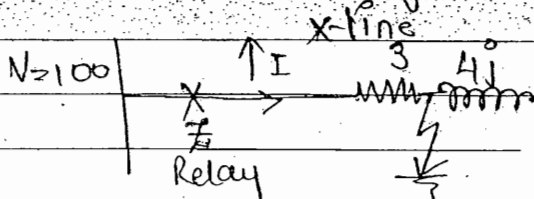
→ The thermal expansion coefficients of these metal are different so that produces bending depending on the temp. change. This principle is used in Bi-metallic switch for :-

(1) Protection of overloading of electrical motor,

Gen. etc. (2) Used in MCB (3) Used in A.C. Refrigerator and iron box for temp. control.

• For high capacity gen. more than 5MVA temp. sensitive Relay like thermocouple, RTD are used for protection of wdg. from the failure of cooling medium.

• Protection of X-line using Distance Relay :-



$Z_f = \frac{V}{I}$ Impedance seen by the relay during fault.

Z_L = Actual or replica Imped. of line without any fault.

= Setting value of Relay (PSB)

⇒ Healthy (No fault)

$$Z_L = R + jX_L = 3 + j4$$

$$|Z_L| = 5$$

$$I = \frac{100}{5} = 20 \text{ A.}$$

⇒ Fault $I \uparrow \Rightarrow I \Rightarrow 50 \text{ A.}$

$$Z_f = \frac{100}{50} = 2$$

$$|Z_f| \geq |Z_L| \rightarrow \text{Trip}$$

$$|Z_f| < |Z_L| \rightarrow \text{Block}$$

• Universal Torque Equation :-

$$T_D = K_1 I^2 + K_2 V^2 + K_3 VI \cos(\theta - \tau) - K_4$$

where T_D = operating time $K_1 I^2 = O/c$ $K_2 V^2 = O/V$
 $K_3 VI \cos(\theta - \tau)$ = Directional K_4 = Spring.
 restraining Torque.

ex:- Over Current Relay:-

Assume $K_2 = K_3 = 0$, $T_D = K_1 I^2 - K_4$

① Trip $T_D > 0$	② Block $T_D \leq 0$
$K_1 I^2 > K_4$	$K_1 I^2 \leq K_4$
$I > \sqrt{\frac{K_4}{K_1}}$	$I \leq \sqrt{\frac{K_4}{K_1}}$

I = fault current, $\sqrt{K_4/K_1}$ = PSB value of O/C Relay.

(1) Impedance (Z) Relay:-

Assume $K_3 = 0$, K_4 = very small $K_2 = -ve$

$$T_D = \underbrace{K_1 I^2}_{\text{Over current}} - \underbrace{K_2 V^2}_{\text{Restraining}}$$

Impedance Relay is a voltage Restraining over current Relay

✓ Trip ($T_D > 0$)	Block ($T_D \leq 0$) $Z_f \geq Z_L$
----------------------	---------------------------------------

$$K_1 I^2 > K_2 V^2$$

$$\sqrt{\frac{K_1}{K_2}} > \left(\frac{V}{I}\right)$$

$$\sqrt{\frac{K_1}{K_2}} = Z_L$$

$$\frac{V}{I} = Z_f$$

$$\boxed{Z_L > Z_f \text{ or } Z_f < Z_L}$$

✓ Focus of Z-Relay:-

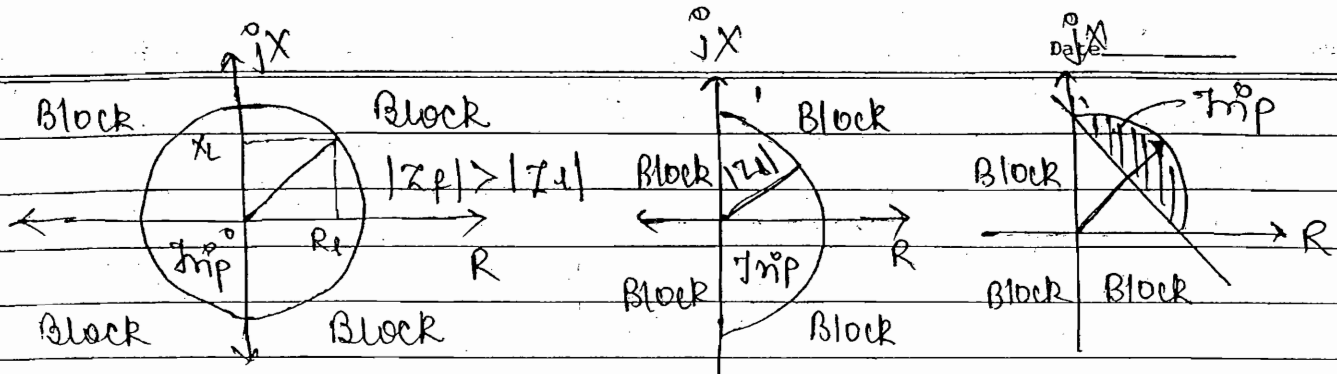
$$Z_L = R_L + jX_L$$

$$\boxed{|Z_L|^2 = R_L^2 + X_L^2} \quad \text{--- (1)}$$

eqn (1) Represents circle equation

$$x^2 = x^2 + y^2$$

$$\text{where } r = |Z_L|$$



Non-directional Z-Relay.
→ all all quadrant.

Directional Z-Relay. 1st & 4th quad.

Angle Imp. relay.
1st qu.
certain appl only.
if required.

(2) Reactance (X) Relay

Assume $K_2 \neq K_4 = 0$

$$T_D = \underbrace{K_1 I^2}_{\text{o/c}} - \underbrace{K_3 VI \cos(\theta - \tau)}_{\text{restraining}}$$

(i) Trip

$$K_1 I^2 > K_3 VI \cos(\theta - \tau)$$

$$\frac{K_1}{K_3} > \frac{V}{I} \cos(\theta - \tau)$$

Reactance Relay is a Directional
Restraint over Current Relay.

Assume $\tau = 90^\circ$, $\frac{V}{I} = Z_f$

$$\frac{K_1}{K_3} = X_f$$

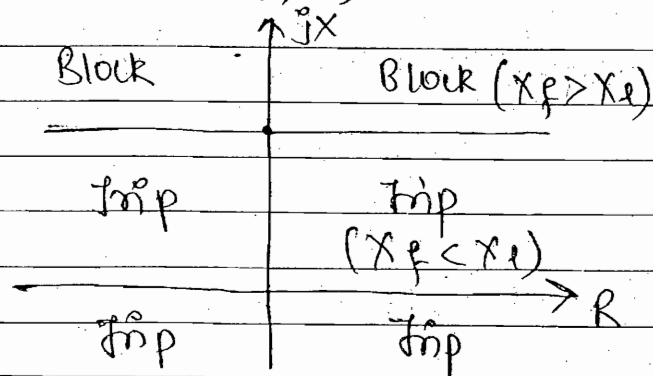
Zone of X-Relay is a
straight line passing through
(0, X_f)

$$X_1 > Z_f \cos(\theta - 90^\circ)$$

$$X_1 > Z_f \sin \theta$$

$$Z_f \sin \theta = X_f$$

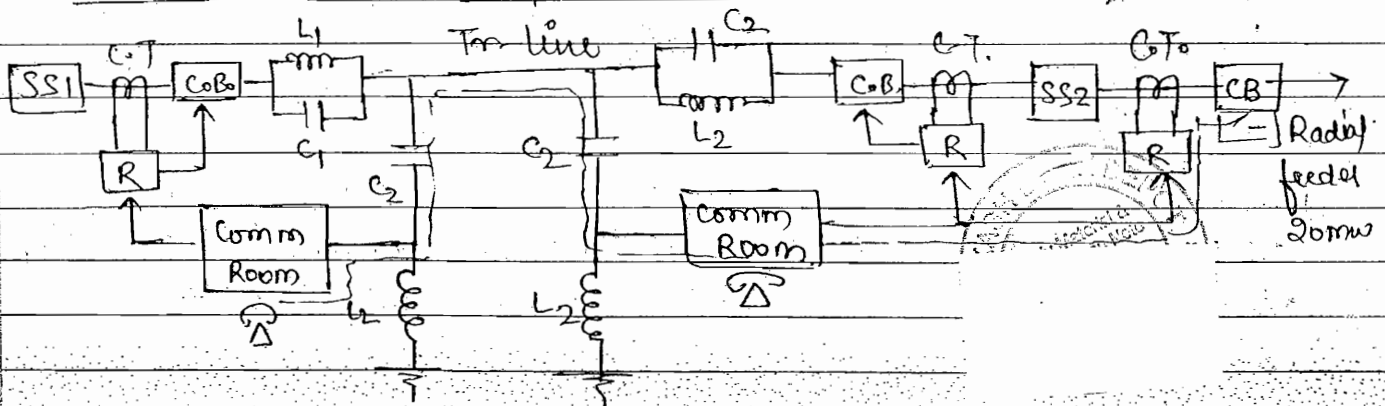
$$\boxed{X_1 > X_f \text{ or } X_f \leq X_1 \Rightarrow \text{Trip}}$$



$$\textcircled{2} \text{ Block } \boxed{X_f \geq X_1}$$

- Under Normal condition syn. gen. delivers active and reactive pow. to the load. If the turbine is present, excitation is failed. Then it will deliver leading VAR's and absorb lagging VAR's. And also deliver the active power. This change of reactive power flow with in the gen. produces unbalanced causes damage to the gen. wdg. To protect the gen. from this effect Mho relay is used, which is basically a mho relay for which an offset is added for identification of loss of excitation.

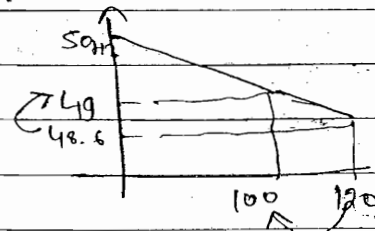
• Current Carrier Protection :-



- Line Trap $f_1 = \frac{1}{2\pi\sqrt{L_1C_1}} \Rightarrow 50\text{Hz.}$
- Wave Trap $f_2 = \frac{1}{2\pi\sqrt{L_2C_2}} \Rightarrow \text{Audio freq.}$

• Current Carrier protection is used :-

- (1) power line carrier protection
- (2) SCADA
- (3) load frequency control

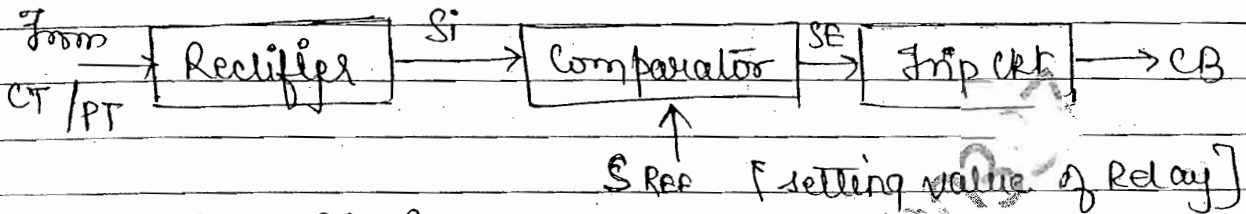


- It consisting of line trap and wave trap LC tuned ckt. line trap unit offers low impedance for

power freq. and high Imp. for the communicatⁿ freq..

The wave trap unit is used low impedance for audio freq. and high Imp for power freq.

• Static Relay:-



$$SE = Si - S_{REF}$$

- ① If $Si > S_{REF} \Rightarrow SE > 0 \Rightarrow \text{Trip}$
- ② If $Si < S_{REF} \Rightarrow SE < 0 \Rightarrow \text{Block}$

• Advantages:-

- ① low power consumption.
- ② store data
- ③ Easily interface with comp.
- ④ More reliable
- ⑤ less maintenance.
- ⑥ Easily programmable
- ⑦ less cost
- ⑧ Occupies less space
- ⑨ stable operation

Date. _____

$P_L \propto (F+25)$ Corona power loss is more in HVAC compared to HVDC.

Disadvantages of Corona

- 1) Power loss occurs
- 2) Produces interference to other lines.
- 3) Charging current increases. f Advantage
- 4) Intensity or peak value of the lightning surge is reduced if lightning surge initiates corona.

Economic / Variable load factor

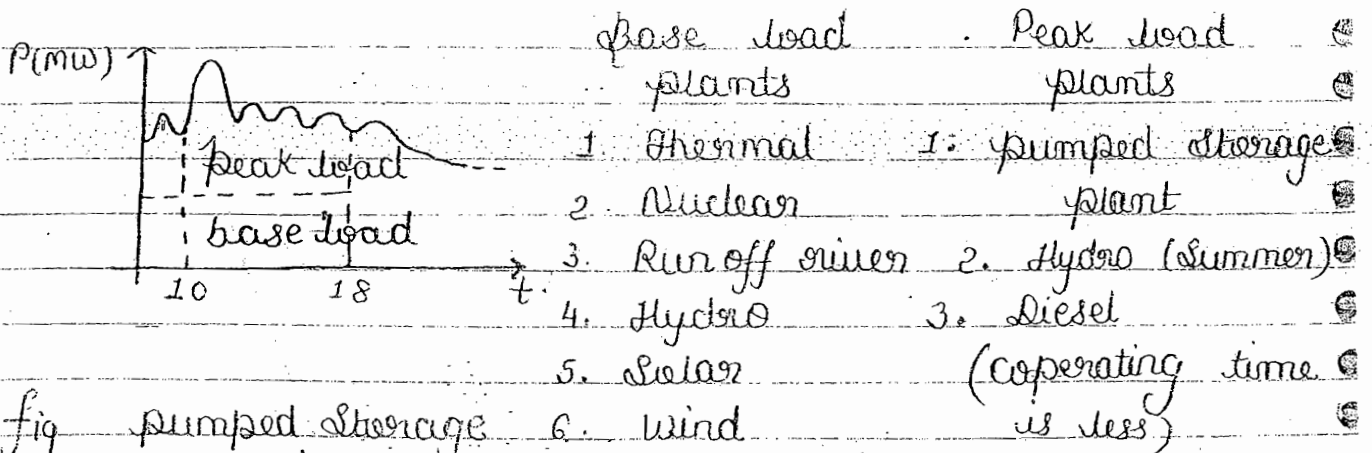
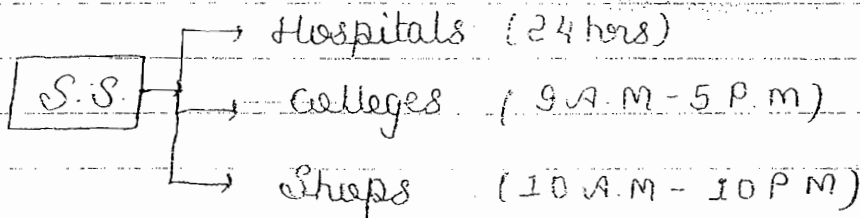
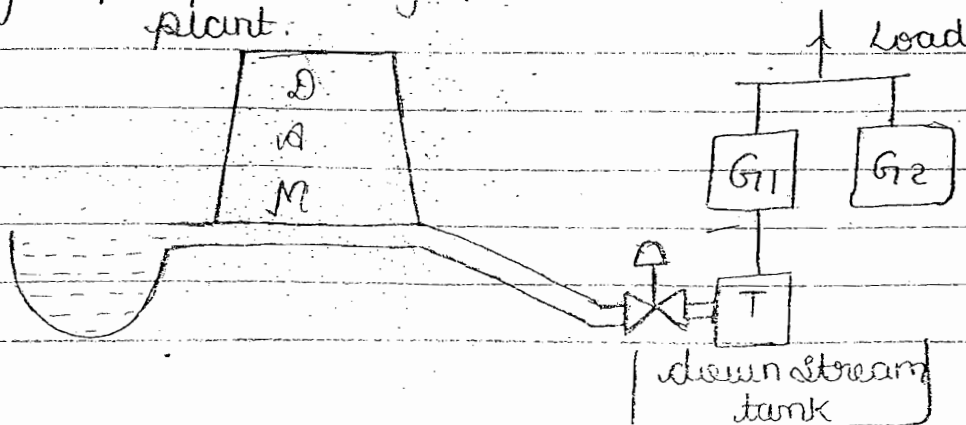


fig pumped storage plant.



Pumped storage plant is also hydro plant

→ Thermal and nuclear operaⁿ time is more (expensive) so they are used as a base load plant.

→ Depending upon availability hydro is used as base or peak load plant.

1) Plant load factor : (P_{lf})

$$P_{lf} = P_{avg} / P_{max}$$

$$= \frac{P_{avg} \times t}{P_{max} \times t}$$

$$P_{lf} = \frac{\text{area under load curve}}{(\text{Rectangular area corresponding to } P_{max})}$$

2) Plant Capacity factor (P_{cf}) →

$$P_{cf} = \frac{P_{avg}}{P_c} \quad P_c = \text{Plant capacity}$$

avg energy produced in total hours
(energy able to produce as per P_c in total hours)

$$\boxed{P_{cf} < 1}$$

3) Plant use factor (P_{uf})

(P_{uf})

$$P_{uf} = \frac{\text{Energy produced in used hours}}{(\text{energy able to produce as per } P_c \text{ in used hours})}$$

$$\boxed{P_{uf} < 1}$$

4. Reserve Capacity R_c : $R_c = P_c - P_{max}$
 $= \frac{P_{avg}}{P_{cf}} - P_{max}$

$$R_c = \frac{P_{avg} - P_{max} P_{cf}}{P_{cf}}$$

$$= P_{max} \left[\frac{P_{avg} - P_{cf}}{P_{max} P_{cf}} \right]$$

$$= \frac{P_{max} (P_{lf} - P_{cf})}{P_{cf}}$$

5. Demand Factor : (D_f)

$$D_f = \frac{P_{max}}{\text{Sum of connected load}}$$

$$\boxed{D_f < 1}$$

6. Diversity factor : (Div_f)

$$(Div_f) = \frac{\text{Sum of individual max demand}}{P_{max}}$$

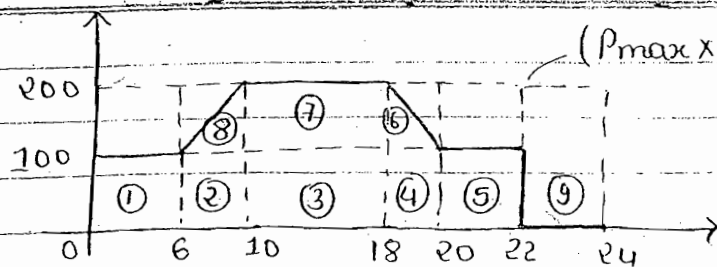
$$\boxed{Div_f > 1}$$

Ques: A Generating Station has a plant installation capacity of 300 MW is delivering the power to the load centre. A load curve is shown in the fig calculate

(i) P_{max} (ii) Plant capacity (iii) P_{avg} (iv) P_{lf}
 (v) P_{cf} (vi) P_{vf} (vii) R_c

Solu:- $P_{max} = 200 \text{ MW}$
 $P_c = 300 \text{ MW}$

$p_{avg} = \text{Total area / Time}$



$$\begin{aligned}
 & 100 \times 6 + 4 \times 100 + 8 \times 100 \\
 & + 100 \times 2 + 100 \times 2 + 0 \times 2 \\
 & + \frac{1}{2} \times 100 \times 4^2 + \frac{1}{2} \times 2 \times 100 \\
 & + 100 \times 8
 \end{aligned}$$

$$4) \quad P_{lf} = P_{avg} / P_{max}$$

$$= \frac{3300}{24} = 137.5 \text{ MW}$$

$$= \frac{137.5}{200} = 0.6875 < 1$$

$$\text{or } \frac{P_{avg} \times 24}{P_{max} \times 24}$$

$$= \frac{3300}{200 \times 24} = 0.6875$$

Total hours

$$5) \quad P_{cf} = P_{avg} / P_c = \frac{137.5}{300} = 0.4583 < 1$$

$$\text{or } R_{cf} = \frac{3300}{300 \times 24} = 0.4583$$

Total hours

$$6) \quad P_{uf} = \frac{3300}{300 \times 22} = 0.5 < 1$$

used hours

(area remains same)

$$7) \quad R_c = P_c - P_{max}$$

$$= 300 - 200 = 100 \text{ MW}$$

$$\text{or } R_c = \frac{P_{max} (P_{lf} - P_{cf})}{P_{cf}} = \frac{200 (0.6875 - 0.4583)}{0.4583} = 100 \text{ MW}$$

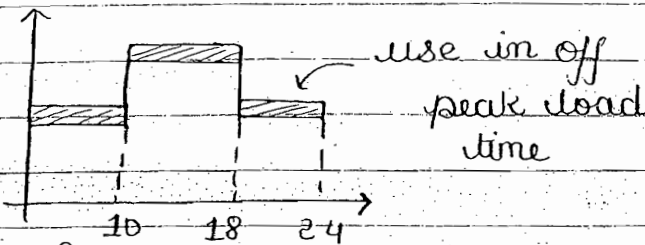
	connected load (kW)	Individual max demand
US → hospitals		
→ colleges	50	40
→ Shops	40	30
	30	25

$$\Sigma = 120 \text{ P(kw)} \quad \Sigma = 95$$

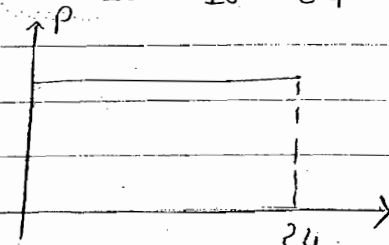
$$Df = \frac{70}{120} < 1 \quad \text{Divf} = \frac{95}{70} > 1$$

Connected load (equipments upto their full capacity)

Individual load demand is diversified. (Divf)



$$P_{Lf} < 1 < 100\%$$



$$P_{Lf} = 1 = 100\%$$

$$P_{Lf} = \frac{P_{avg}}{P_{max}}$$

$$\uparrow \text{Divf} = \frac{\Sigma \text{ 9nd. max}}{P_{max} \downarrow}$$

Practically P_{Lf} more than 1 is also possible. Higher P_{Lf} is better.

Methods of Improving P_{Lf} and diversity factor

If P_{Lf} and diversity factor are higher, indicates max demand is lower so that initial investment on the electrical appliances is reduced which reduces cost of electrical energy.

Because of this reason $P_{Lf} = 1$ or higher than 1 and diversity factor > 1 is preferred.

Chem $\rightarrow$ heat $\rightarrow$ mech $\rightarrow$ Elec
Boiler - Turbine Gen

Increasing industries for running their offices and industrial during off peak load time

Agricultural pumpsets are to be run during off peak load period.

Effective utilisation of sunlight by maintaining proper ventilation betwⁿ the buildings.

Increasing the industries for utilising high Pf loads

Power Generation

Thermal Plant

- H/W $\rightarrow$ hot well
- DM $\rightarrow$ Demineralised $\rightarrow$ (to avoid corrosion of boiler)
- CEP $\rightarrow$ Condensate Extn. pump
- CWP $\rightarrow$ circulating water pump
- BFP $\rightarrow$ Boiler feed pump
- LPH $\rightarrow$ Low pr heater
- HPH $\rightarrow$ High pr heater
- D $\rightarrow$ Deaerator
- ECO $\rightarrow$ Economiser
- LPT $\rightarrow$ Low pressure turbine
- IPT $\rightarrow$ Inter " "
- HPT $\rightarrow$ High " "
- V $\rightarrow$ vacuum pump / steam ejector
- HPCV - High pr Govn. control valve
- IPC - Inter pressure " " "
- HTSH - High temp Super Heater
- ITSH - Inter " " "
- PA - Primary air

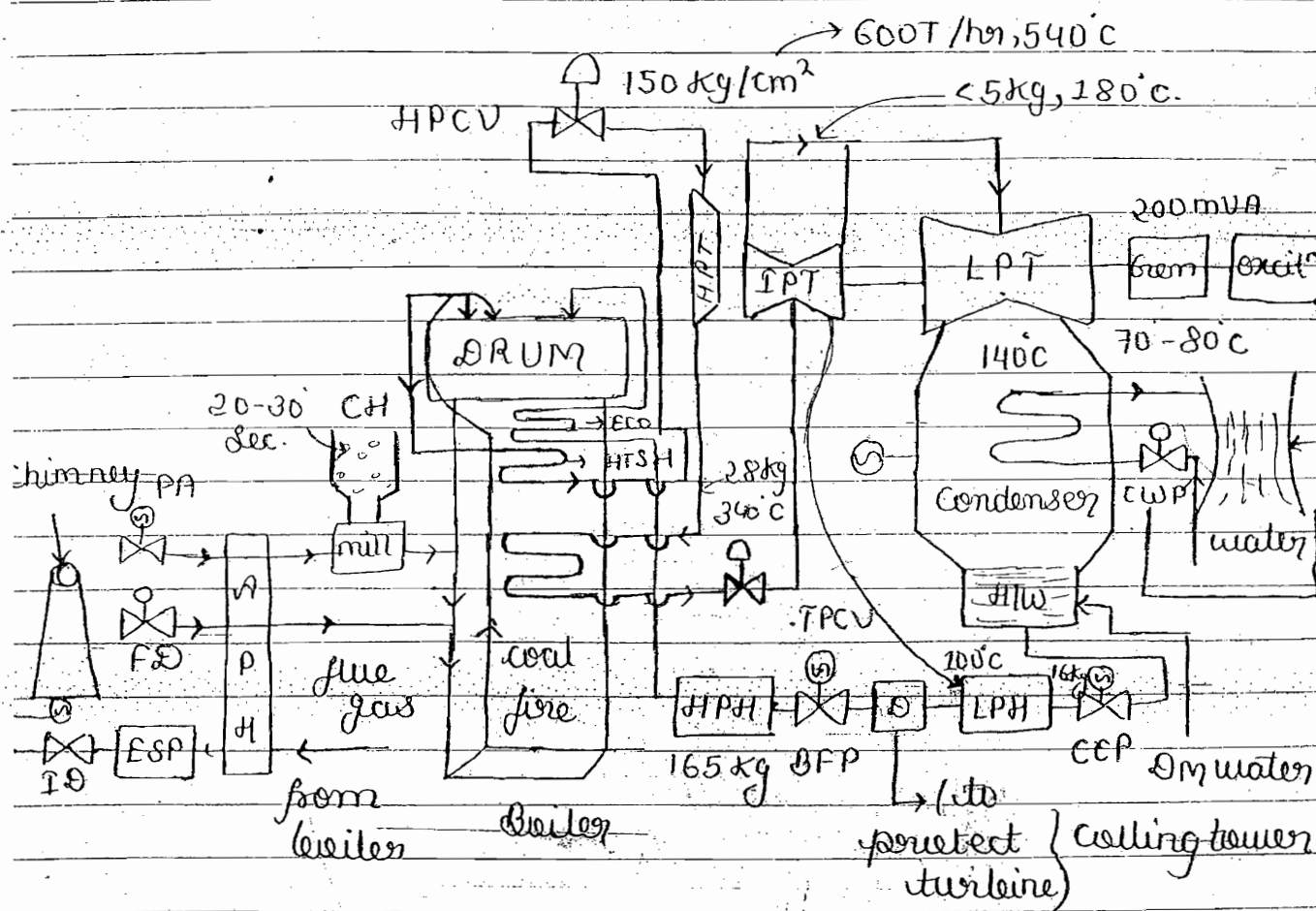
FD - forced draft

ID - induced draught

ESP - Electrostatic Precipitator

APH - air pre heater

CH - Coal Hopper



Thermal Plant is working on the principle of Rankine Cycle. That is the process of reheating steam for improving efficiency. Thermal eff is betwⁿ 35-40%.

Anthracite - <10%.

Bituminous - 20-30%

Lignite - 30-50%

Peat > 50%.

for burning of coal
(as like woodstick)

Energy of coal $\Rightarrow$ kcal/kg

1 unit = 1 kWh = 860 kcal heat energy.

Ex.

Bituminous :

Energy $\rightarrow$ 2 kWh/kg = 1720 kcal/kg

$\eta = 40\% = 2 \times 0.4 = 0.8$ kWh/kg

1 kg = 0.8 kWh $\rightarrow$ 1 kWh = $1/0.8 = 1.25$ kg coal.

P = 200 MW , 1 day = 24 hr

energy = $200 \times 24 = 4800$ MWhr = 4800×10^3 kWh

coal = $4800 \times 10^3 \times 1.25$ kg = 6000 T/day
(tonnes/day)

Ash = $\frac{6000 \times 200}{100} = 1200$ T/day

(Huge amount of ash produced)

²³⁵U₉₂ - 1 kg = 270 000 kg coal (less requirement of coal so transportation cost is

more)

$$\eta_o = \eta_{th} \times \eta_c$$

$$\eta_o = \eta_B \times \eta_{\text{turbine}} \times \eta_g$$

$\eta_o =$ over all η

$\eta_B =$ Boiler η , $\eta_g =$ Generation η

$\eta_{th} =$ Heat $\eta =$ boiler & thermal η

- For protecting boiler tubes from corrosion Zn water is used.

For improving η_{th} , LP and HP heaters are used

so that water temp. is increased.

These heaters are of steam heaters

Deaeration is used for removal of dissolved gases from the water for protection of turbine.

BFP is the highest pressure generating pump in the thermal plant which nearly consumes 4mw electrical power & produces upto 165 kg of pressure.

Economiser used for absorbing heat from flue gases so that water temp is increased for improvement of thermal efficiency.

Water circulates naturally from drum to boiler and again to the drum due to density difference of water and steam. In high capacity plants extra pumps is used for this purpose HTSH heater improves steam temp upto 540°C.

Steam is reheated in the HTSH for improving the thermal efficiency. This is the principle of Rankine cycle.

Steam directly sent from IP turbine to LP turbine. Vacuum pump is used for absorbing steam from the L.P turbine to Condenser.

- Circulating water is used for conversion of Steam into water. This water is sent to the boiler. circulating water is cooled by using cooling turbine.
- PA fan is used for conveying coal hopper from mill to boiler.
- Fb fan is used to supply oxygen for proper combustion of coal.
- ID fan is used to extract flue gas from boiler.
- ESP working on the principle of electrical field used for collection of ash from the flue gas. APH used to increase the PA & Fb fan, air temp so that moisture from the coal is removed.
- HPCV and IPCV are used for controlling flow rate of Steam into the turbine so that speed of freq. are controlled.

Hydro Power Generation

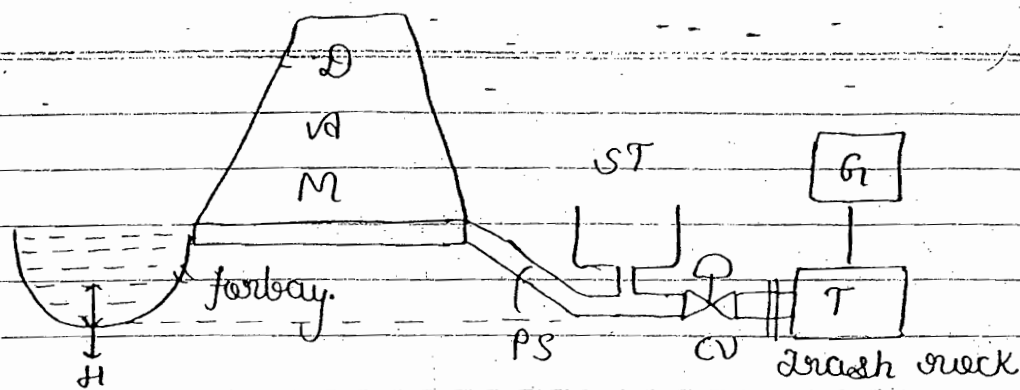
Potential $\rightarrow$ kinetic $\rightarrow$ Mech $\rightarrow$ Elec.

PS $\rightarrow$ penstock

ST $\rightarrow$ surge tank

CV $\rightarrow$ Control Valve

H $\rightarrow$ mean water head



Electrical Power Output (P) → (avoid entering waste material)

1) Discharge (Q) is given -

$$P = 0.735 \eta QWH$$

$$= 9.81 \times 10^{-3} \eta QWH \text{ kW}$$

η → plant efficiency

Q → discharge of water in m^3/sec

= $\frac{\text{Capacity of reservoir in } \text{m}^3}{3600 \text{ Sec.}}$

W = density of water = 1000 kg/m^3

H = mean water head in m.

2) Rainfall (F) is given -

$$P = 3.14 \times 10^{-3} \eta QWH KAFH \text{ --- kW}$$

η → plant η

K → yield factor (what we get)

A → attachment area sq. km.

F → annual rainfall in mm

H → mean water head in m

$$\left[\begin{array}{l} \text{Energy} = \text{Power} \\ \times t \end{array} \right]$$

$H \rightarrow$ variable

Head (m)	Turbine
2-15	propeller or kaplan
15-70	kaplan or francis
70-500	francis or pelton
>500	Pelton
Pumped storage	DERIZ

$H < 30 \rightarrow$ low head

$30 < H < 300 \rightarrow$ medium head

$H > 300 \rightarrow$ high head.

